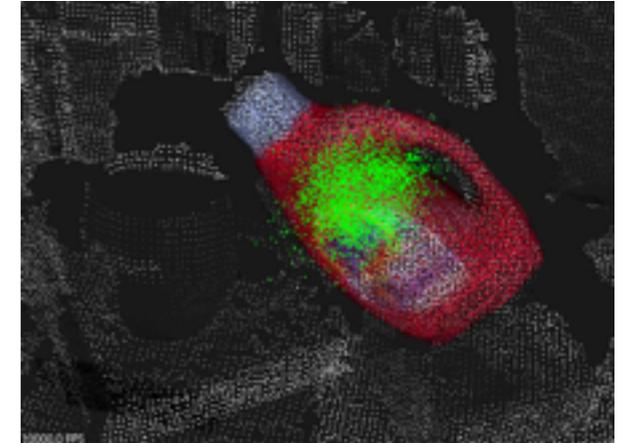
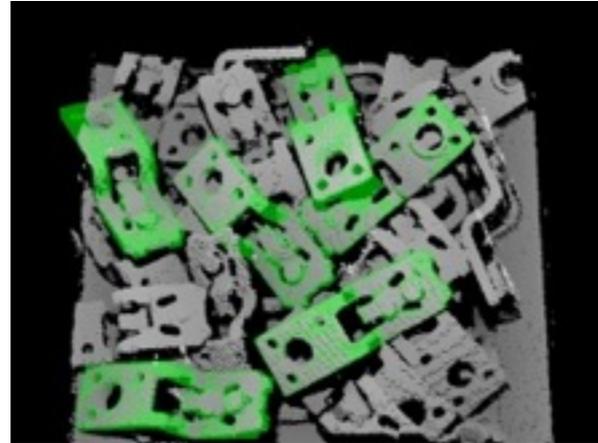


# Visual Object Perception in Unstructured Environments



**Changhyun Choi**

Robotics Ph.D. Program

Interactive Computing, College of Computing

Georgia Institute of Technology

**Prof. Henrik I. Christensen (Advisor)**

**Prof. James M. Rehg**

**Prof. Irfan Essa**

Interactive Computing

College of Computing

Georgia Institute of Technology

**Prof. Anthony Yezzi**

Electrical and Computer Engineering

Georgia Institute of Technology

**Prof. Dieter Fox**

Computer Science and Engineering

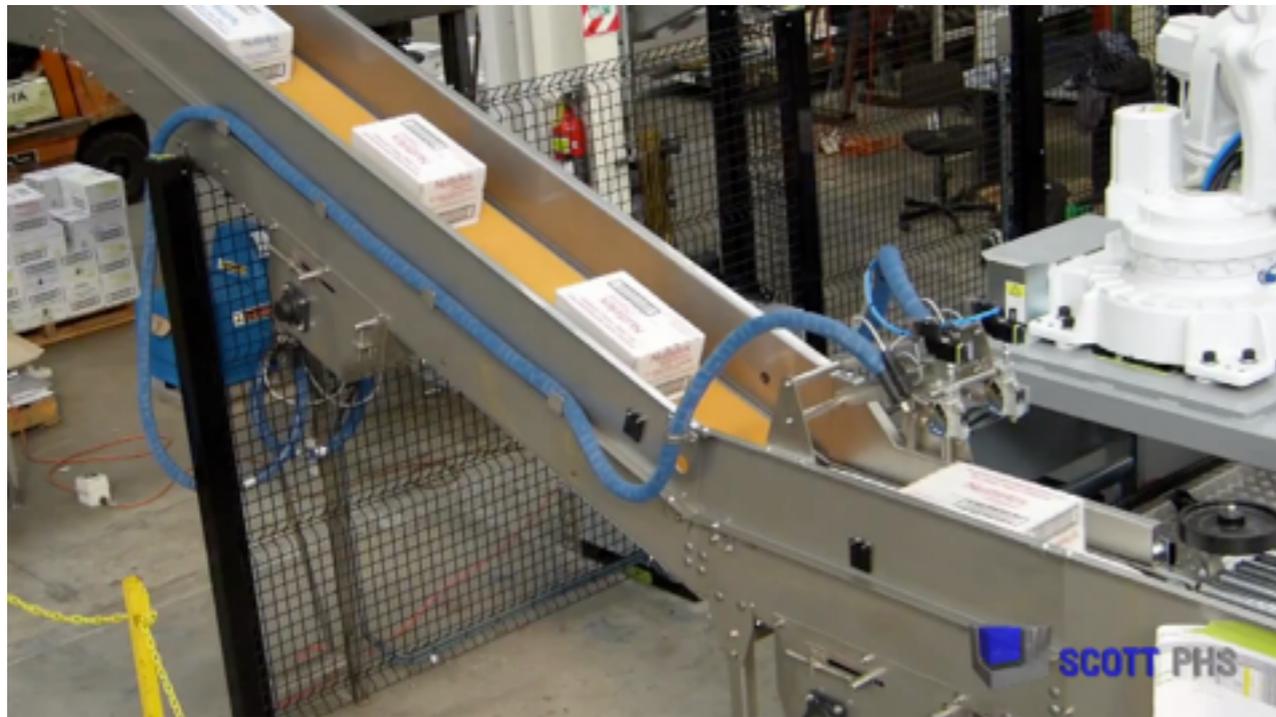
University of Washington

# Outline

- Introduction
- State of the art
- Remaining challenges
- Motivations
- Thesis statement
- Approaches
- Conclusions & Future work

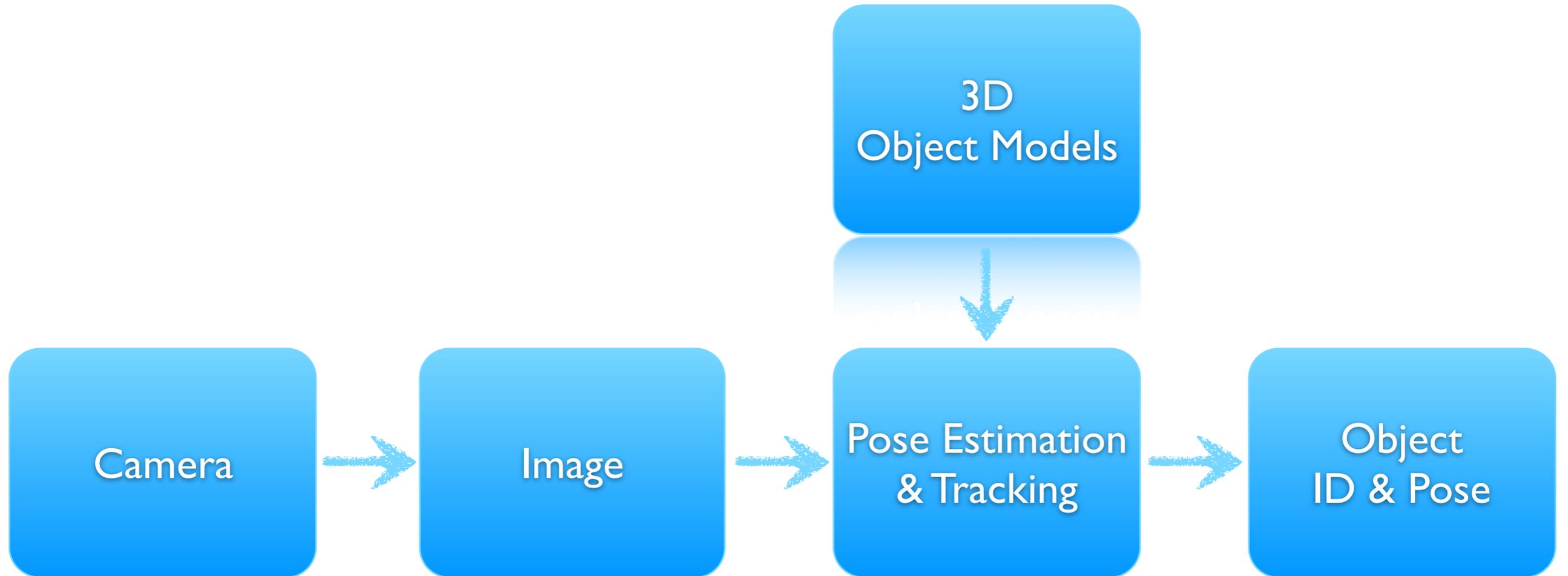


# Introduction

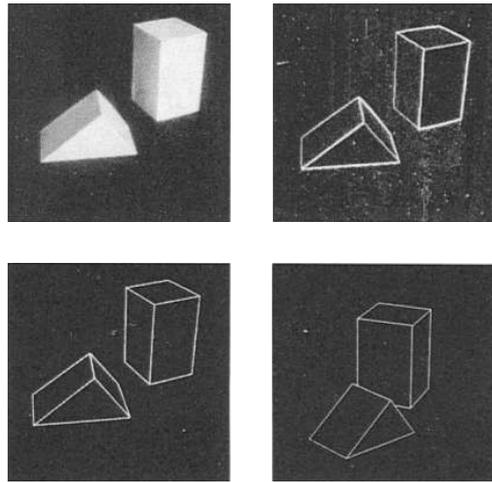


- Pick-and-place task
- Robots moving from **controlled** settings to **unstructured** environments
- **Robust** object perception is crucial

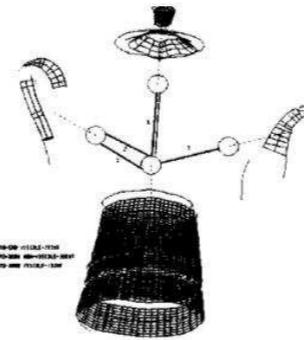
# Problem Formulation



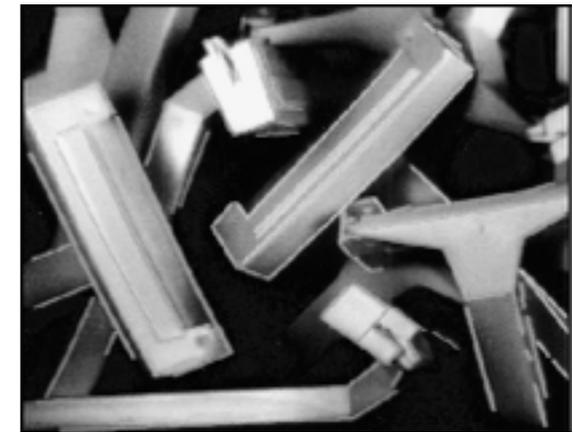
# Early Object Perception



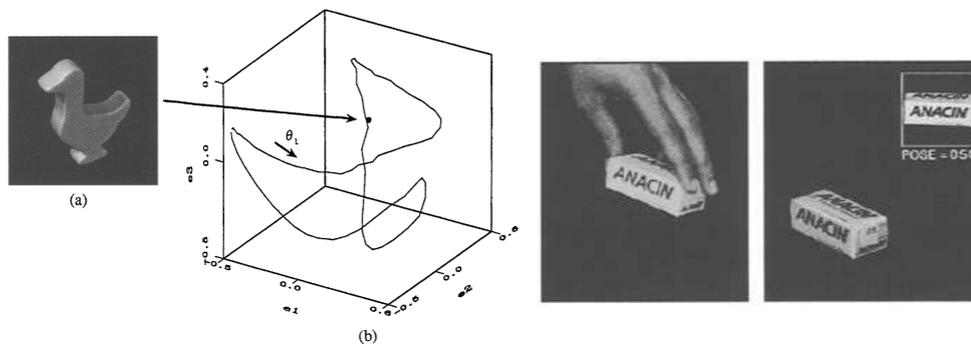
Convert 2D photo to 3D model  
 perspective projection  
 edge detection, line fitting  
 6-DOF transform  
 [Roberts 65]



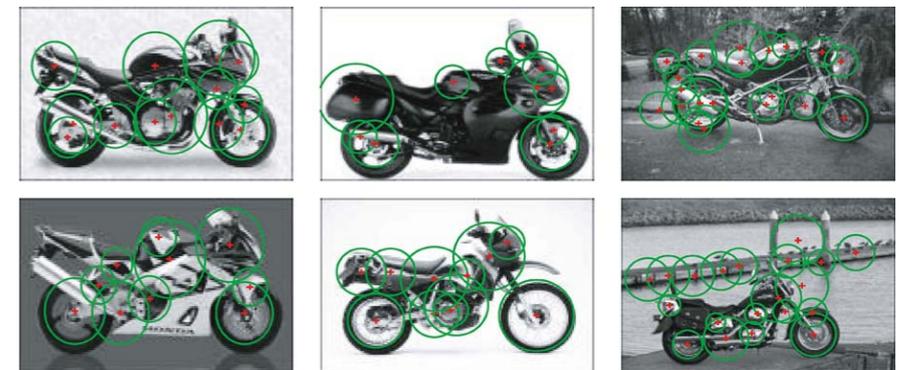
*Categorical 3D* shape models: GC, geon  
 viewpoint invariant  
 textureless objects  
 [Binford 71, Brooks 83, Biederman 85,  
 Dickinson et al. 92, ...]



*Exact 3D* shape models: polyhedron or CAD  
 viewpoint invariant  
 textureless objects  
 [Lowe 87, Thompson and Mundy 87,  
 Huttenlocher and Ullman 90, , ...]



*Exemplar 2D* appearance model: 2D templates  
 viewpoint dependent  
 textured objects  
 [Murase and Nayar 95, Ohba and Ikeuchi 97,  
 Black and Jepson 98, ...]



*Categorical 2D* appearance model:  
 spatial models with local appearance features  
 viewpoint dependent  
 textured objects with clutter and occlusion  
 [Lowe 99, Mikolajczyk and Schmid 04,  
 Fei Fei et al. 06, Fergus et al. 07, ...]

# State of the Art

## [Collet et al., IJRR'11]



- SiftGPU feature
- Sparse 3D keypoint models
- Iterative Clustering
- **Require** well textured objects
- **Cannot handle** textureless objects

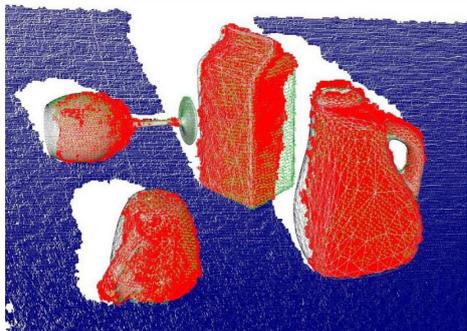
## [Hinterstoisser et al., PAMI'11]



- Template Matching
- Combine *image gradients* and *surface normals*
- Can handle untextured objects
- **Require** large amount of templates (e.g. 2000)
- **Coarse** pose estimation
- Produce **jitter noises** in pose estimates

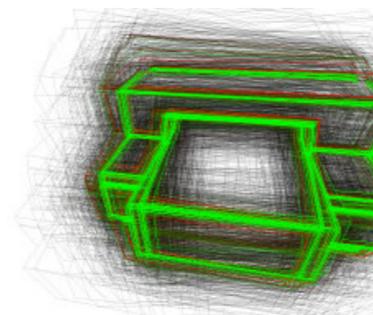
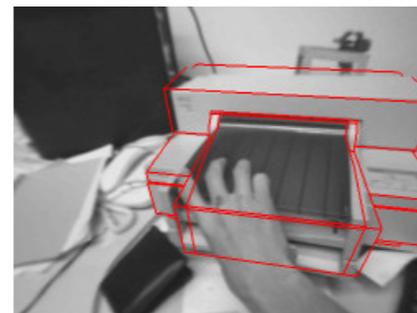
## [Aldoma et al., ICCV workshop'11]

## [Lai et al., AAAI'11]



- Table-top assumption
- Object segmentation + CVFH/kernel descriptors
- **Require** planar background
- **Hard** in cluttered environment

## [Klein et al., BMVC'06]



- Particle Filter
- Arbitrary shaped object
- **Require** a given starting pose
- **Do not** address challenging cases

# Remained Challenges

1. Object with and without Textures
2. Background Clutter
3. Object Discontinuities
4. Real-time Constraints



# Challenge 1: Texture



Handling both **textured** and **textureless** objects

- Textured objects
  - **Photometric:** *color, keypoints, edges* or textures from surfaces
- Textureless objects
  - **Geometric:** *point* coordinates, surface *normals*, depth discontinuities

# Challenge 2: Clutter



**Controlled** environments



**Unstructured** environments



**Difficulties = Degree of Clutter**

- False measurements
- False pose estimates
- Stuck in local minima
- No table-top assumption

# Challenge 3: Discontinuities



Occlusions



Out of FOV



Blur

- **Ideal vs Reality**
  - **Occluded** by other objects, human, or robots
  - Object goes **out** of the camera's field of view
  - **Blurred** in images
- **Re-initialization** problem

# Challenge 4: Real-time



- Constrained by timing limitations
- Scarcely see real-time state-of-the-art

# Definition and Scope I

monocular  
or RGB-D

object instance recognition

6-DOF p.e.  
and tracking

Model-based Visual Object Perception  
in Unstructured Environments



3D mesh models

cluttered &  
obj. discontinuities

# Definition and Scope 2

photometric image formation in 2D

intensity, color, edges from texture, keypoint descriptors, ...



Visual features: Photometric & Geometric

3D geometric shapes

depth points, edges from geometric shapes, line segments, planes, normals, ...

# Motivations

Known 3D object model **was** strong assumption



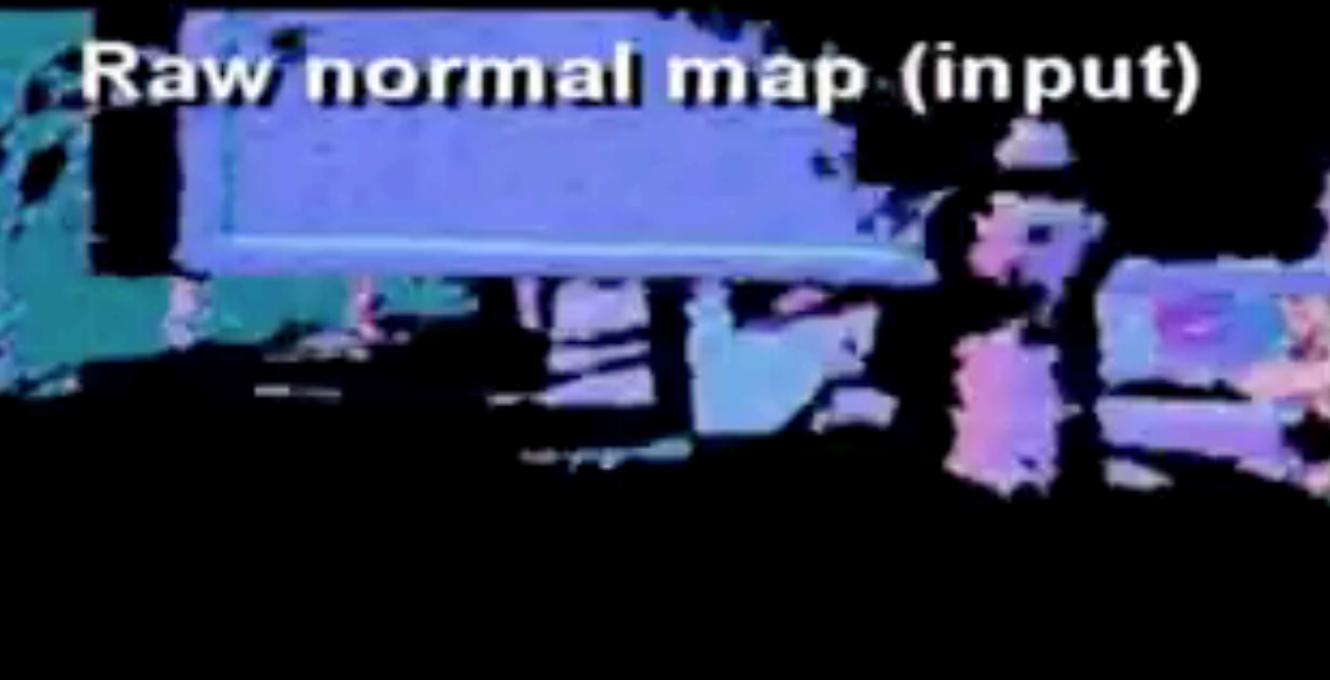
3D object models have been *accumulated* on the Internet!

# Motivations



Google 3D warehouse

(about 2.5 million models)



[Izadi et al., SIGGRAPH Talks 2011]

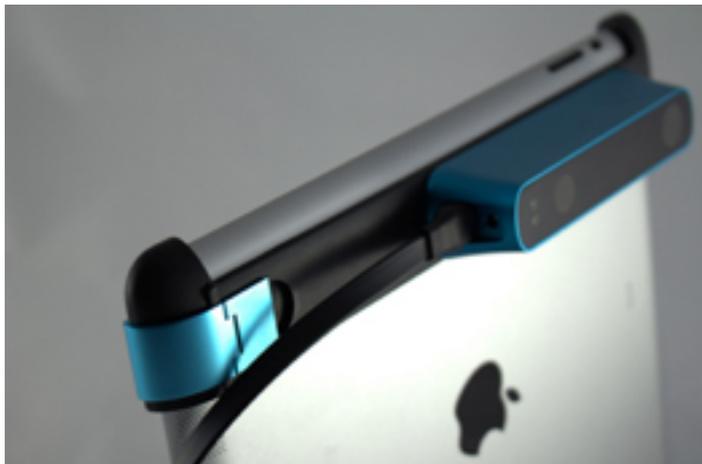
3D modeling will be a **trivial** task with **Kinect!**

# Motivations

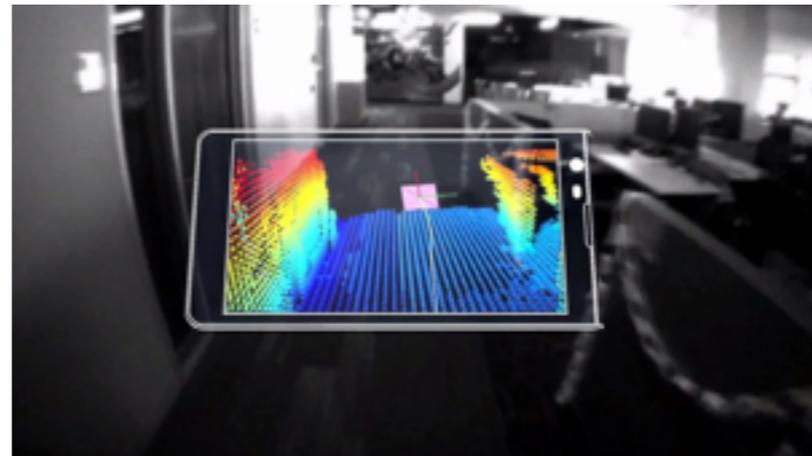


24 million Kinects sold

Depth sensors are **everywhere!**



Occipital, Inc



 Google Project Tango



Apple + PrimeSense



# AUTODESK® 123D® CATCH



[ AUTODESK 123D CATCH ]

3D modeling will be a **trivial** task **even** with a **mobile phone!**

# Motivations

- Promising in Robotics
  - exist in 3D space
  - interact with 3D world
  - 3D data is significant information for robots
- Advantages
  - Foreground object segmentation is trivial
  - Employ various **geometric** features from (3D models and 3D scene depth)



# Thesis Statement



- To close the loop between the **geometric era** of early computer vision and the currently dominating **appearance age**, both **photometric** and **geometric** features need to be considered.
- The **combination** of these features enables object perception algorithms not only to be **more effective** but also to handle an **increased spectrum of objects**.
- **Two theoretical frameworks** using **multiple pose hypotheses** based on combined features are contributed in this thesis.
- These new frameworks are **robust** to significant **clutter** and **occlusions**, and are therefore **efficacious** solutions for visual object perception in **unstructured** environments.

# Approaches

photometric

geometric

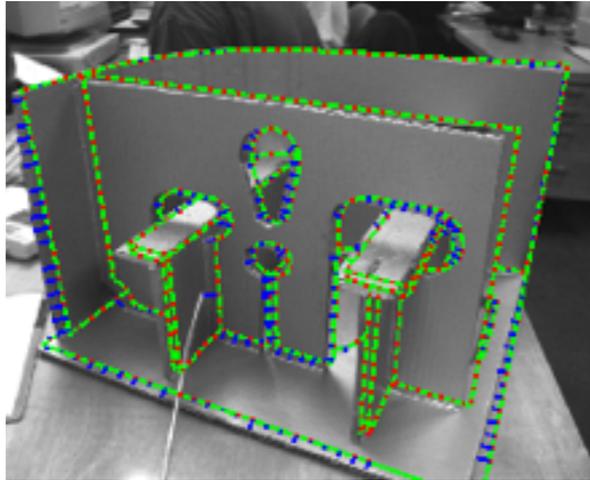


- 2D Visual Information (Monocular Camera)
  - **Combining Keypoint and Edge Features**  
[ICRA'10, ICRA'11, IJRR'12]
  - Extending to Textureless Objects  
[IROS'12]



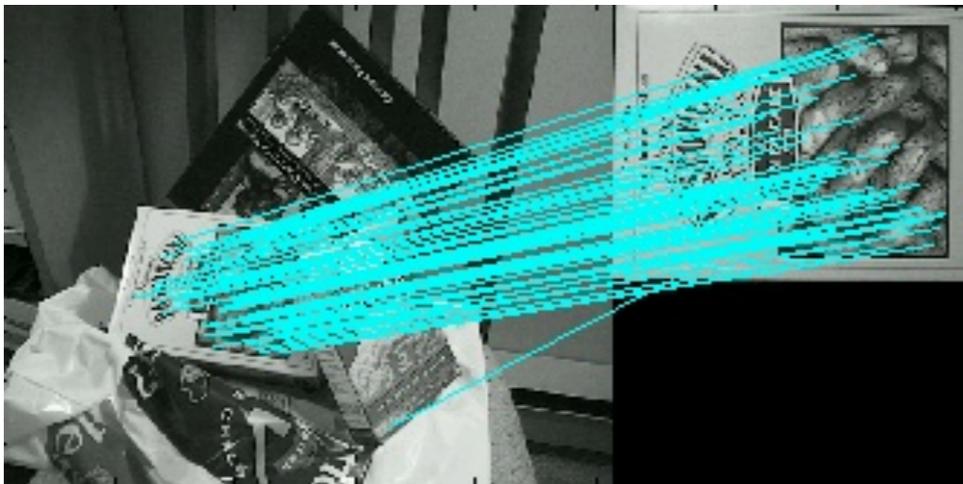
- 3D Visual Information (RGB-D Camera)
  - Voting-based Pose Estimation using Pair Features  
[ICRA'12, IROS'12]
  - Object Pose Tracking  
[IROS'13]

# Related Work



[Harris, 92] [Drummond, PAMI'02]

- **Edge-based** approaches
  - Cheap to extract edges (real-time)
  - Applicable to textureless objects
  - Not distinctive enough
  - Might be stuck in local minima

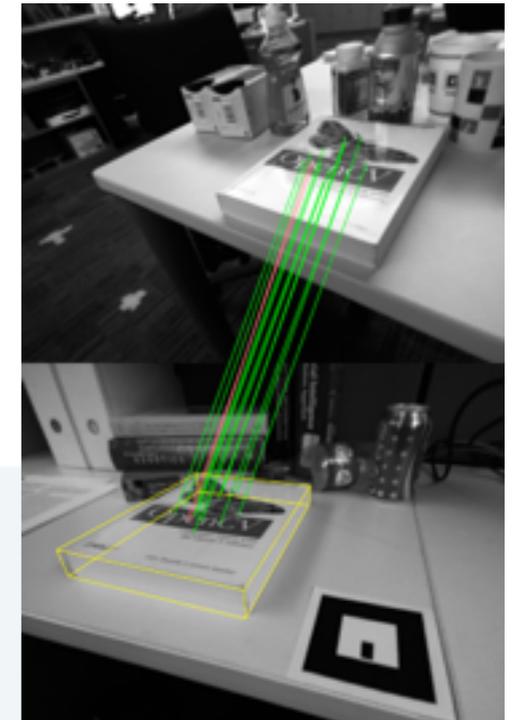
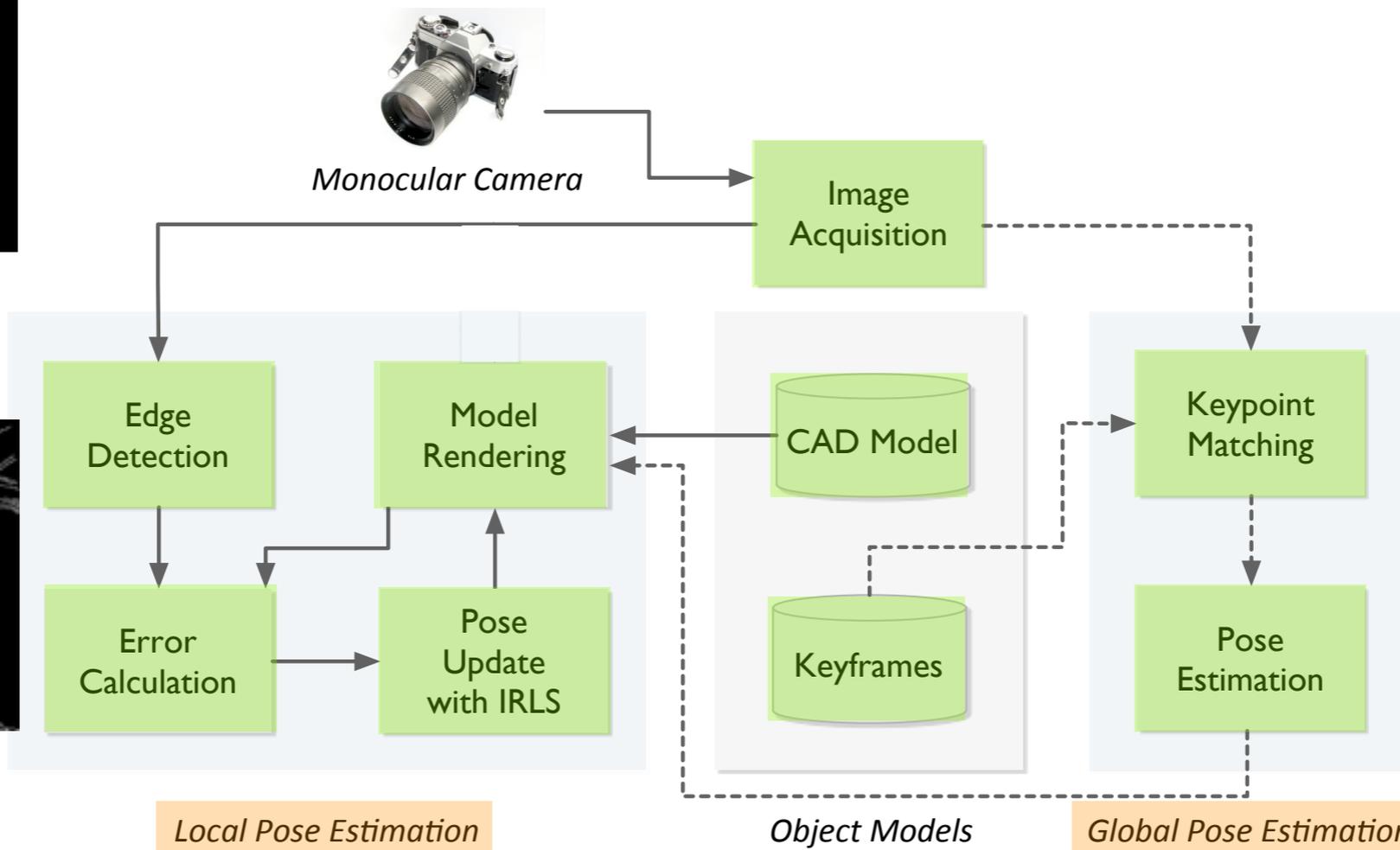
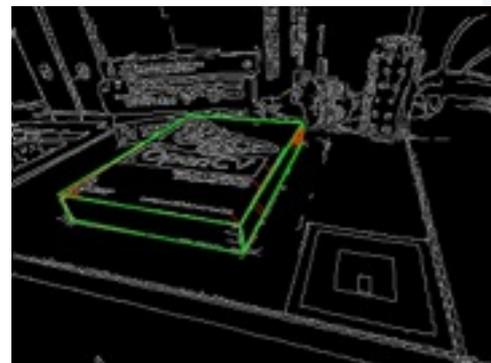
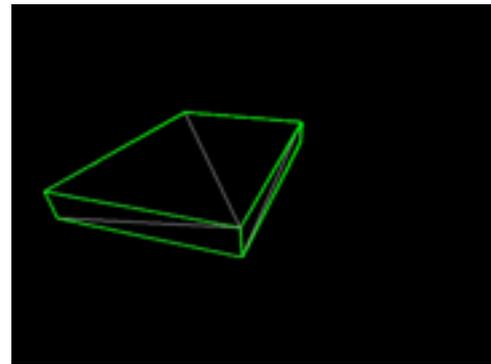


[Lowe, IJCV'04] [Gordon, 06] [Collet, IJRR'11]

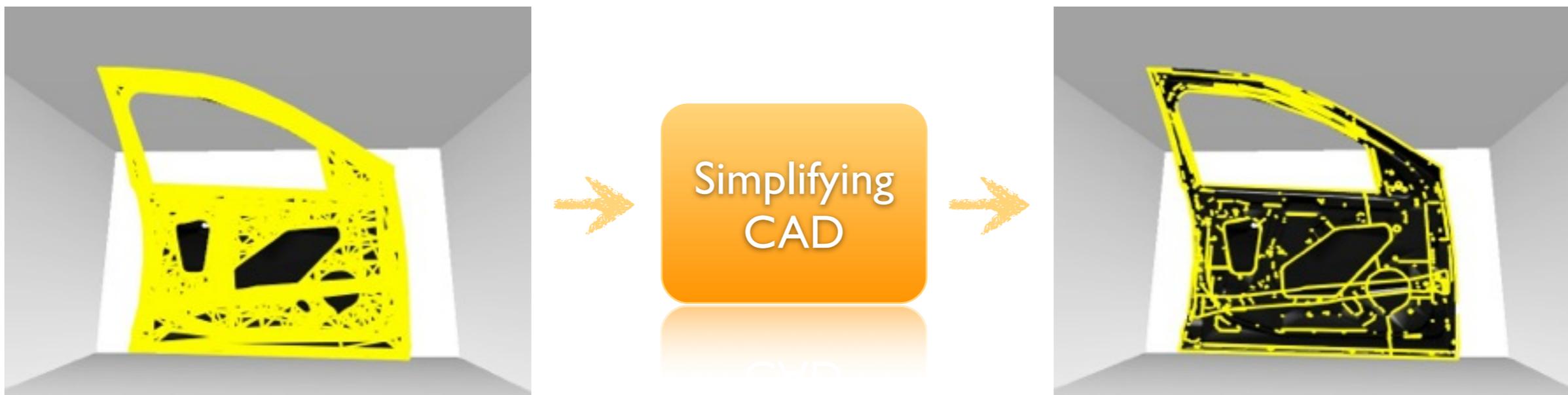
- **Keypoint-based** approaches
  - Good for initialization
  - Invariant to scale and rotation
  - Only applicable to textured objects
  - Computationally expensive



# Overview

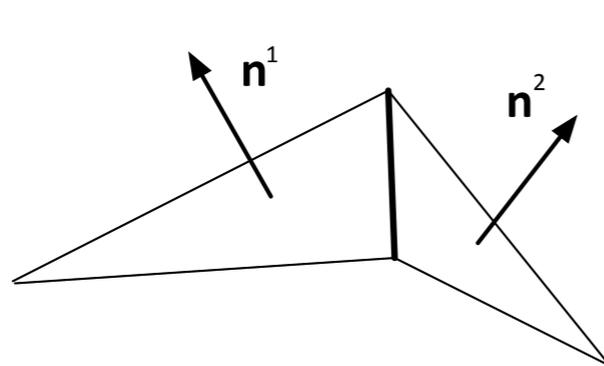


# Simplifying CAD Model

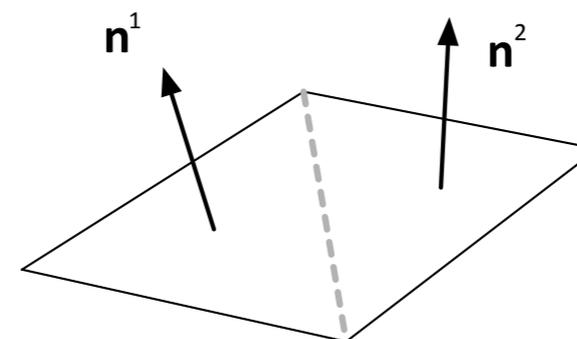


- Original CAD models are too **complex**.
- Most edges in CAD do not appear in the real edge image.
- We should **simplify** in some way.

# Salient Edges



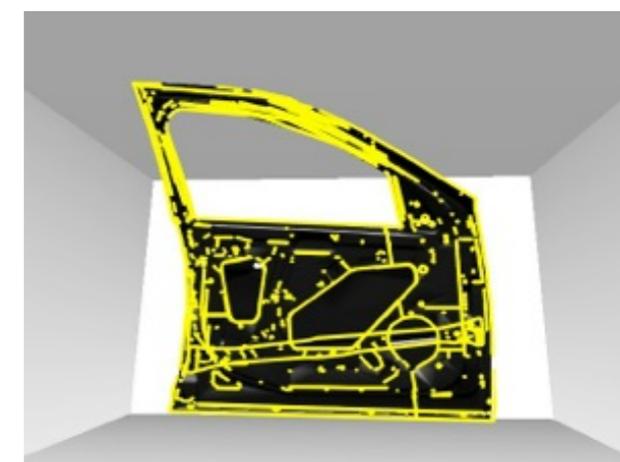
Sharp Edge

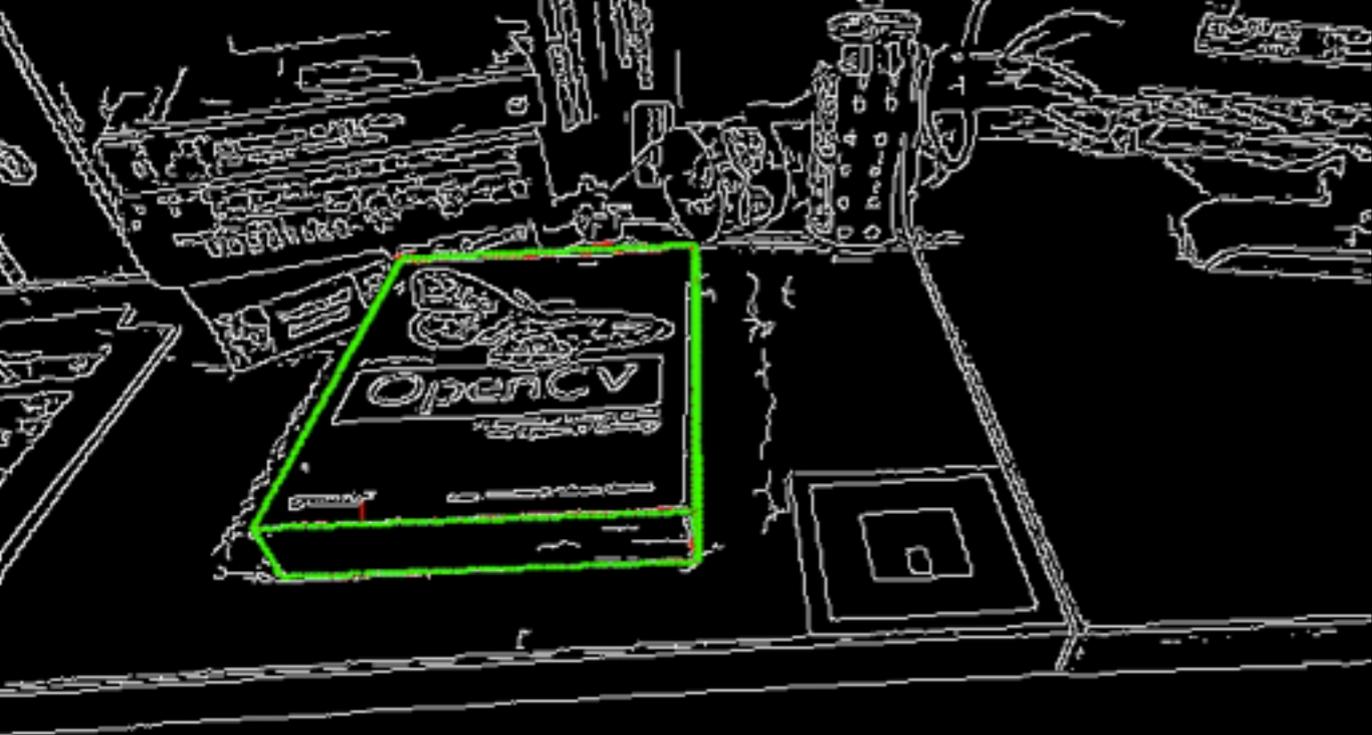


Dull Edge

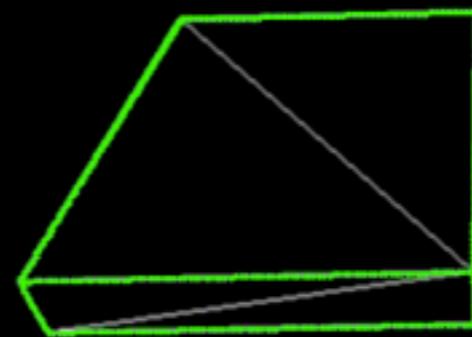
$$I(edge_i) = \begin{cases} 1 & \text{if } |\mathbf{n}_i^1 \cdot \mathbf{n}_i^2| \leq \tau_s \\ 0 & \text{otherwise} \end{cases}$$

- Use **face normal vectors**
- Automatically determine **salient edges** which are more likely to be **visible** in images

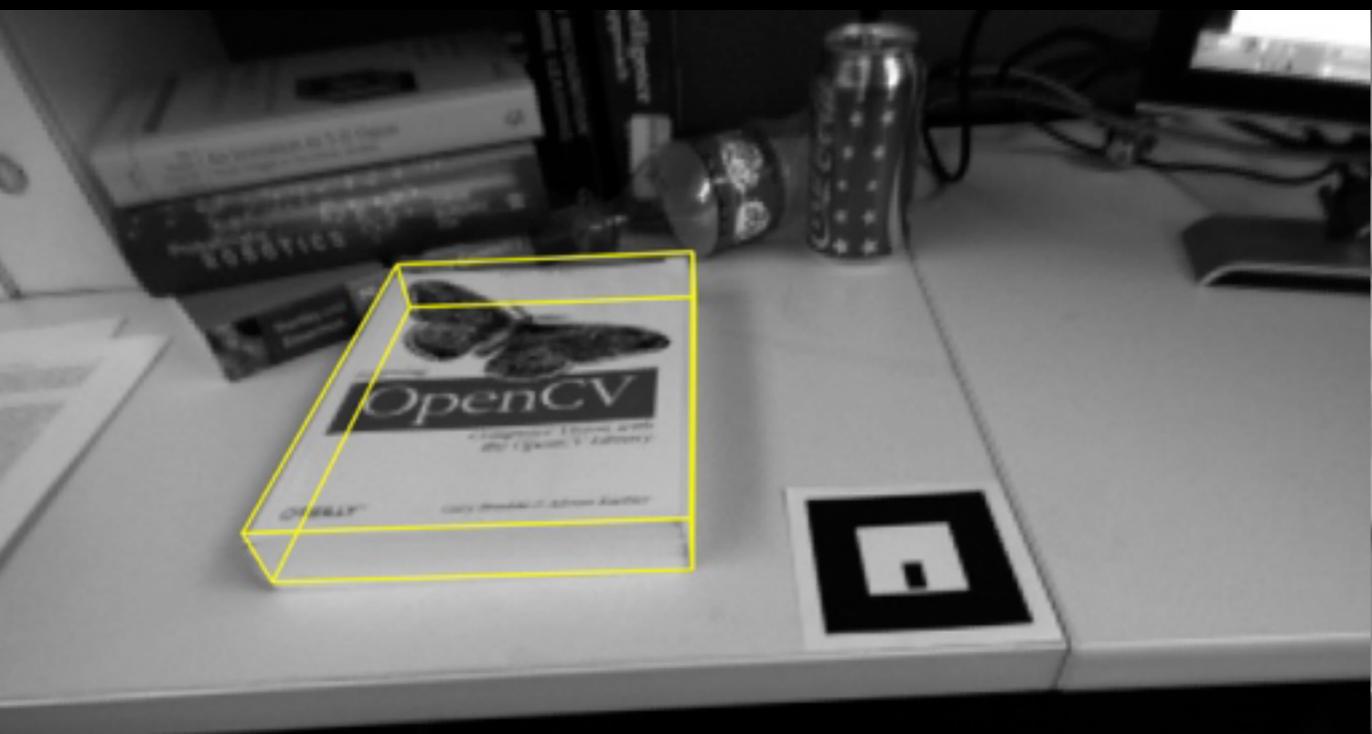




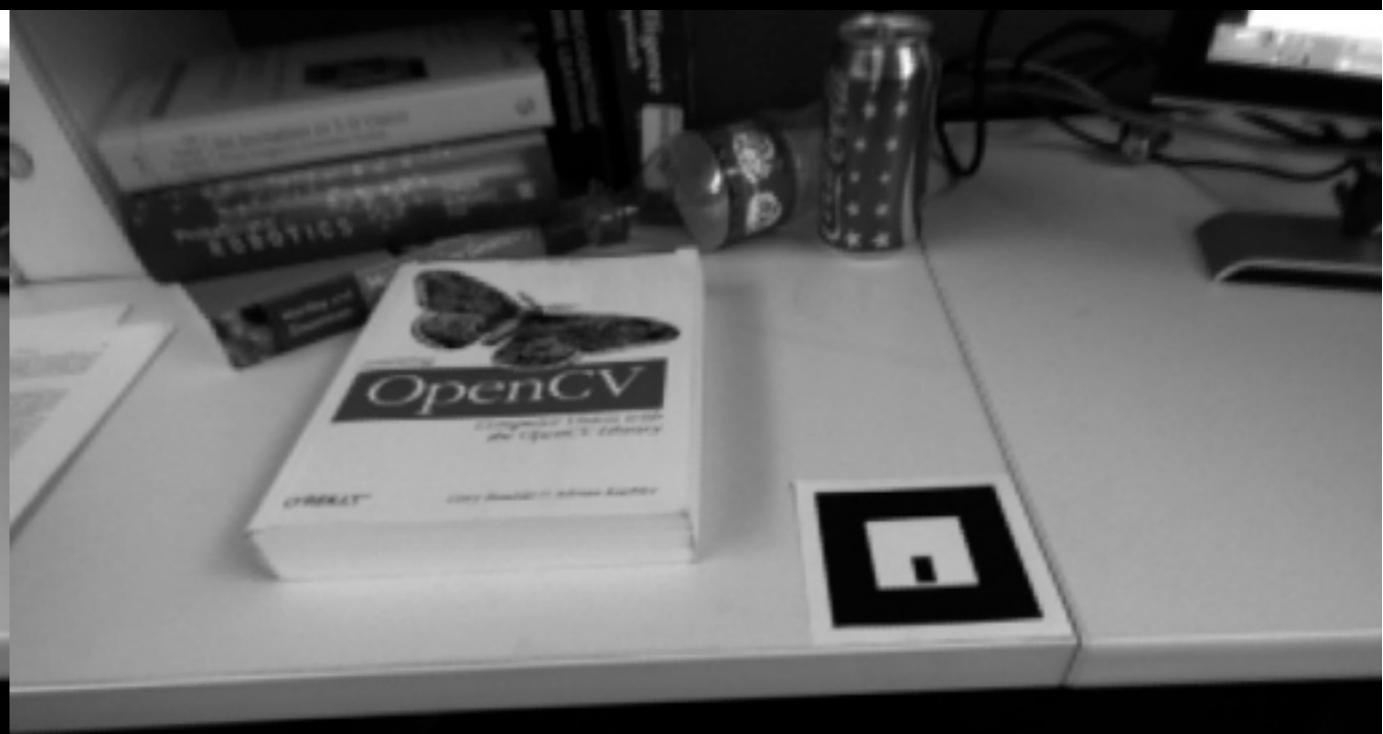
edges



model rendering



our approach



keypoint only

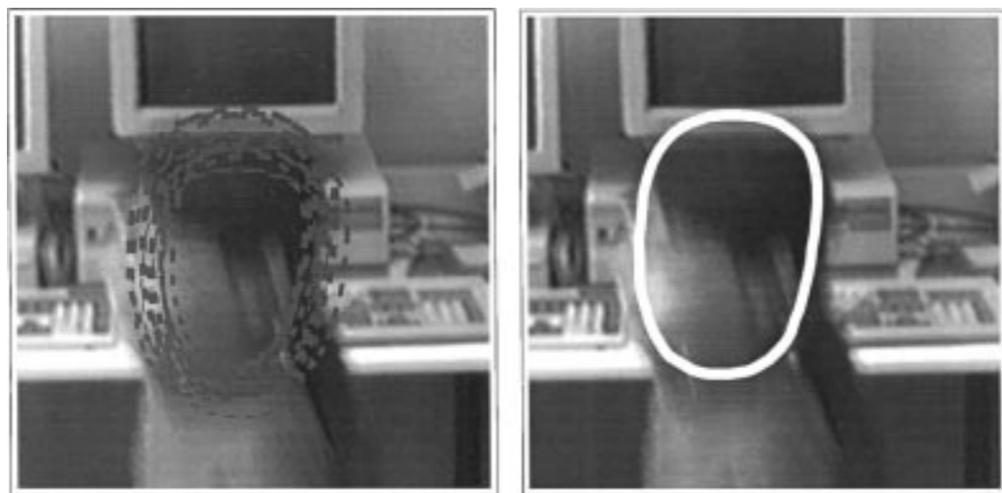
# Limitation



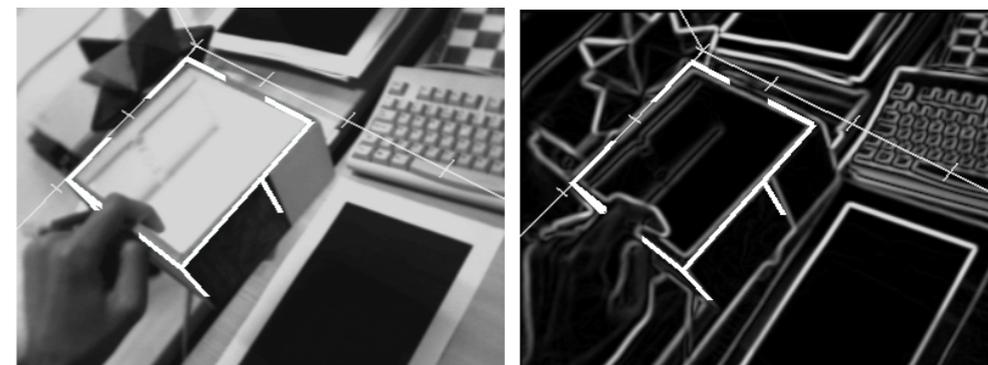
- **Single** pose hypothesis
  - **Wrong** prior pose → not converging to global optimum
- **Ambiguous** edges
- Stuck in **local minima**
  - Highly cluttered environment
  - Occlusions
- **Multiple** pose hypotheses
- **Particle Filtering**

# Related Work

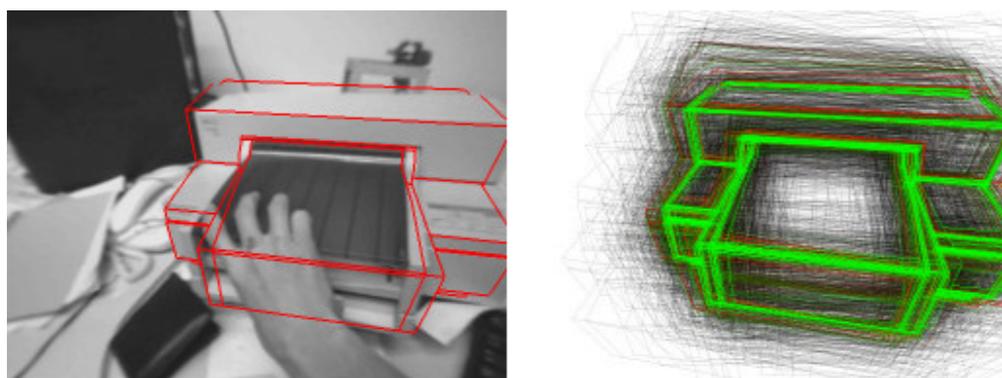
## Particle Filtering using Edges



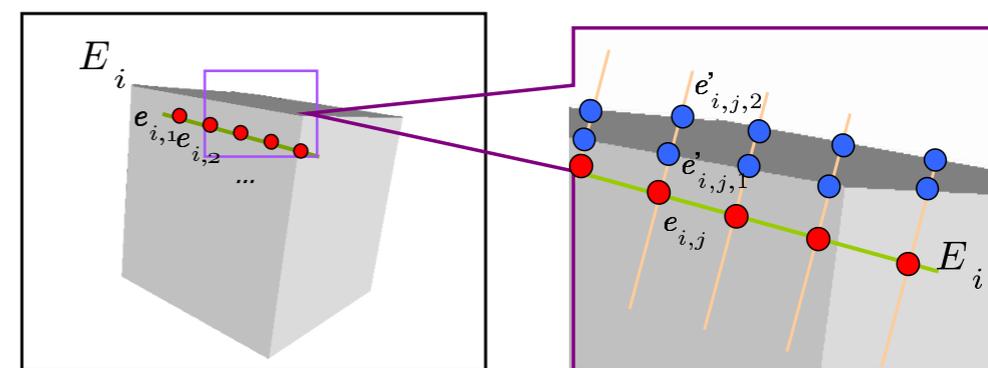
[Isard, IJCV'98] Condensation in 2D



[Pupilli, ICPR'06] PF for 3D edge-based tracking



[Klein, BMVC'06] PF for complex object tracking



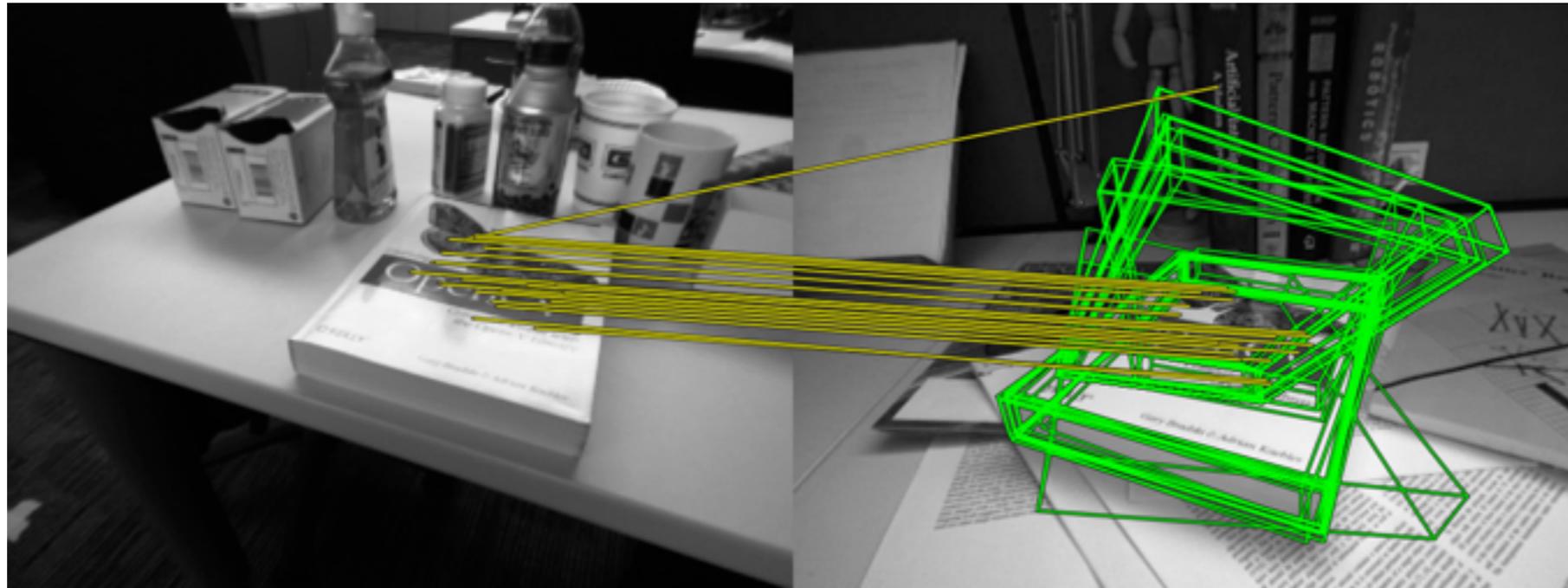
[Teuliere, ICRA'10] Multiple edge correspondences

# Contributions



- Given starting pose
- Gaussian random walk
- No re-initialization
- Initialization
- AR(1) state dynamics
- Auto re-initialization

# Initialization



Keyframe (image, 2D & 3D keypoints)

Input image

Initialize the particle filter using keypoints

- Given 2D-3D keypoints correspondences
- Randomly choose a set of minimum correspondences
- Solve PnP problem to estimate candidate poses
- Weights proportional to inlier ratio of remaining correspondences
- Importance sampling

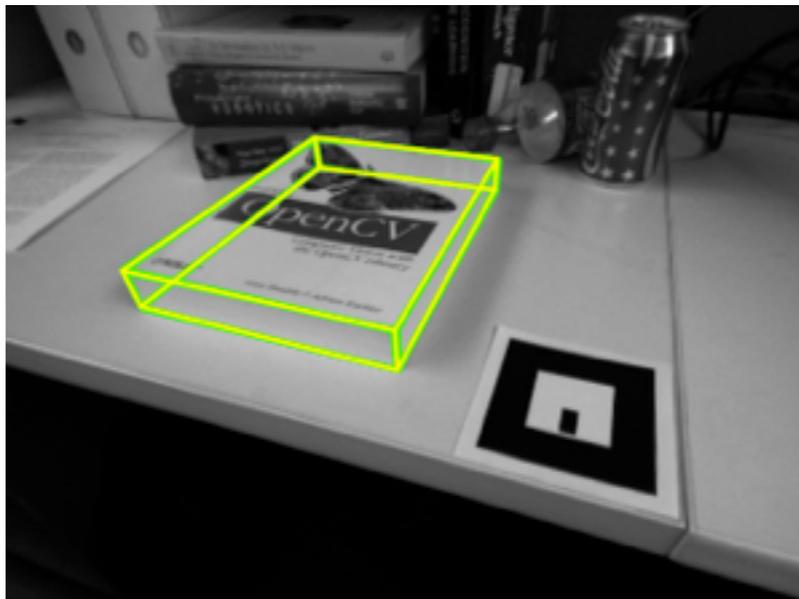
# AR Dynamics

$$X_t = X_{t-1} \cdot \exp(A_{t-1} + dW_t \sqrt{\Delta t}),$$

$$A_{t-1} = a \log(X_{t-2}^{-1} X_{t-1})$$

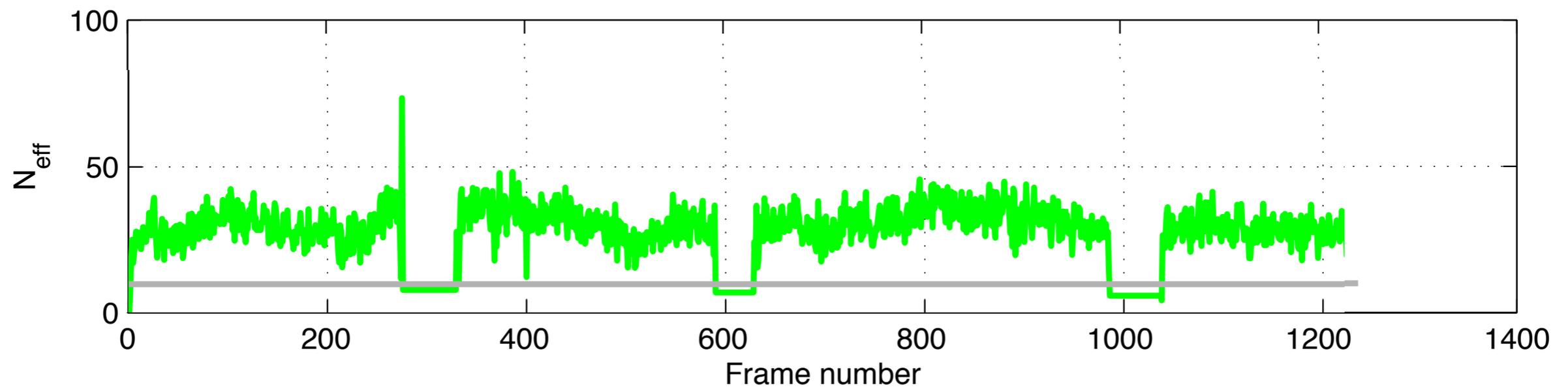
- Instead of Gaussian random walk models
- Linear **prediction** based on previous states
- **Propagate** particles more **effectively**

# Re-initialization



$$\widehat{N}_{eff} = \frac{1}{\sum_{i=1}^N (\tilde{\pi}^{(i)})^2}$$

Effective number of particle size



# Experiments

The **synthetic** image sequence of the  
"Book" object: complex background case

The **synthetic** image sequence of the "Car  
door" object: complex background case

The "Book" object

The **real** image sequence of the "Teabox"  
object

The **real** image sequence of the "Car door"  
object

The "Car door" object

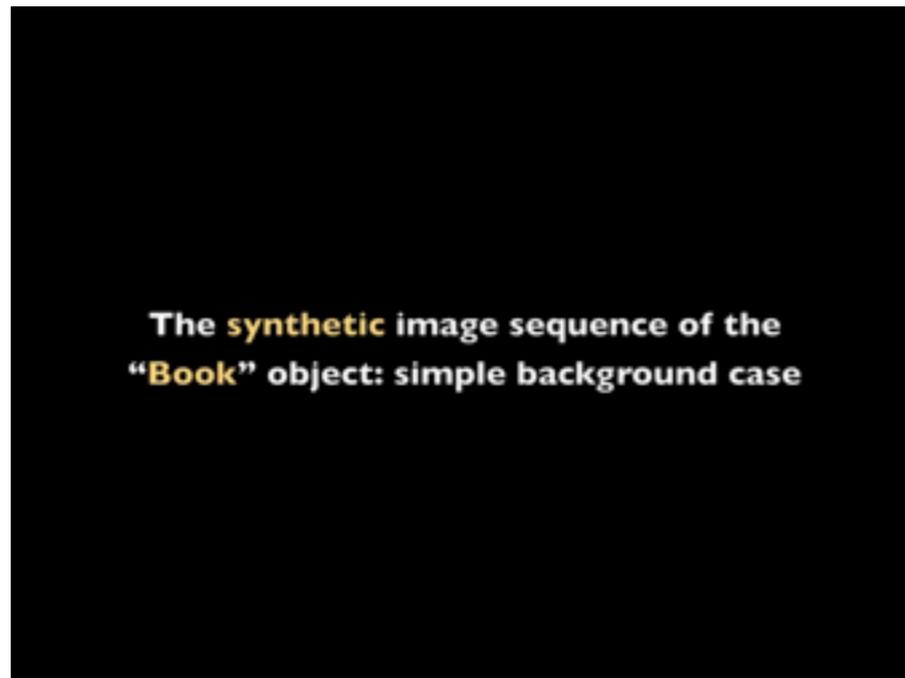
Single vs. Multiple pose hypotheses

with vs. without AR state dynamics

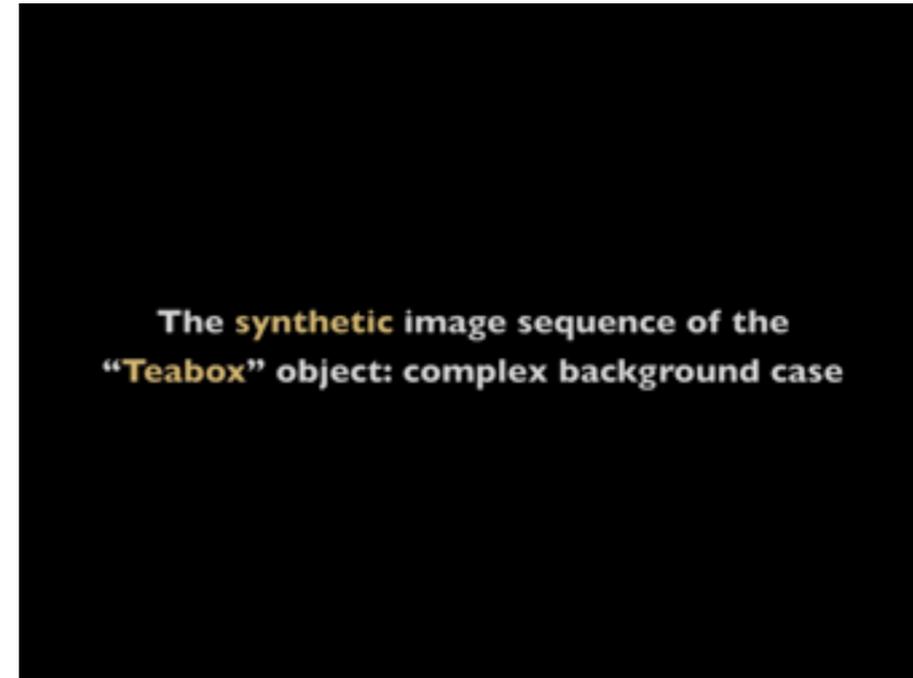
Reinitialization exp.

# Ours vs. BLORT

SYNTHETIC

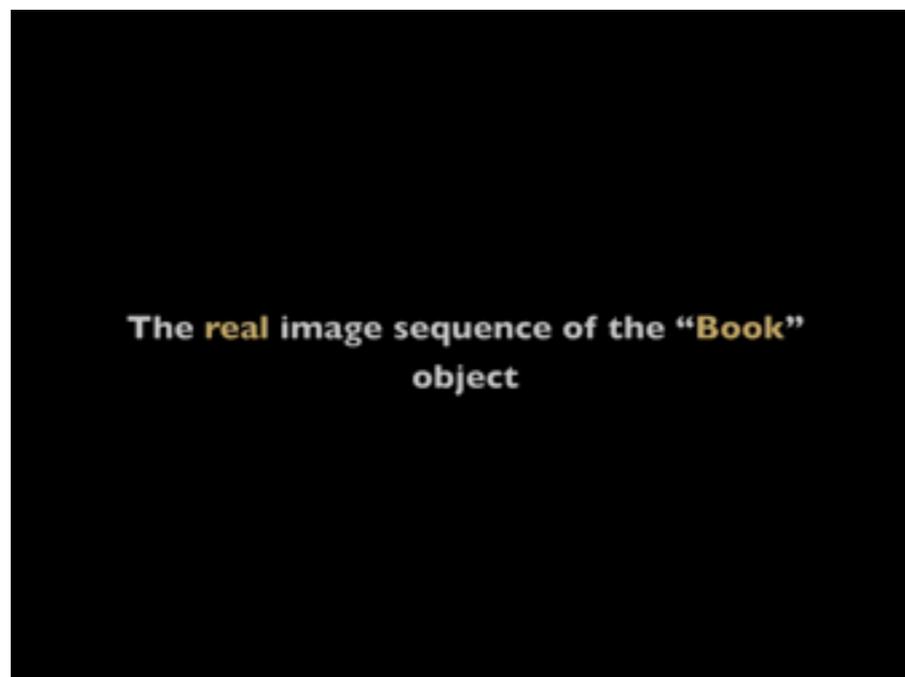


Book



Teabox

REAL

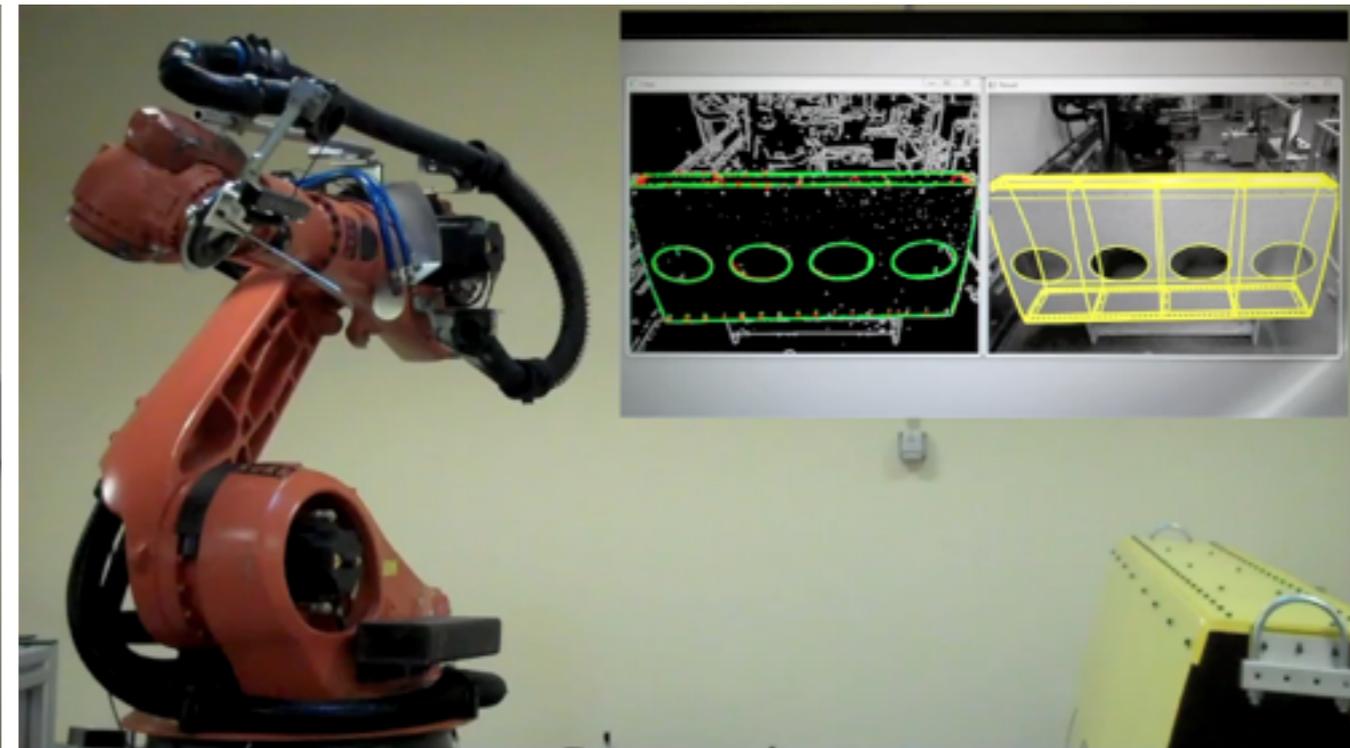
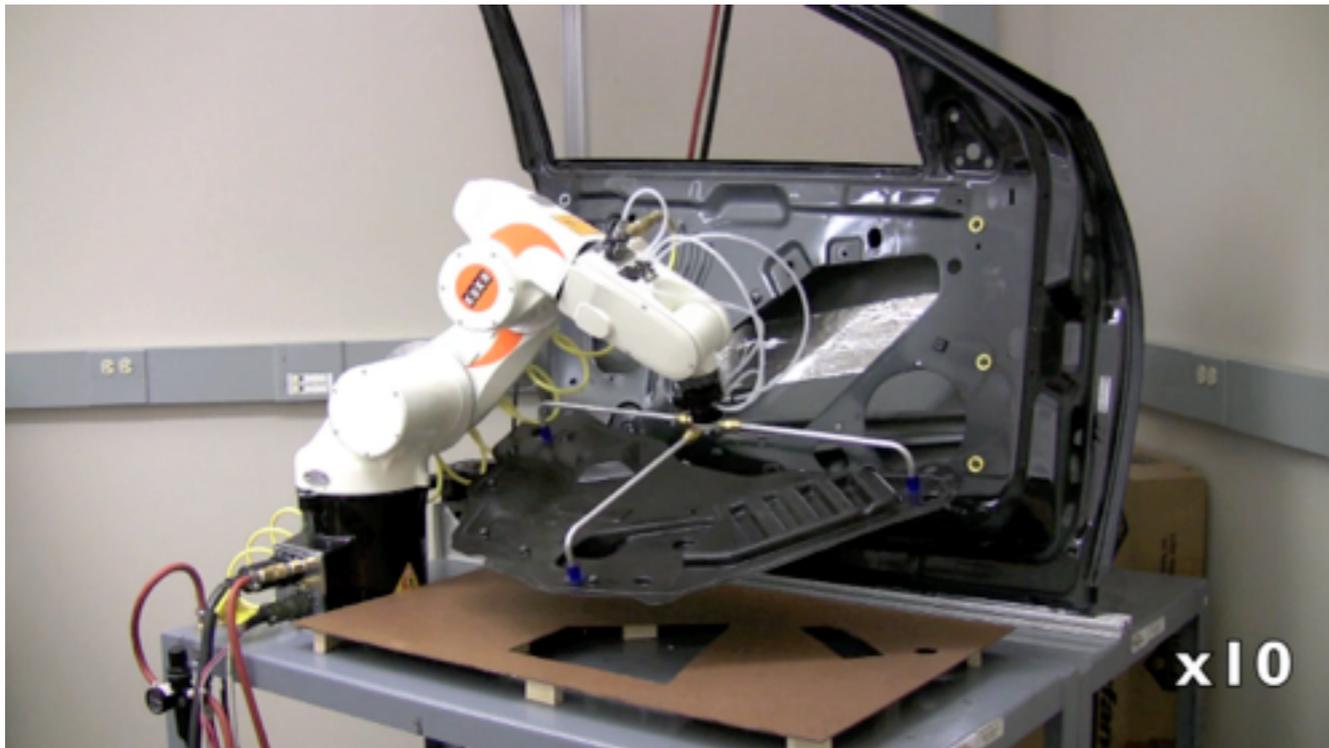


Book



Cup

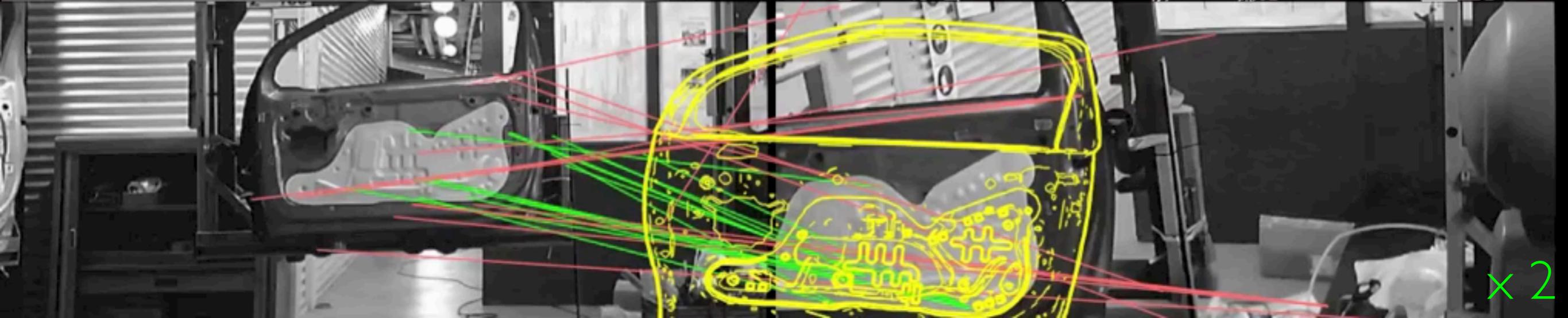
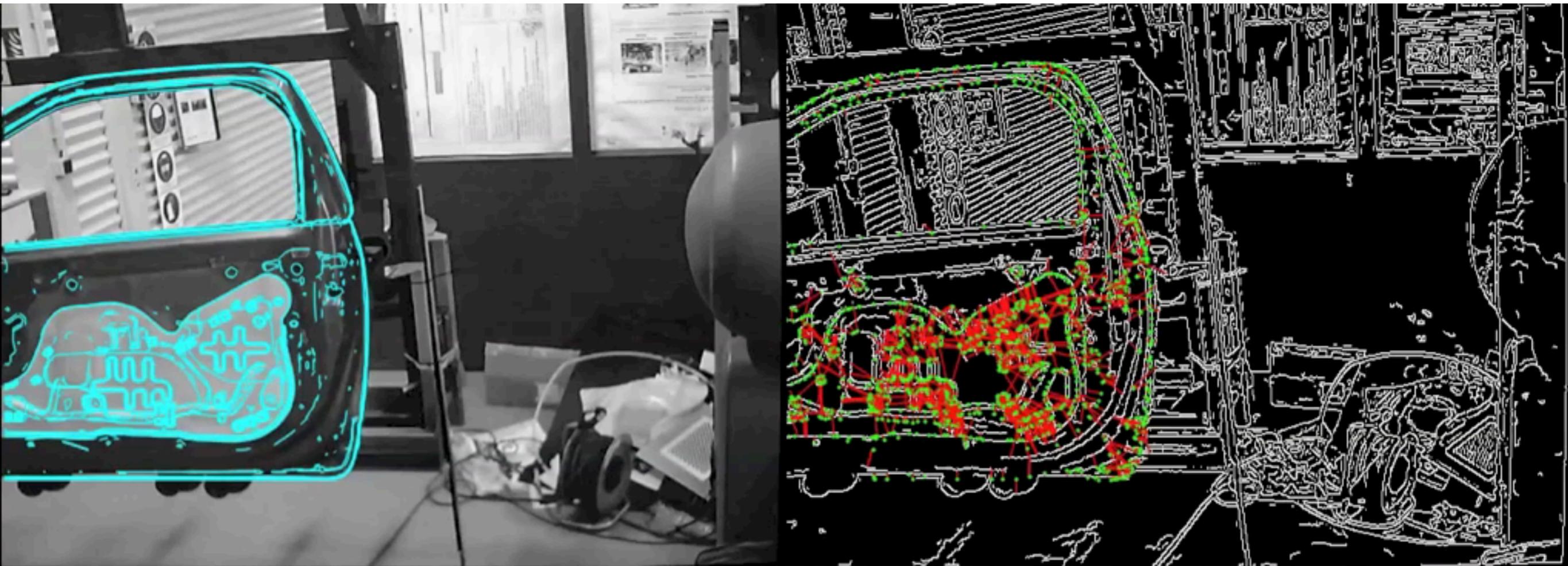
# Robotic Assembly



# Robotic Assembly



PEUGEOT



# Approaches



- 2D Visual Information (Monocular Camera)
  - Combining Keypoint and Edge Features [ICRA'10, ICRA'11, IJRR'12]
  - **Extending to Textureless Objects** [IROS'12]

geometric



- 3D Visual Information (RGB-D Camera)
  - Voting-based Pose Estimation using Pair Features [ICRA'12, IROS'12]
  - Object Pose Tracking [IROS'13]

# Textureless Objects



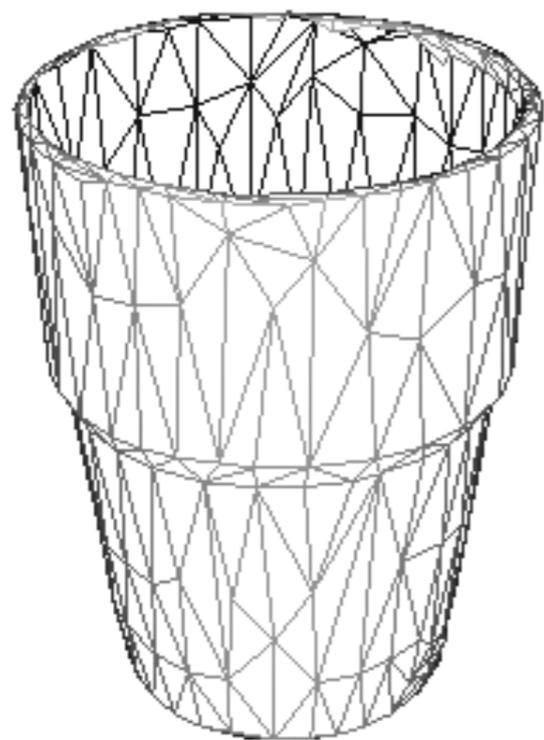
Textureless object



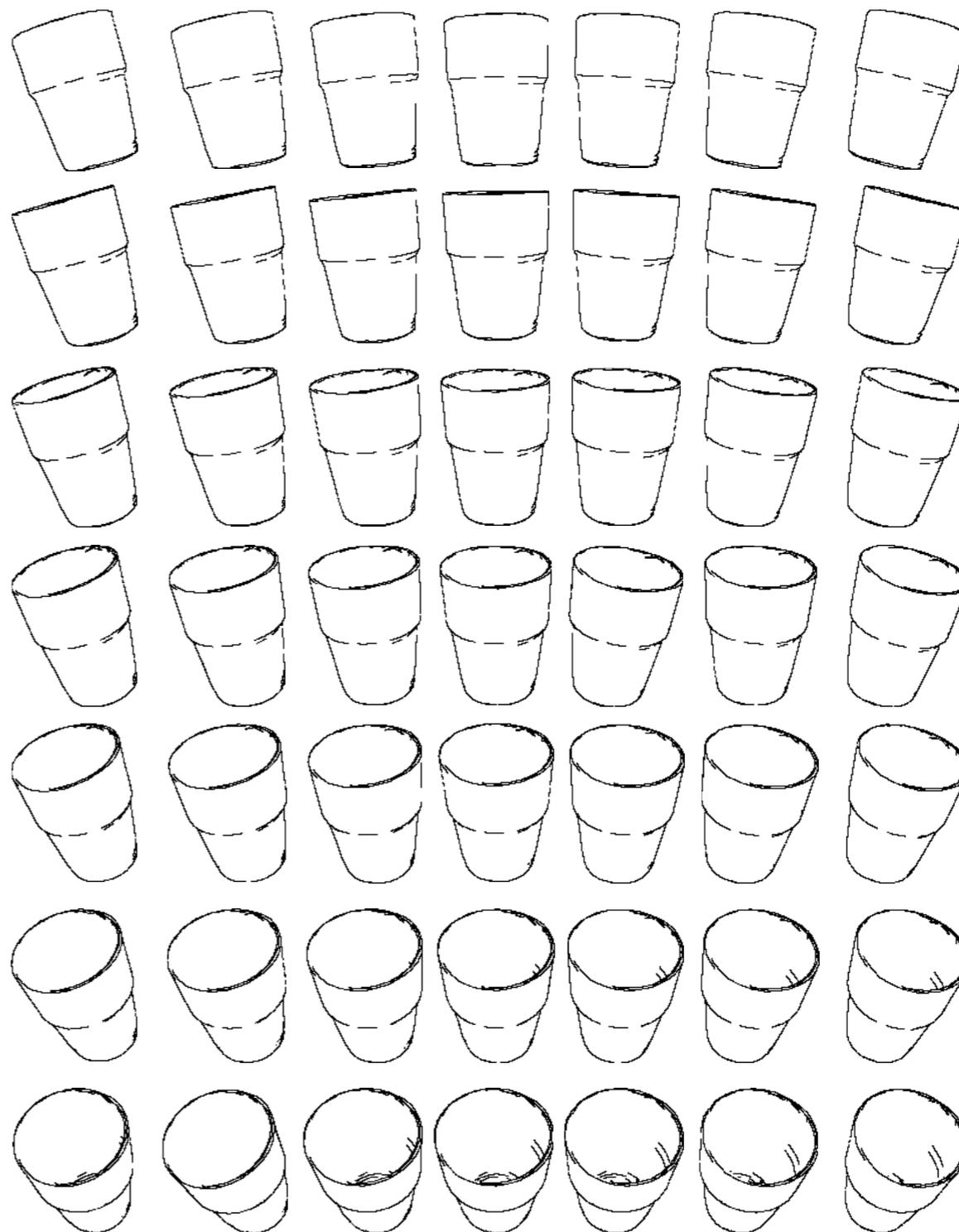
Edge template

- **Edges** (or boundaries) are preferred for textureless objects.
- From CAD model to Edge templates
- Efficient **chamfer matching** [Liu, CVPR'10]
- **Coarse 3D pose estimation** from 2D chamfer matching results
- Annealing Process after Initialization

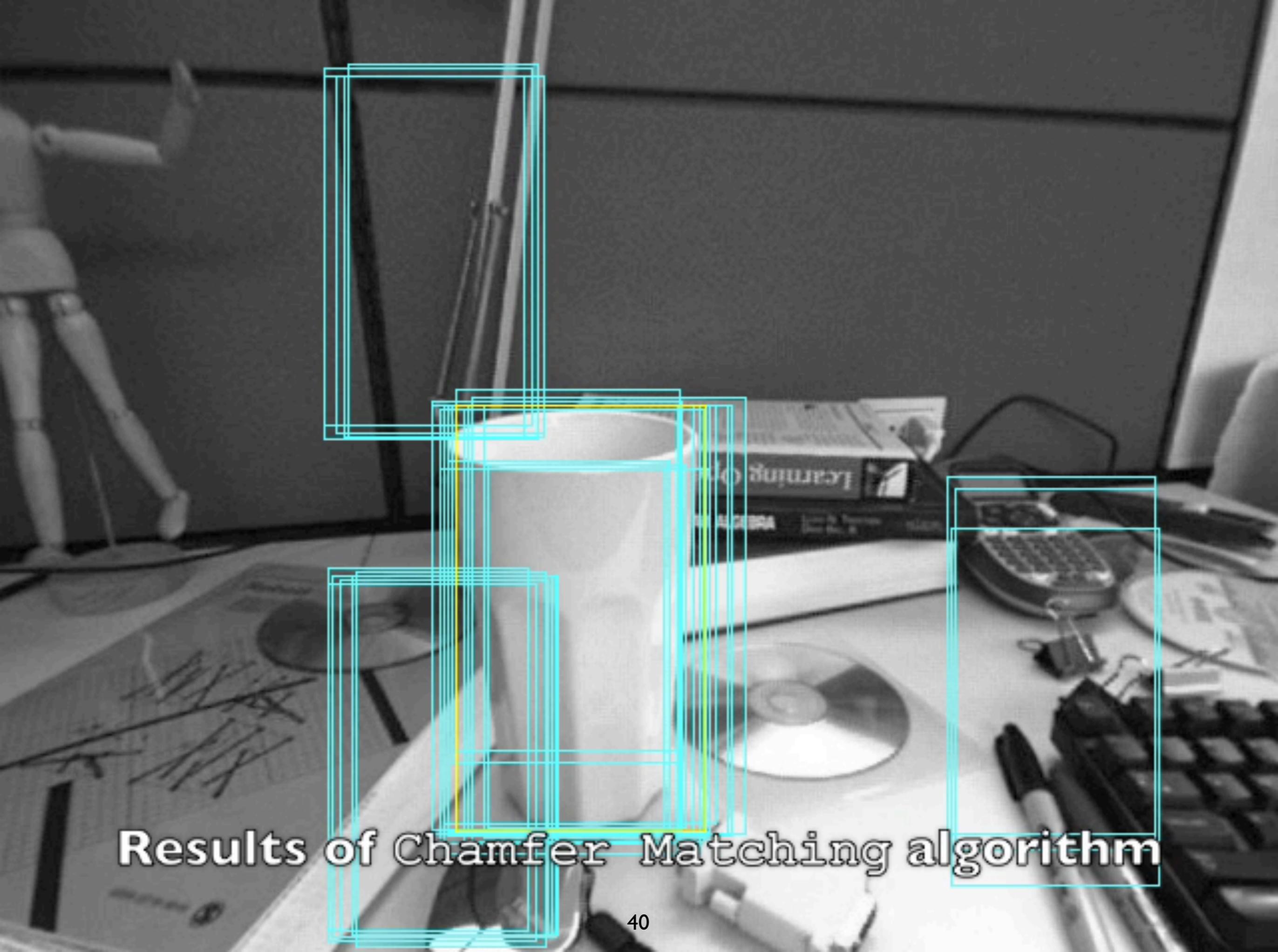
# Edge Templates



CAD model

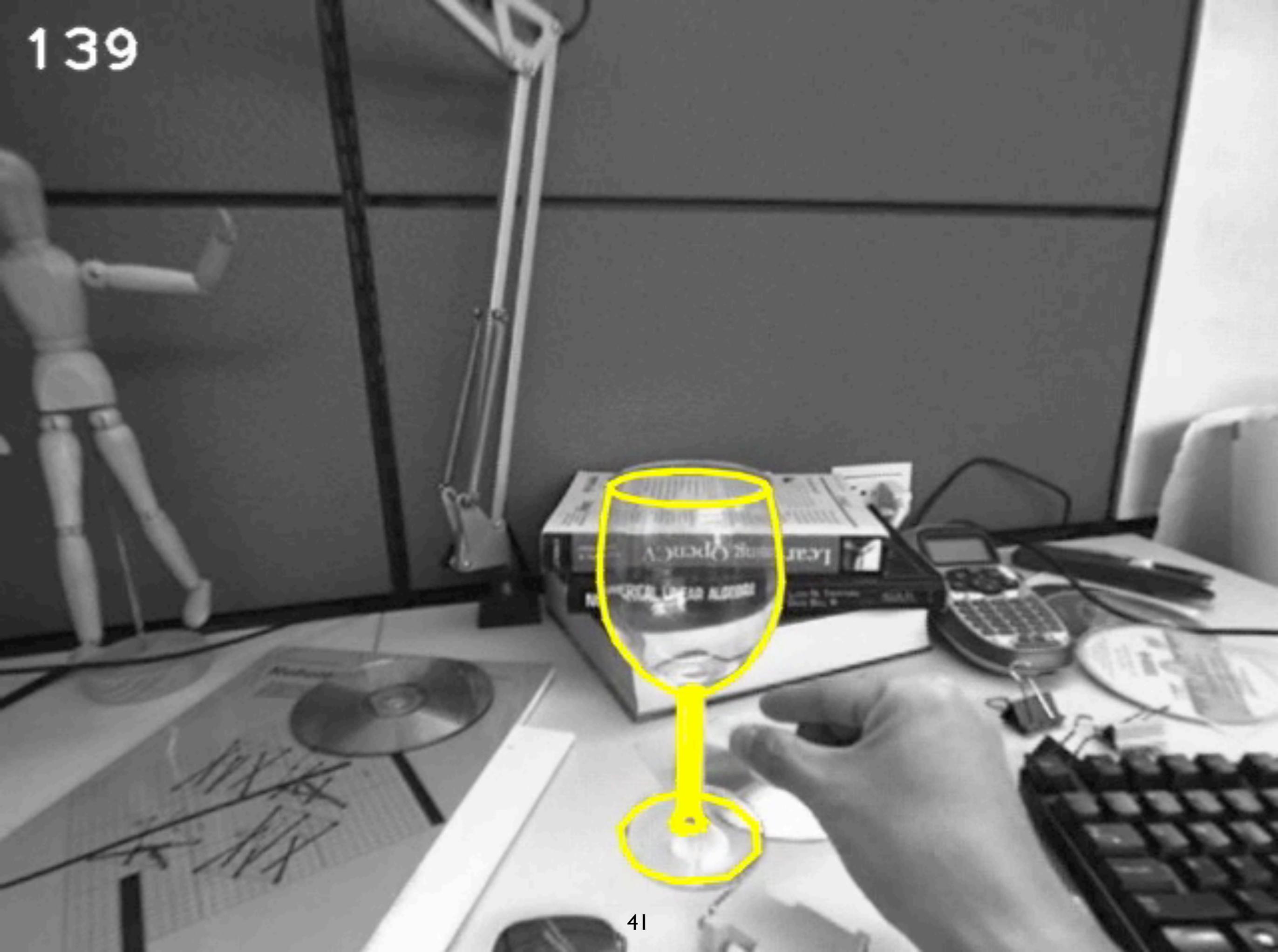


Edge Templates



**Results of Chamfer Matching algorithm**

139



# Approaches



- 2D Visual Information (Monocular Camera)
  - Combining Keypoint and Edge Features [ICRA'10, ICRA'11, IJRR'12]
  - Extending to Textureless Objects [IROS'12]

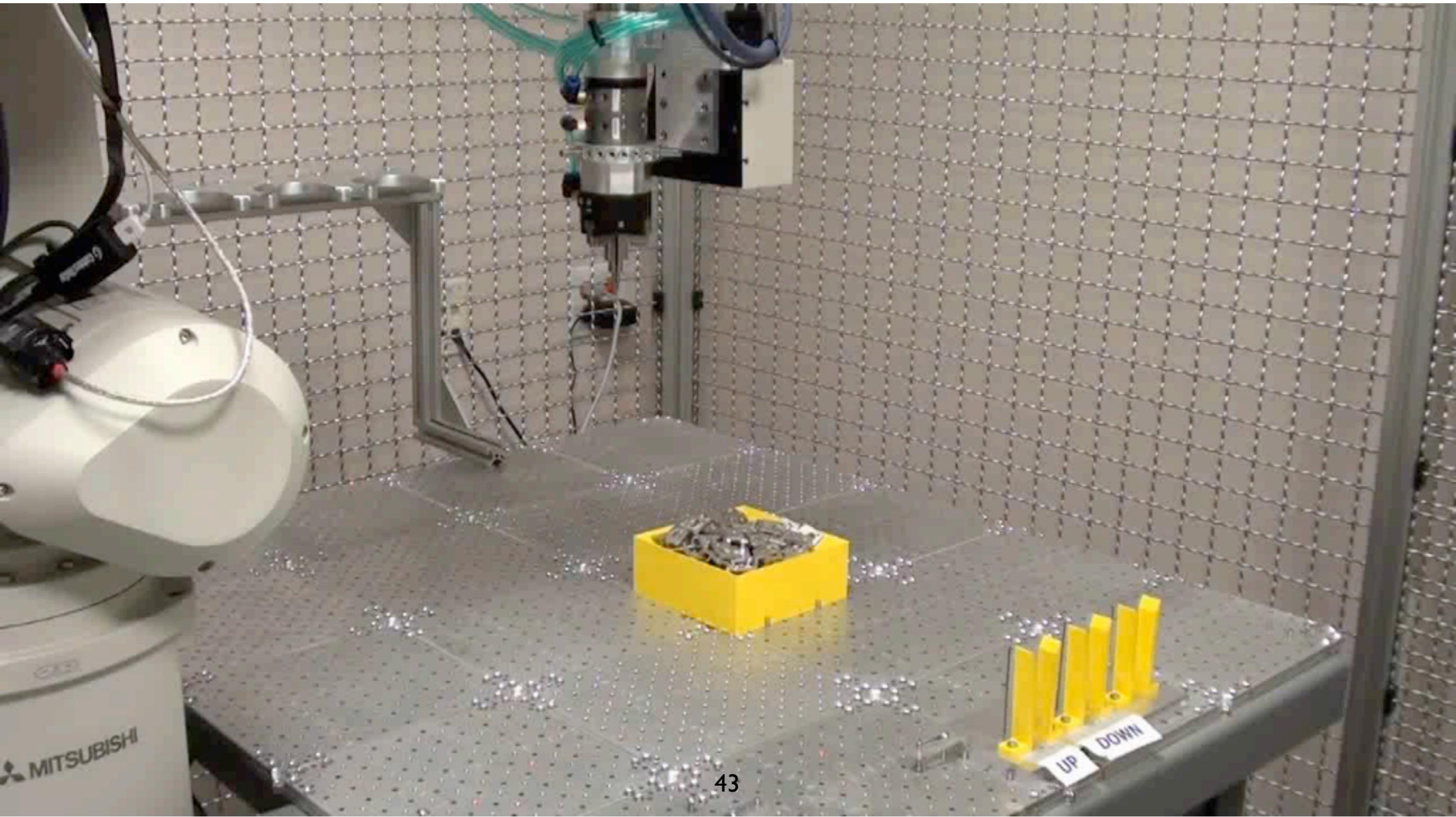


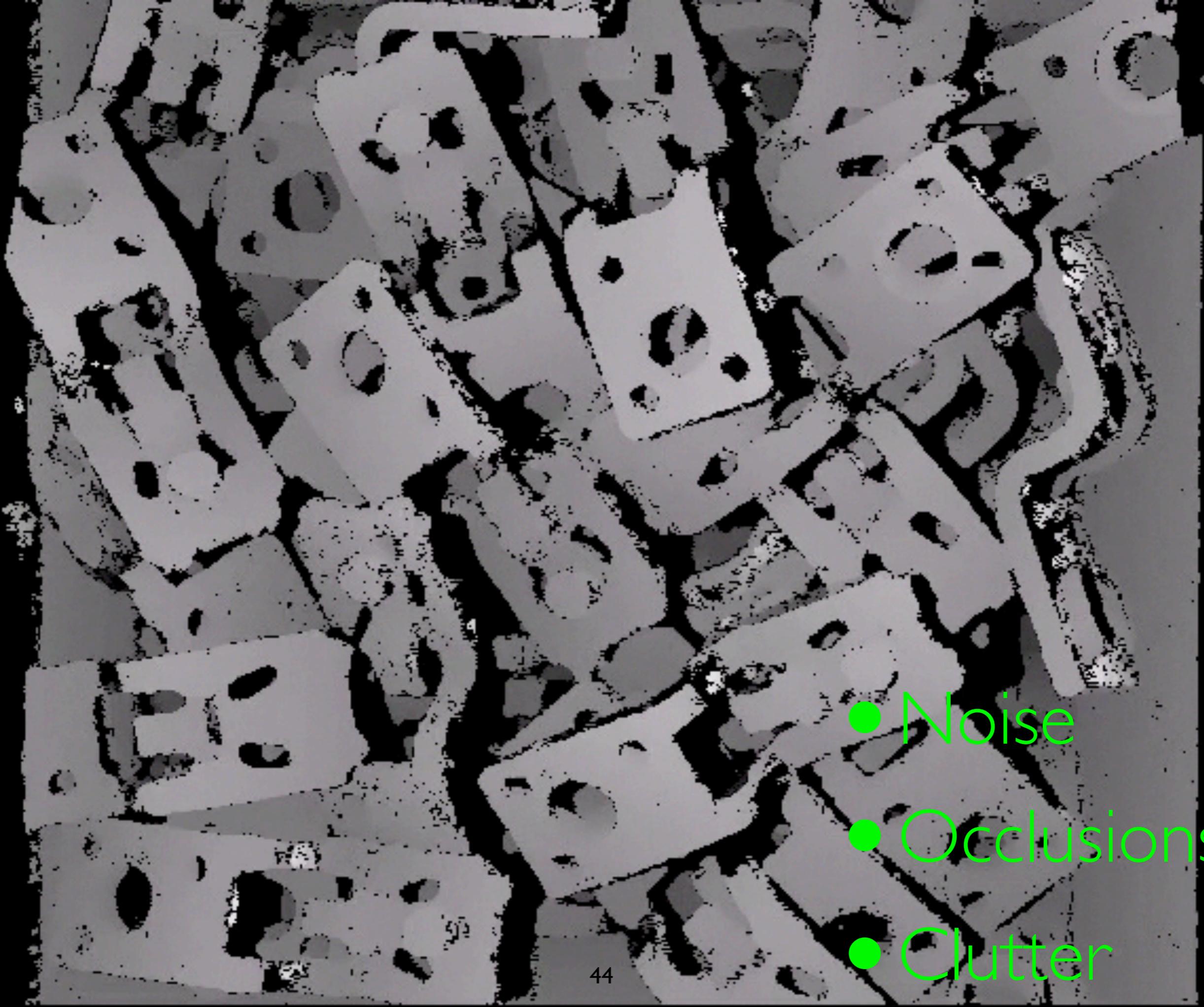
- 3D Visual Information (RGB-D Camera)
  - **Voting-based Pose Estimation using Pair Features** [ICRA'12, IROS'12]
  - Object Pose Tracking [IROS'13]

**geometric**

**geometric +  
photometric**

# Overview





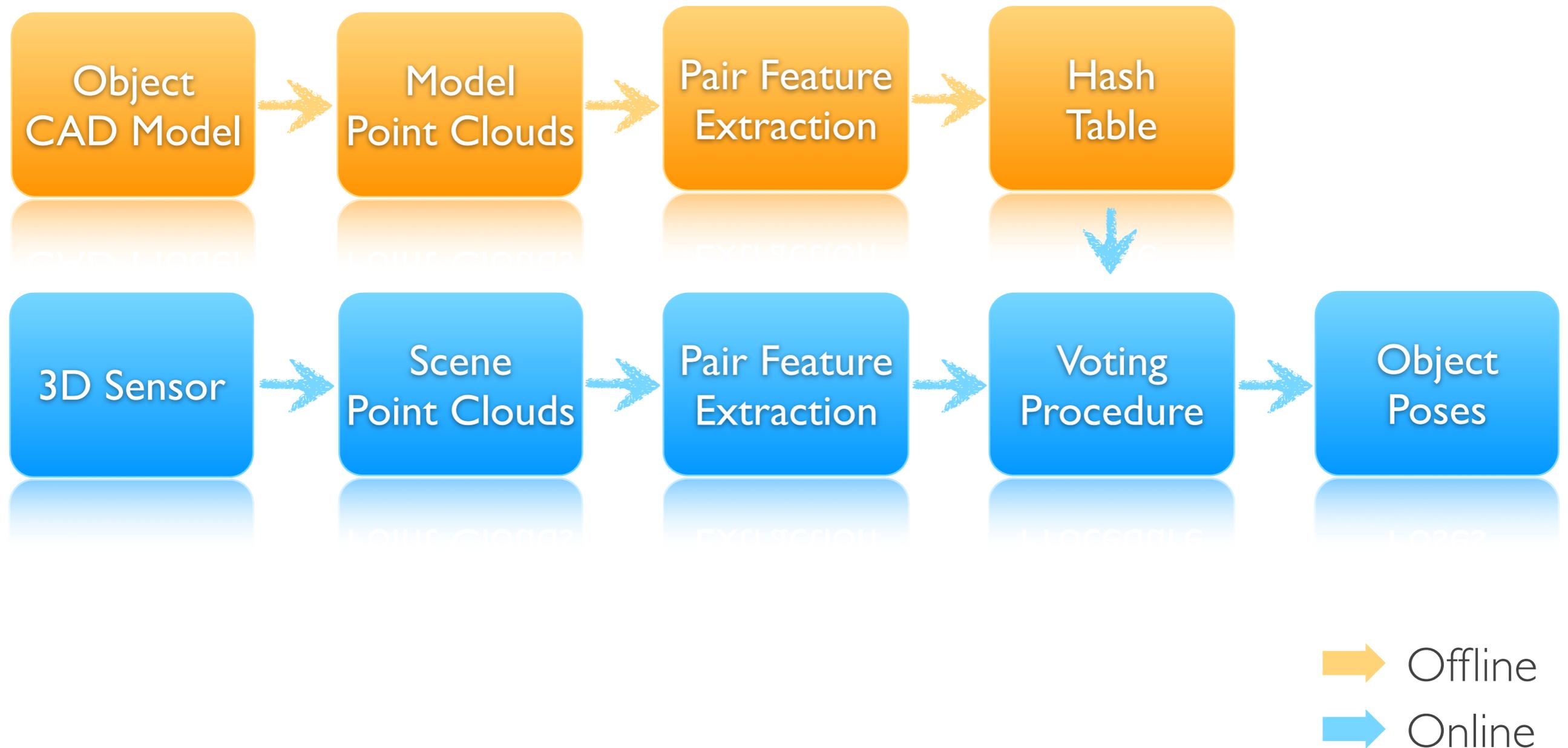
- Noise
- Occlusions
- Clutter

# Contributions

- Exploiting objects' **boundary** information
  - B2B, S2B, and L2L features
- Better for **planar** objects
- **Sparser** primitives
- More **efficient**



# Flowchart



# Geometric Primitives

Surface Points



Boundary Points



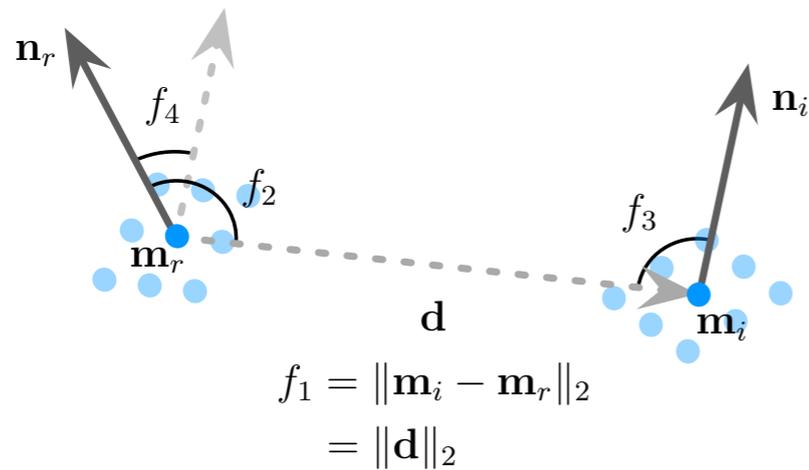
Surface & Boundary



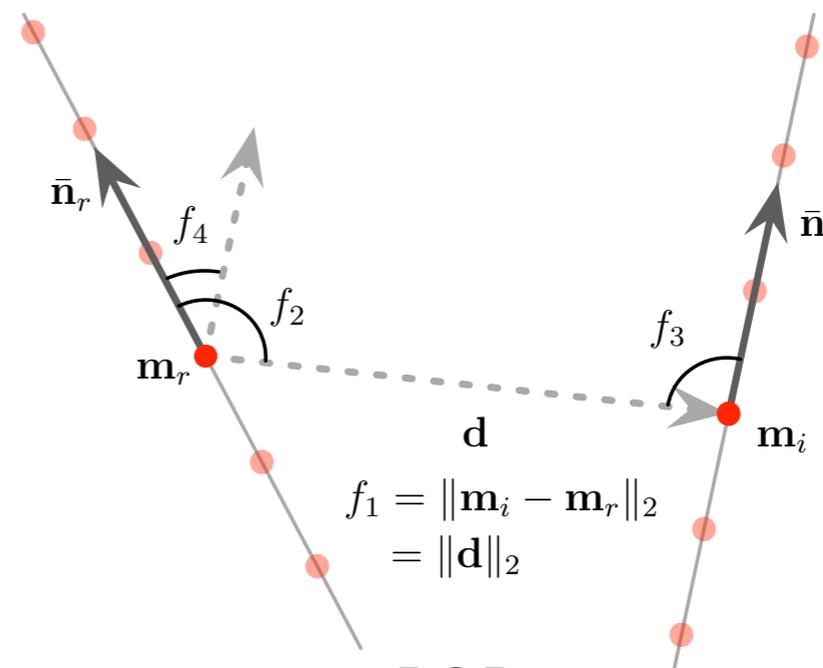
Lines



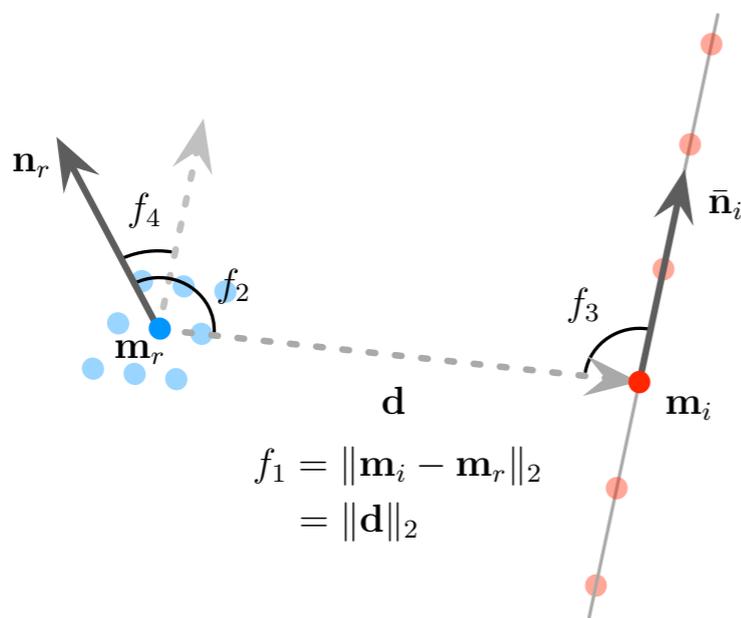
# Pair Features



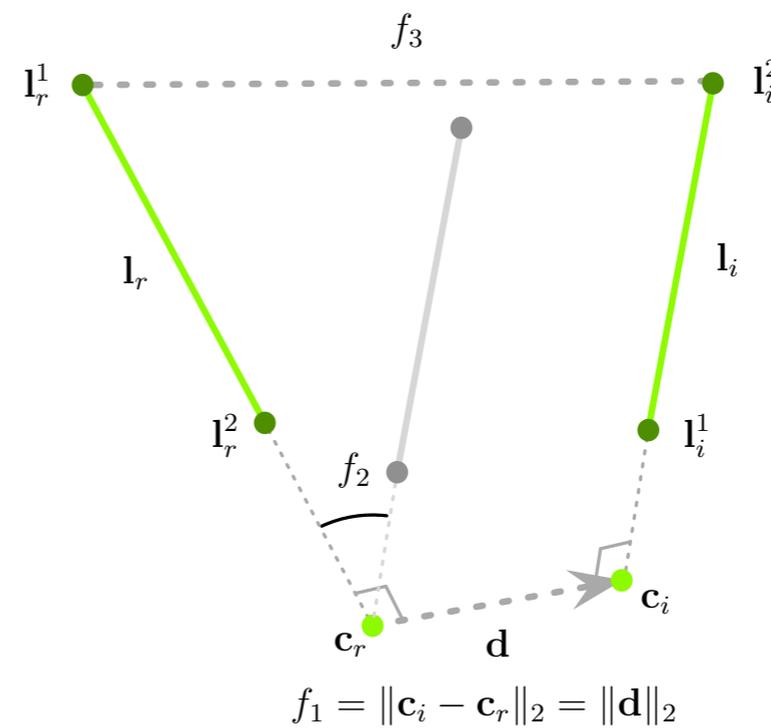
S2S (Drost et al.)



B2B



S2B

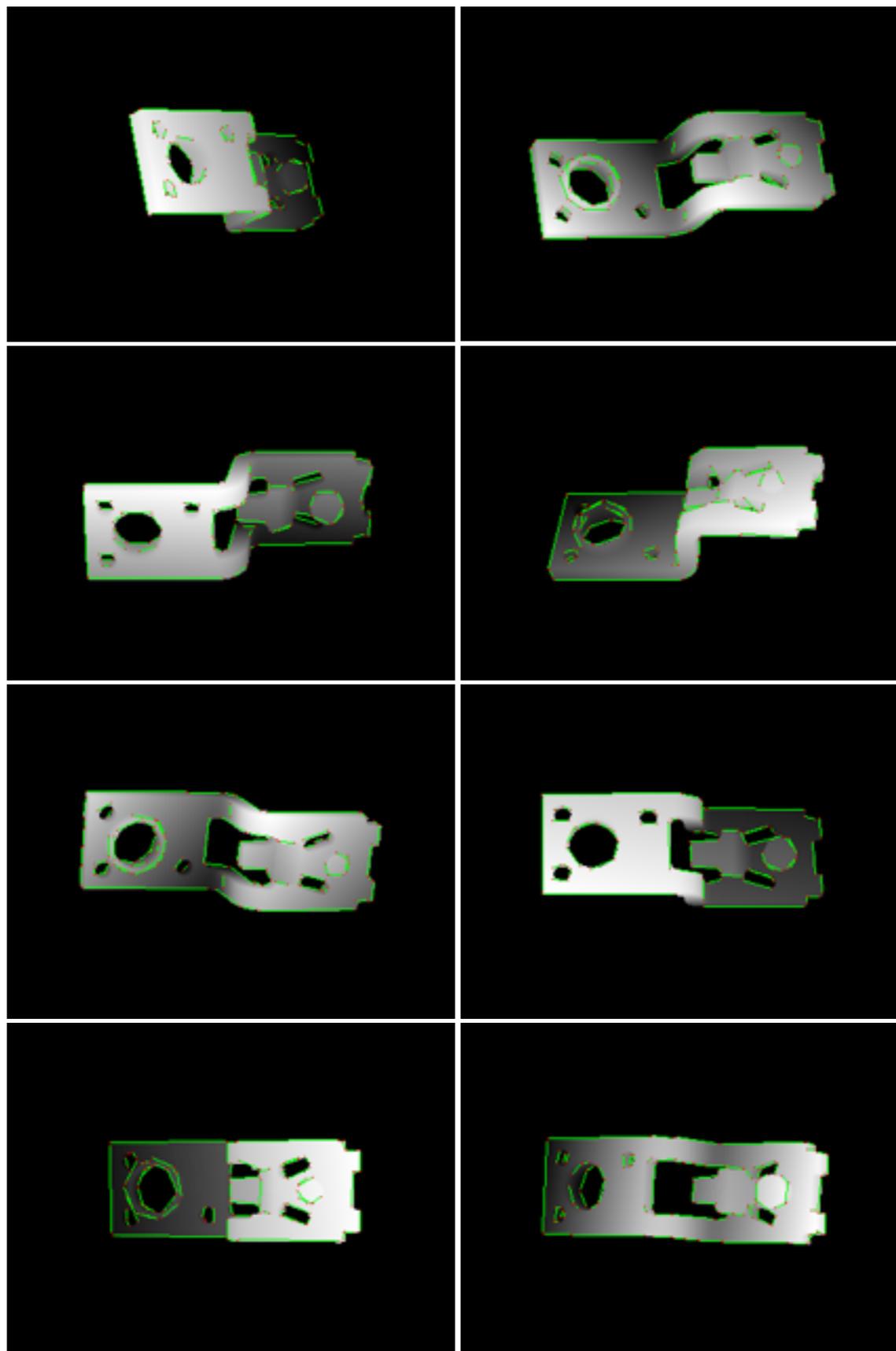


L2L

# Object Learning



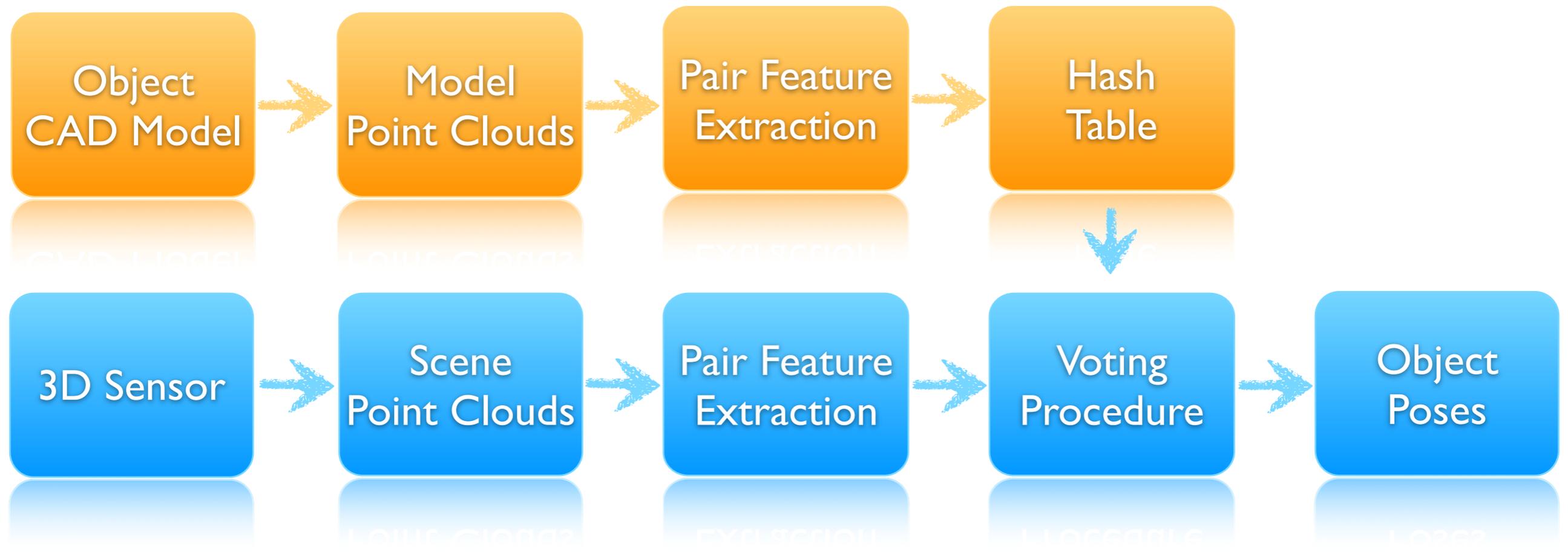
CAD model



Hash  
Table

15016

# Flowchart



➔ Offline  
➔ Online

# Why Voting?

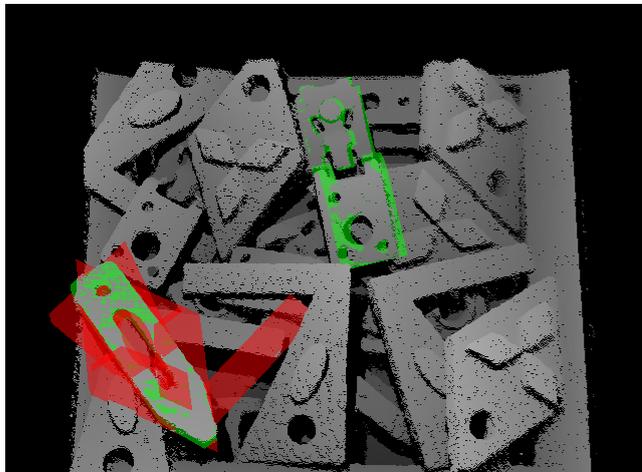


- **Low dimensional** pair features: 3D or 4D
- **One** scene pair feature → **Many** model pair features
  - Self symmetric regions
  - Noise
  - Background clutter
- **Voting procedure** to overcome the *ambiguities*
- **Maximum** votes → the **most likely** pose hypothesis

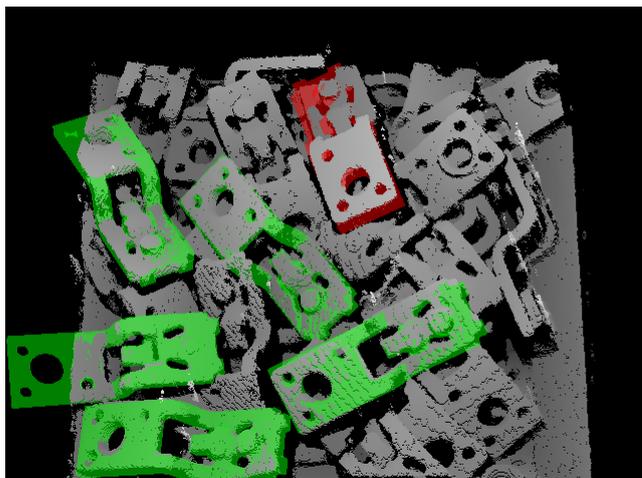
→ True Positives  
→ False Positives

# Real Scan

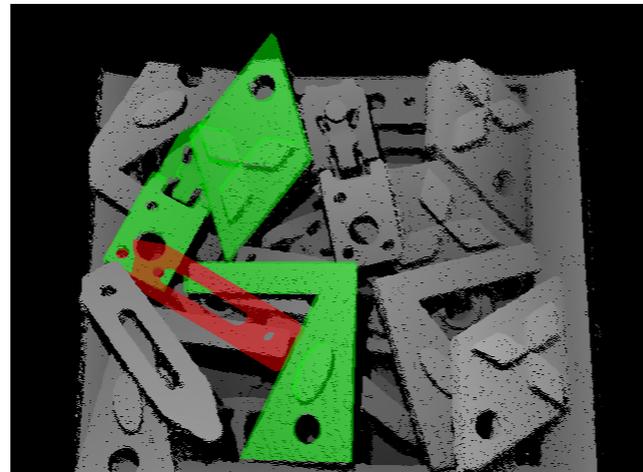
S2S



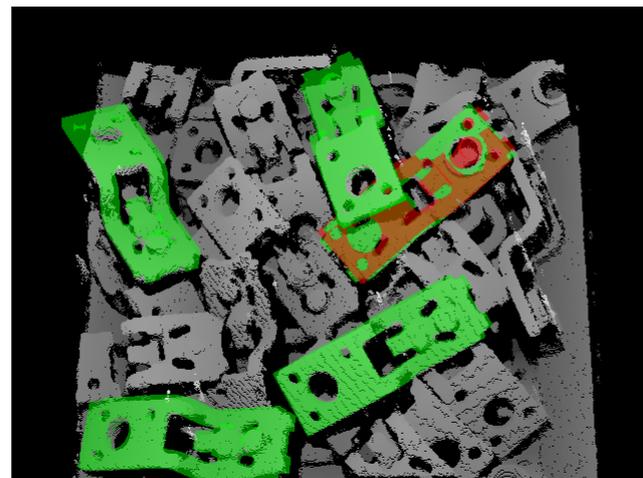
S2S



B2B



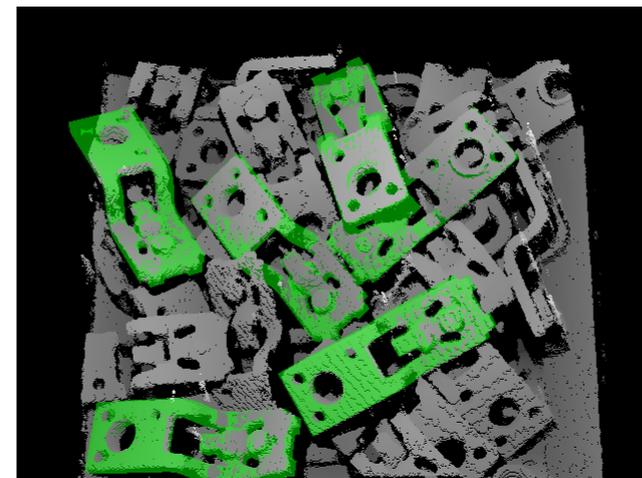
B2B



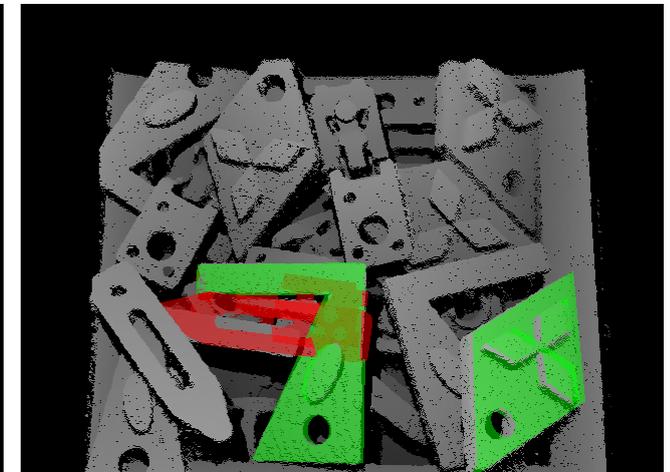
S2B



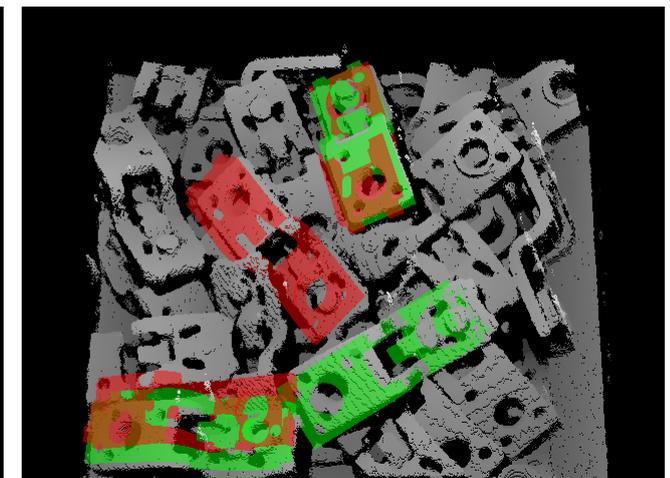
S2B



L2L



L2L



# Processing Time

TABLE I  
AVERAGE NUMBERS OF PAIR FEATURES IN THE SYNTHETIC SCENE  
DATASET AND RELATIVE PROCESS TIME.

Feature	Number of Features	Relative Process Time <sup>†</sup>
<b>S2S</b> [23]	23040000 (= 4800 × 4800)	3.21
<b>B2B</b>	2616953 (≈ 1618 × 1618)	<b>1.00</b>
<b>S2B</b>	7689280 (≈ 4800 × 1602)	1.20
<b>L2L</b>	121058 (≈ 348 × 348)	1.03

<sup>†</sup> The fastest method, *B2B*, is shown as one.

- Our pair features are **sparser** and **faster**.



# Exploiting Color Info.

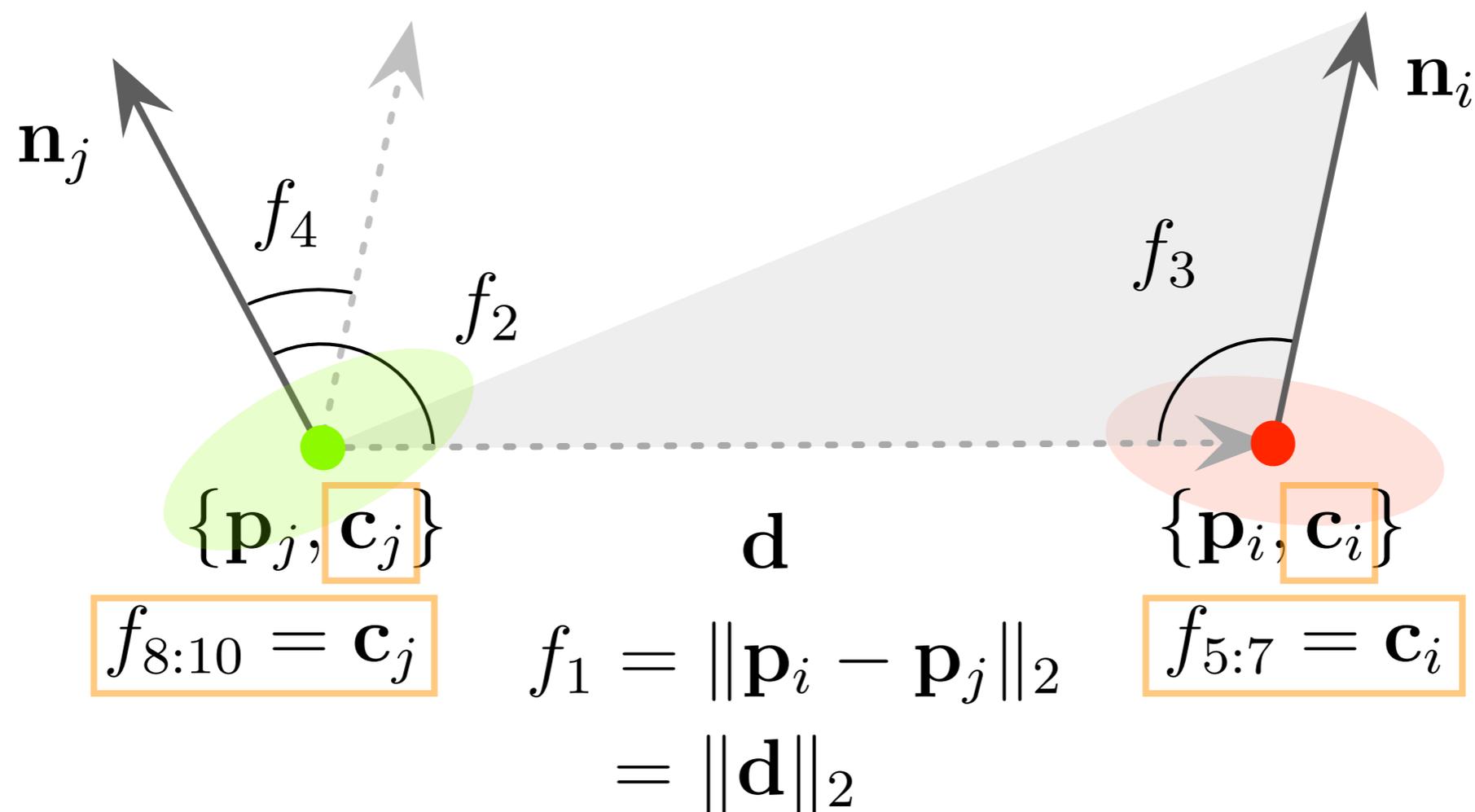


- Industrial parts
  - Low texture or textureless
  - **Boundary** information is useful



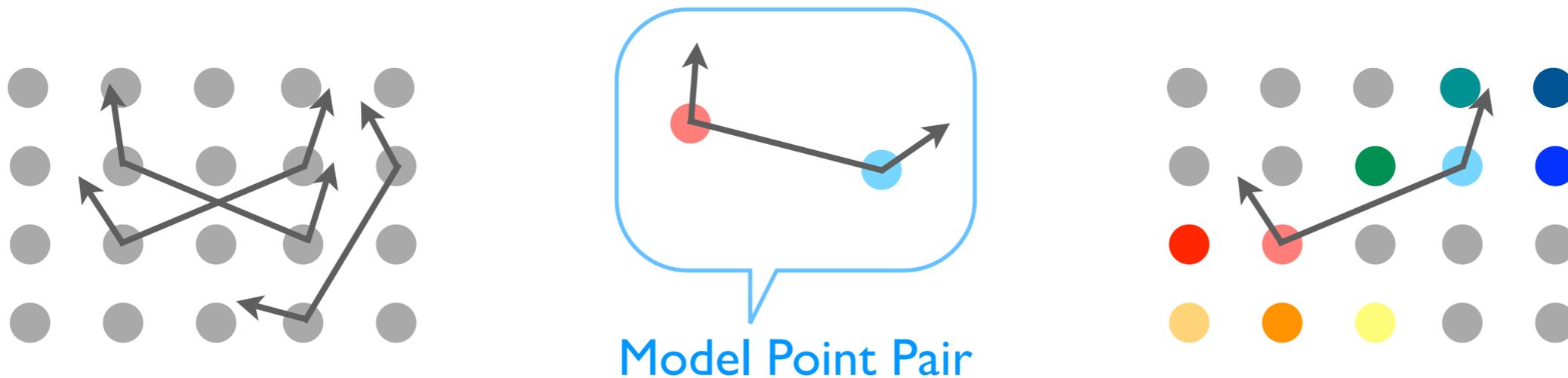
- Daily objects
  - Rich **color** and texture information
  - Exploit both **color** and **depth** information

# Color Point Pair Feature



- **PPF** (Drost et al.): 4 dimensional
- **CPPF** (proposed): 10 dimensional

# Why Color Points?



To **prune** unnecessary feature matching

- **Point Pair Feature**

- Objects having rich variations in surface normals
- **Inefficient** for planar or self-symmetric objects
- **False matching** from background clutter

- **Color Point Pair Feature**

- **Prune** potentially false matches based on **color similarity**
- HSV color space
- More **efficient** because unnecessary votes are skipped

# Parallel Implementation



- parallel NVIDIA Thrust lib
  - reduction
  - counting
  - partition
  - binary search
  - sorting
  - ...

# Test Objects



Clorox



Flash



Kuka Mug



Milk



MVG Book



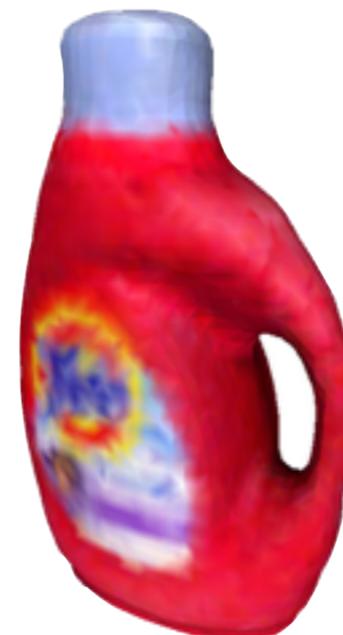
Orange Juice



Pringles



Starbucks Mug



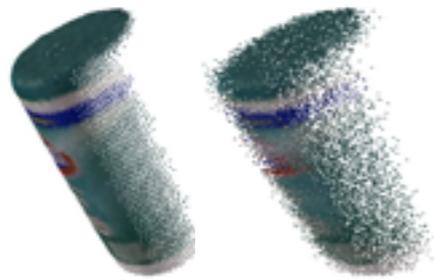
Tide



Wrench

# Performance Evaluation

Dataset



Gaussian noise



MOSI



SOMI



Real cluttered scenes

Compared Approaches



Hinterstoisser et al., PAMI'11  
with/without ICP

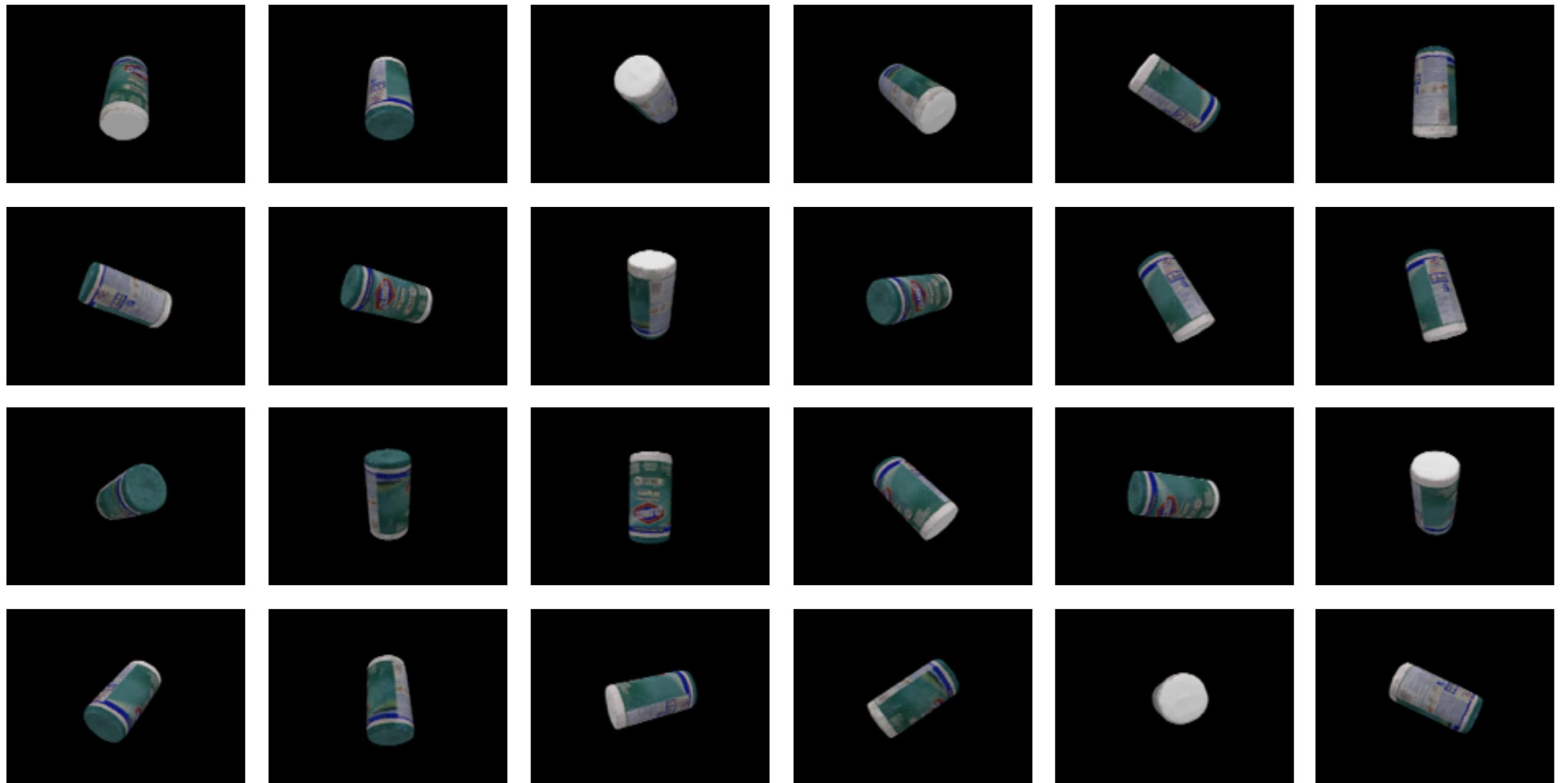
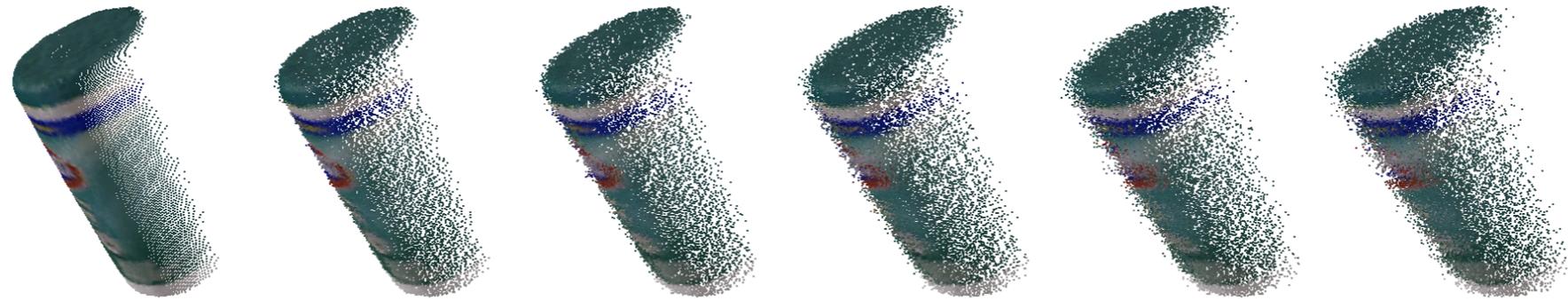


Papazov et al., IJRR'12

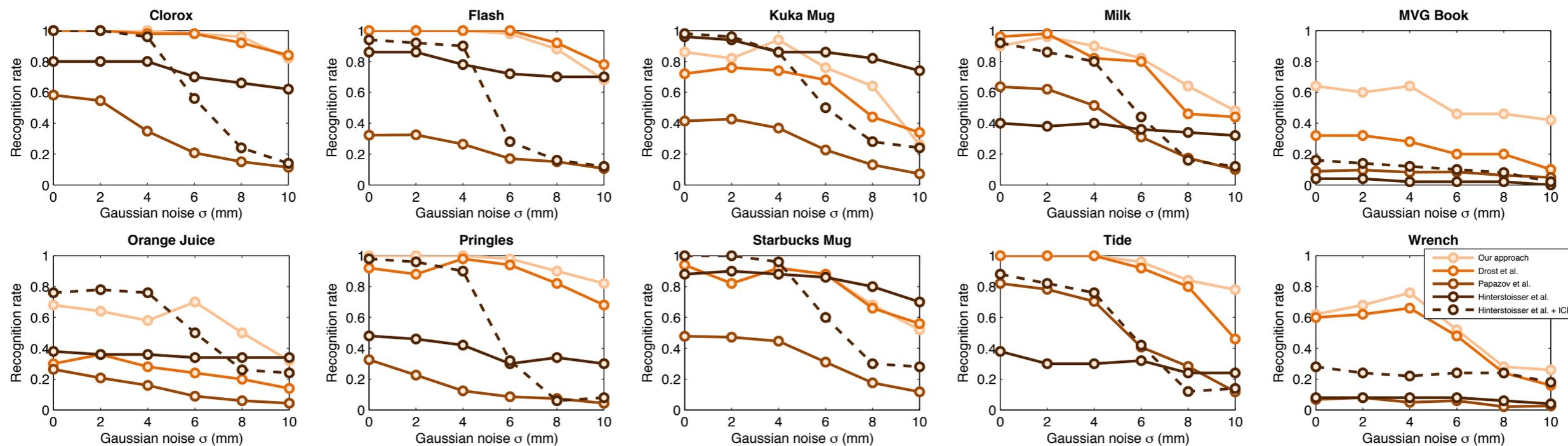
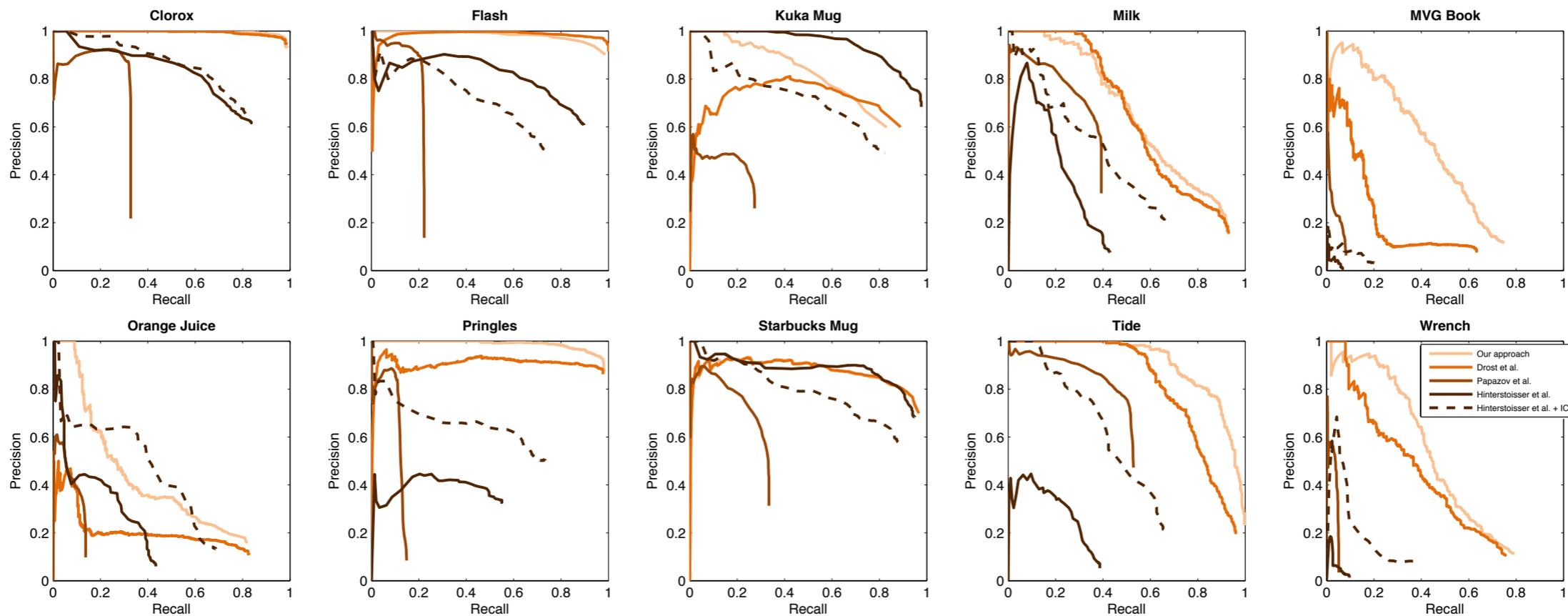


Drost et al., CVPR'10

# Dataset: Gaussian noise



# Results: Gaussian noise



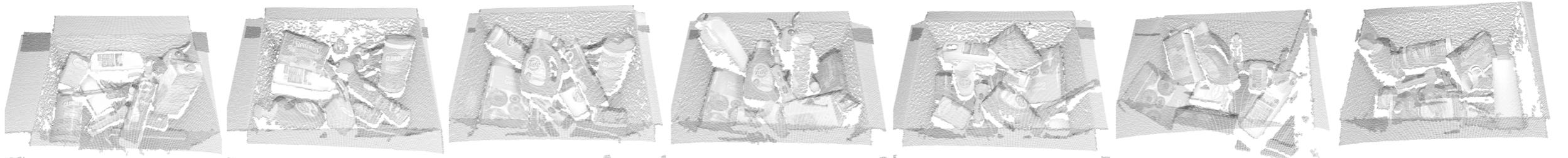
# Cluttered Scenes



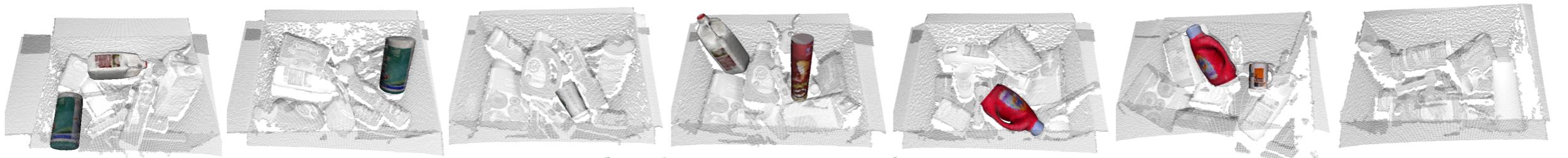
# Pose Estimation Results



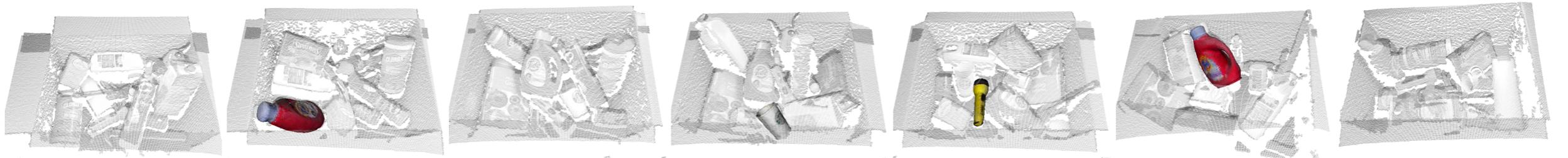
[1]



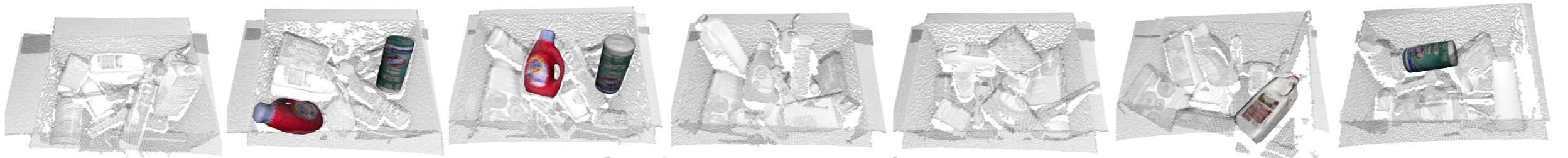
[2]



[3]



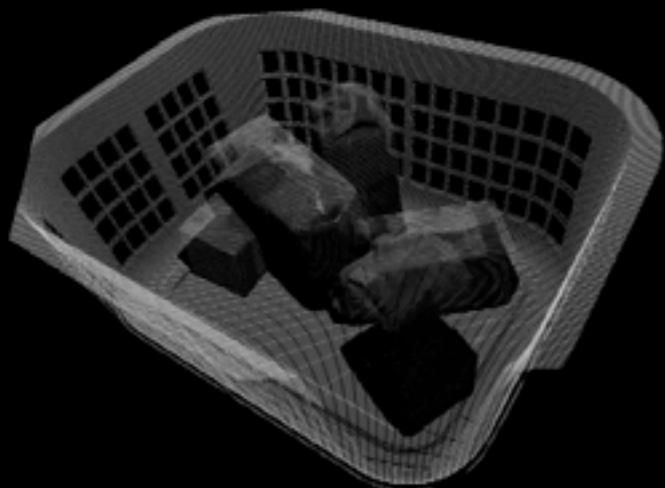
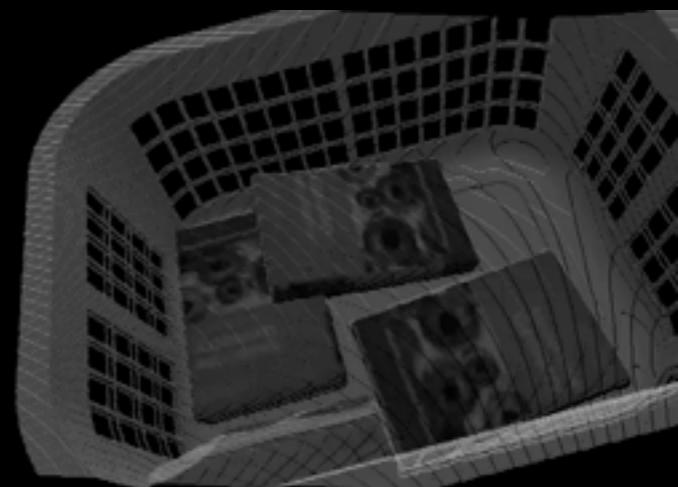
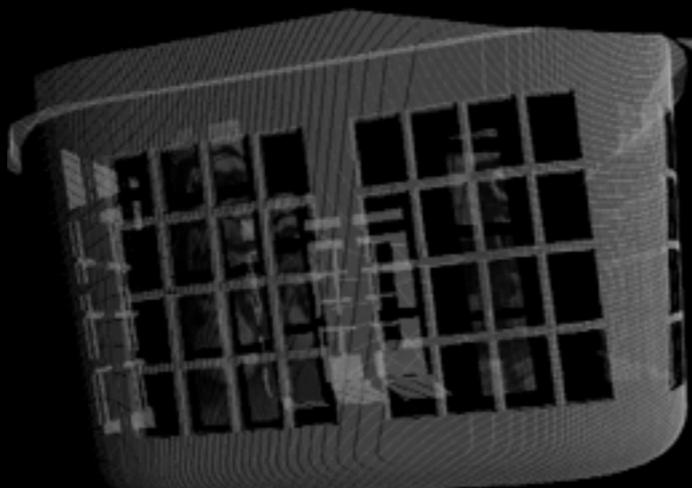
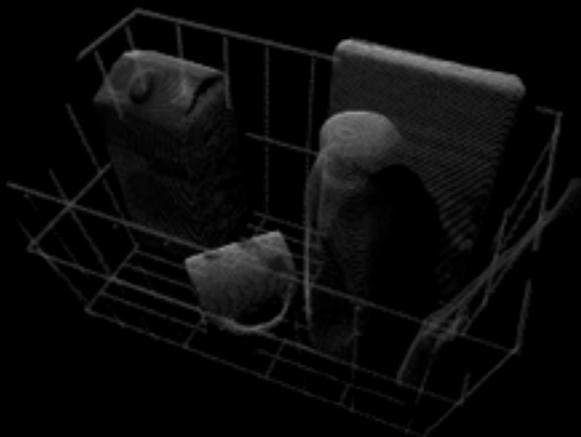
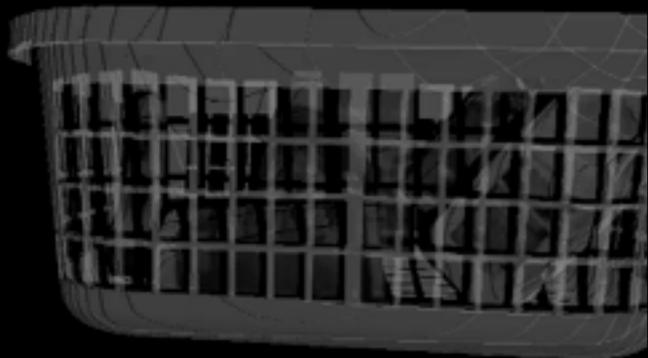
[4]



[5]



Hinterstoisser et al. without [1] and with ICP [2], Papazov et al. [3], Drost et al. [4], and ours [5]



# Approaches



- 2D Visual Information (Monocular Camera)
  - Combining Keypoint and Edge Features [ICRA'10, ICRA'11, IJRR'12]
  - Extending to Textureless Objects [IROS'12]



- 3D Visual Information (RGB-D Camera)
  - Voting-based Pose Estimation using Pair Features [ICRA'12, IROS'12]
  - **Object Pose Tracking** [IROS'13]

real-time



# Motivations



- Posterior p.d.f. as a set of weighted particles
- **Slow** frame rate due to a serial likelihood evaluation of particles
- Inherently **parallel** algorithm
- each particle weight update is **independent** of other updates

To **parallelize** the time-consuming likelihood evaluation

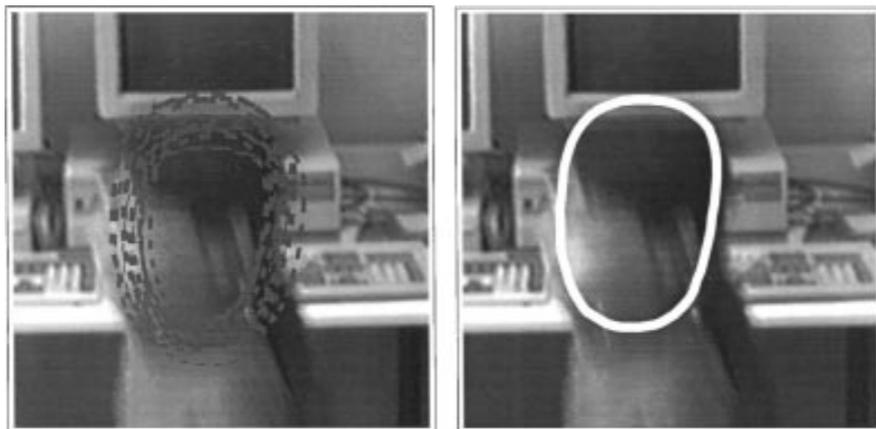
# Contributions



- Rich features from RGB-D channels (colors, points, normals)
- Frame Buffer Object (FBO) in OpenGL & CUDA OpenGL interoperability
- Multiple object rendering

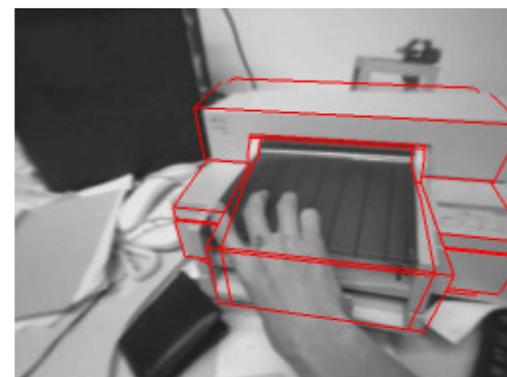
# Related Work

Edges



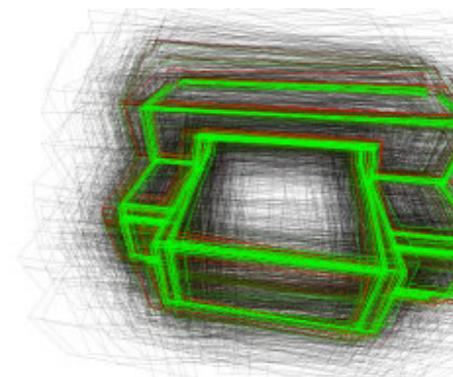
[Isard, IJCV'98]

Condensation in 2D

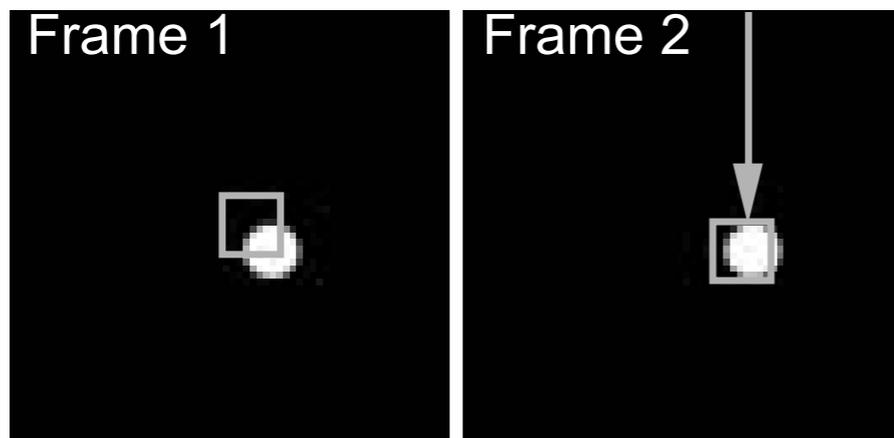


[Klein, BMVC'06]

Fast PF using GPU shader



Intensity



[Montemayor, SIGGRAPH'04]

Simple PF on GPU

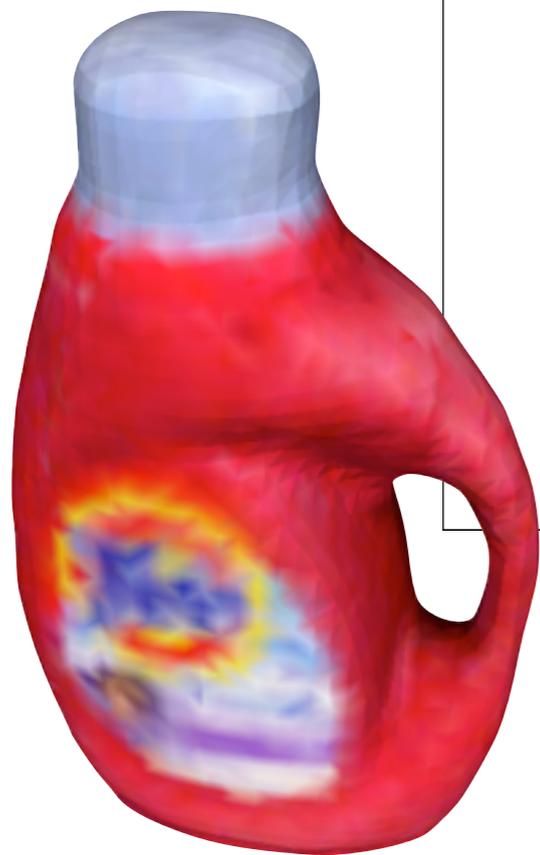


[Azad, ICRA'11]

Fast PF using CUDA

Employ **rich** features: *depth*, *normals*, and *color*

# Likelihood Evaluation



# Likelihood Evaluation

RGB-D scene

rendered object

a point in  $\mathbf{M}_t$

$$p(\mathbf{Z}_t | \mathbf{X}_t^{(n)}, \mathbf{M}_t) = \prod_{(i,j) \in \mathcal{A}} p(\mathbf{z}_t^{(i)} | \mathbf{X}_t^{(n)}, \mathbf{m}_t^{(j)})$$

n-th pose

a point in  $\mathbf{Z}_t$

$$\mathcal{A} = \{(i, j) | \text{proj}(\mathbf{x}(\mathbf{z}_t^{(i)})) = \text{proj}(\mathbf{X}_t^{(n)} \cdot \mathbf{x}(\mathbf{m}_t^{(j)}))\}$$

# Distance functions

$$d_e(\mathbf{x}_1, \mathbf{x}_2) = \begin{cases} \|\mathbf{x}_1 - \mathbf{x}_2\| & \text{if } \|\mathbf{x}_1 - \mathbf{x}_2\| \leq \tau \\ 1 & \text{otherwise} \end{cases}$$

Euclidean distance

$$d_n(\mathbf{n}_1, \mathbf{n}_2) = \frac{\cos^{-1}(\mathbf{n}_1^\top \mathbf{n}_2 - 1)}{\pi}$$

Normal distance

$$d_c(\mathbf{c}_1, \mathbf{c}_2) = \|\mathbf{c}_1 - \mathbf{c}_2\|$$

Color distance

# Likelihood Evaluation

$$p(\mathbf{Z}_t | \mathbf{X}_t^{(n)}, \mathbf{M}_t) = \prod_{(i,j) \in \mathcal{A}} p(\mathbf{z}_t^{(i)} | \mathbf{X}_t^{(n)}, \mathbf{m}_t^{(j)})$$

$$\begin{aligned}
 p(\mathbf{z}_t^{(i)} | \mathbf{X}_t^{(n)}, \mathbf{m}_t^{(j)}) &= \exp^{-\lambda_e \cdot d_e(\mathbf{x}(\mathbf{z}_t^{(i)}), \mathbf{X}_t^{(n)} \cdot \mathbf{x}(\mathbf{m}_t^{(j)}))} \\
 &\cdot \exp^{-\lambda_n \cdot d_n(\mathbf{n}(\mathbf{z}_t^{(i)}), \mathbf{X}_t^{(n)} \cdot \mathbf{n}(\mathbf{m}_t^{(j)}))} \\
 &\cdot \exp^{-\lambda_c \cdot d_c(\mathbf{c}(\mathbf{z}_t^{(i)}), \mathbf{c}(\mathbf{m}_t^{(j)}))}
 \end{aligned}$$



Ours



PCL tracking



Ours

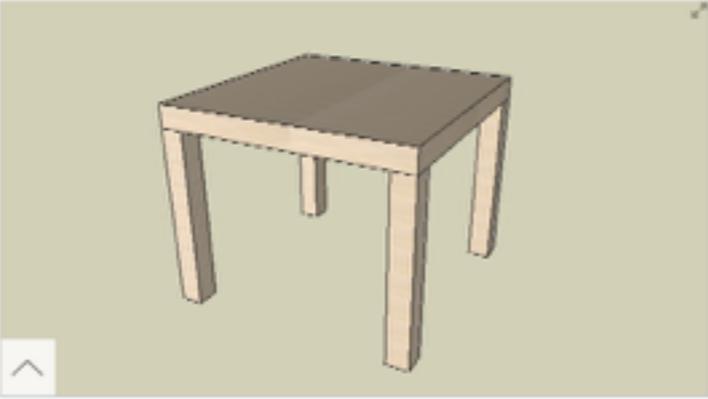


PCL tracking

# 3D models on the Web

SketchUp 3D Warehouse

## IKEA LACK Side Table



Download

Downloads	33,454
.skp File Size	32.4 kB
Polygons	24
Materials	1
Uploaded	7/12/07
Last Modified	3/12/14

Share Embed

Abhimat  
13 models

Tags  
Furniture, IKEA, IKEA LACK, IKEA Side Table, LACK, Side Table

This is a model of the LACK Side Table available from IKEA. The color of this model is Birch Effect.  
For more information, visit: <http://www.ikea.com/us/en/rcaaling/products/48104270>

SketchUp 3D Warehouse

## bookcase IKEA EXPEDIT 149x79 cm



Download

Downloads	11,002
.skp File Size	32.9 kB
Polygons	61
Materials	16
Uploaded	1/16/07
Last Modified	3/12/14

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Julien Perret  
5 models

Tags  
bookcase, furniture, IKEA, meuble, étagère

a bookcase from IKEA.  
For more information, visit: <http://julien.perret.googlepages.com/sketchup3dcomponents>

SketchUp 3D Warehouse

## IKEA Karlstad Canapea 2 locuri



Download

Downloads	628
.skp File Size	68.5 kB
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Share Embed

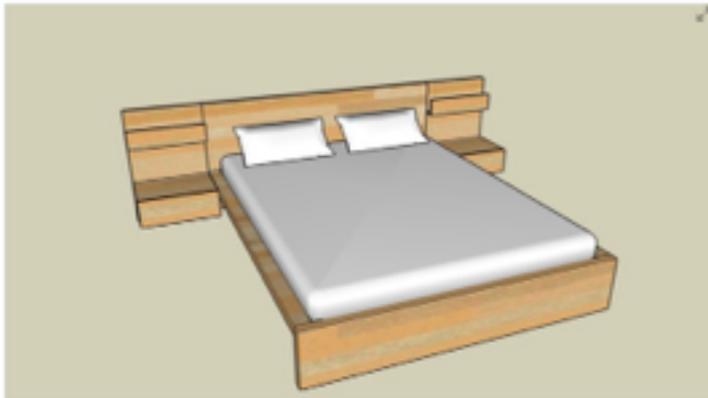
Iedu  
16 models

Tags  
canapea, IKEA

Dimensiuni produs L&Aime: 165 cm, Ad&ncime: 94 cm, l&Aime ansamblat: 80 cm, Ad&ncime per&nt: 56 cm, l&Aime per&nt: 45 cm

SketchUp 3D Warehouse

## IKEA Malm Queen Platform Bed with Nightstands



Download

Downloads	50,388
.skp File Size	125.1 kB
Polygons	255
Materials	10
Uploaded	6/9/08
Last Modified	3/12/14

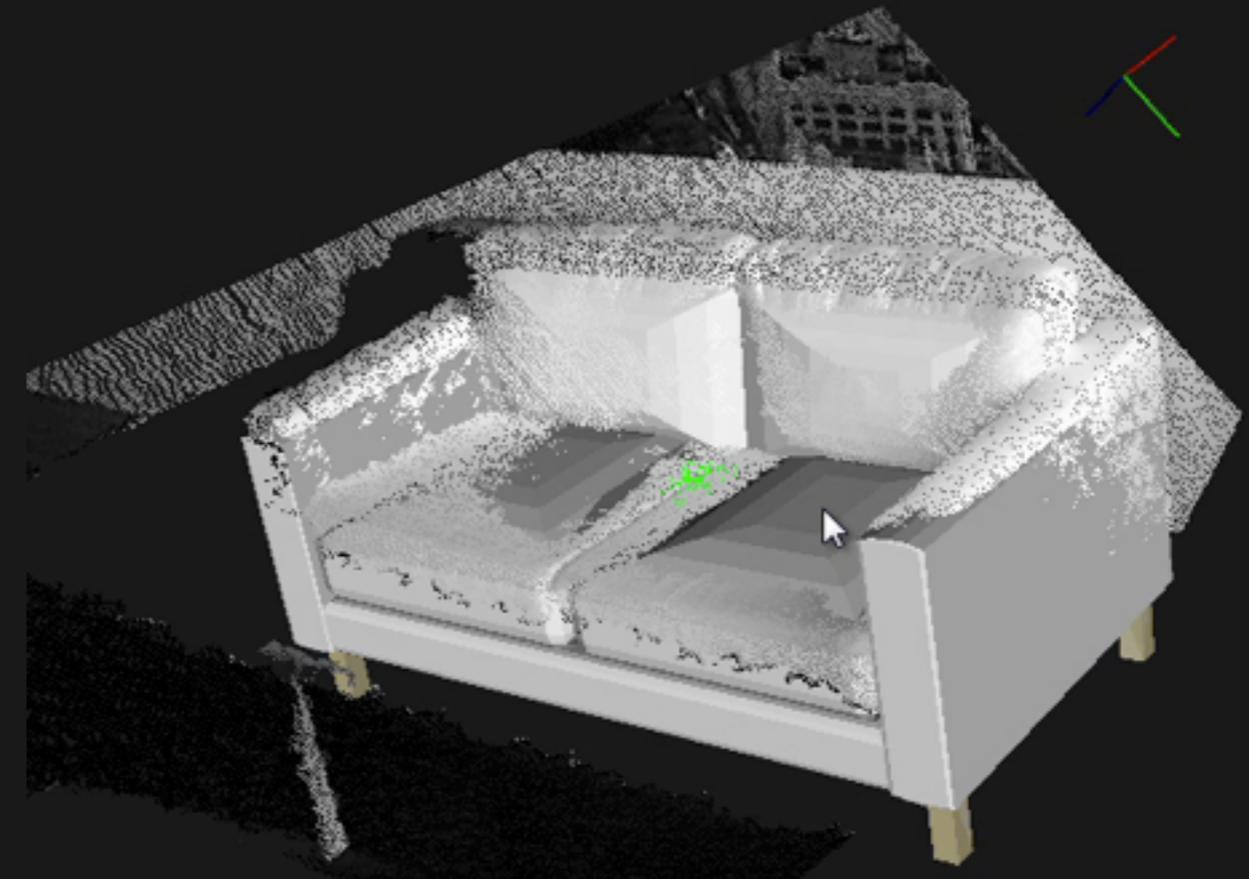
Share Embed

dianejwright  
9 models

Tags  
bed, malm, platform, queen

Queen platform bed for the Malm series. Birch finish. 2 attached nightstands.  
For more information, visit: <http://www.ikea.com/us/en/rcaaling/products/569849241>

real-time



SketchUp 3D Warehouse Sign in Search 3D Warehouse

**HermanMiller**

### Herman Miller Aeron Chair



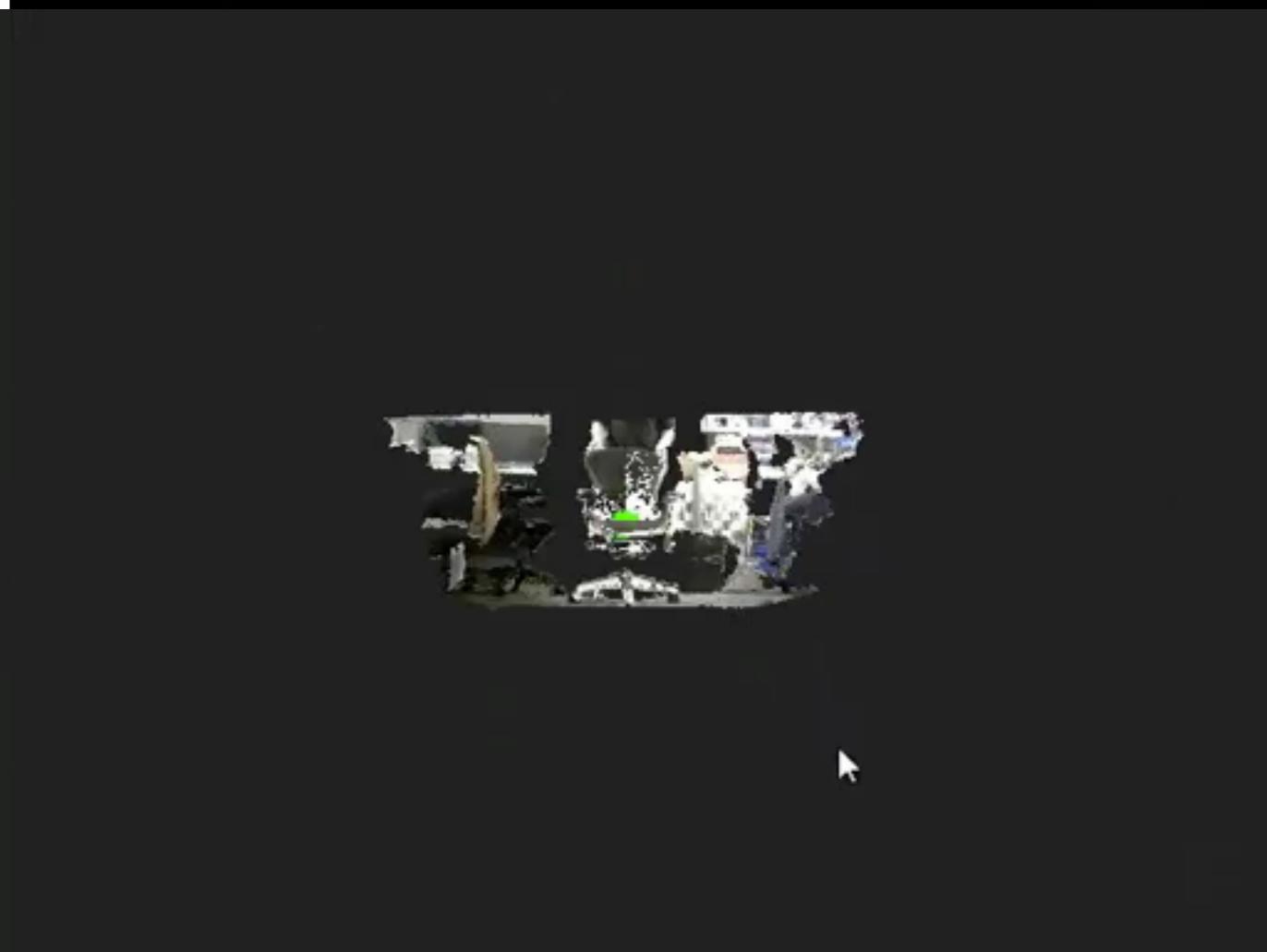
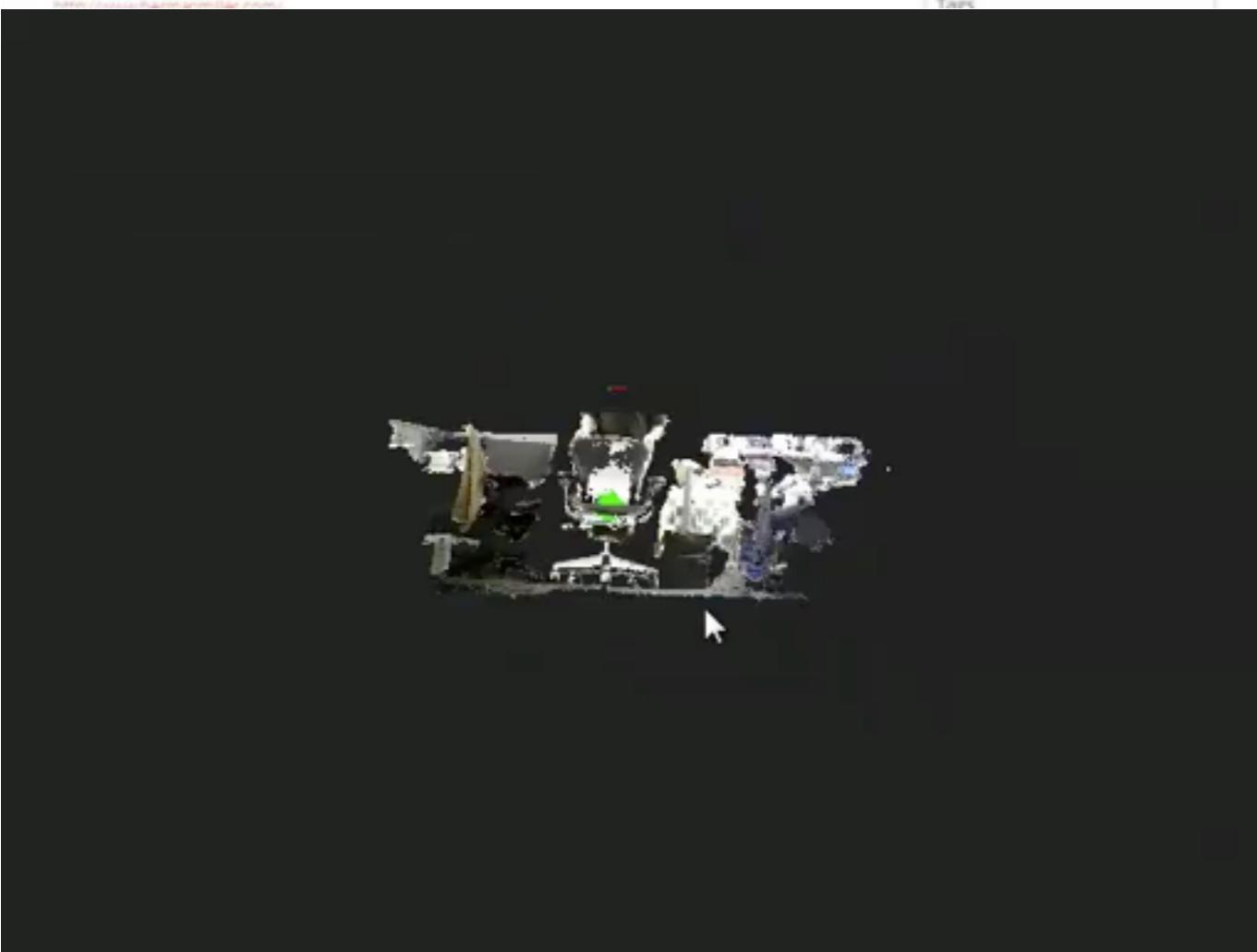
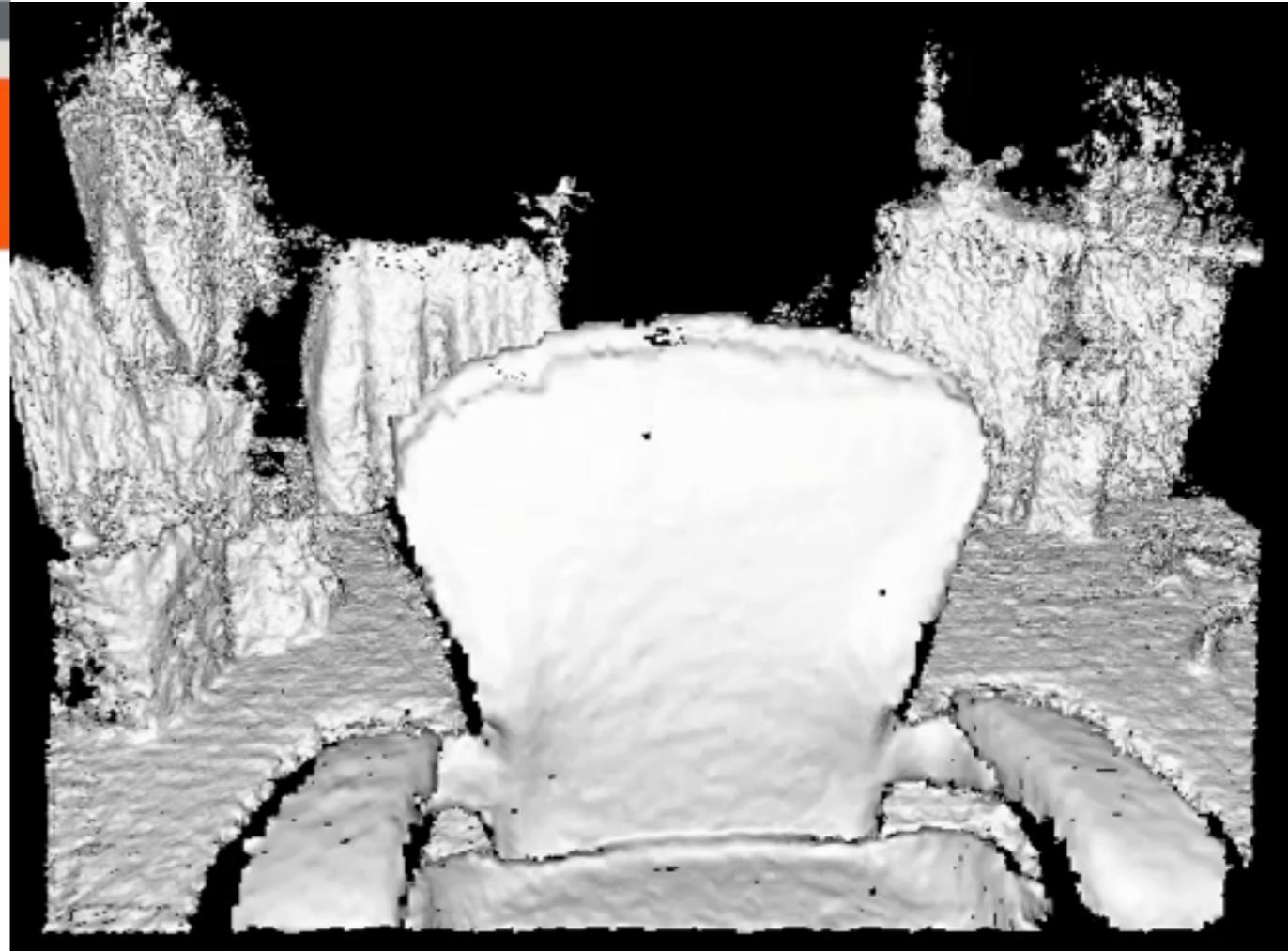
**Download**

Downloads	313
.skp File Size	2.2 MB
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Uploaded	3/4/14
Last Modified	3/4/14

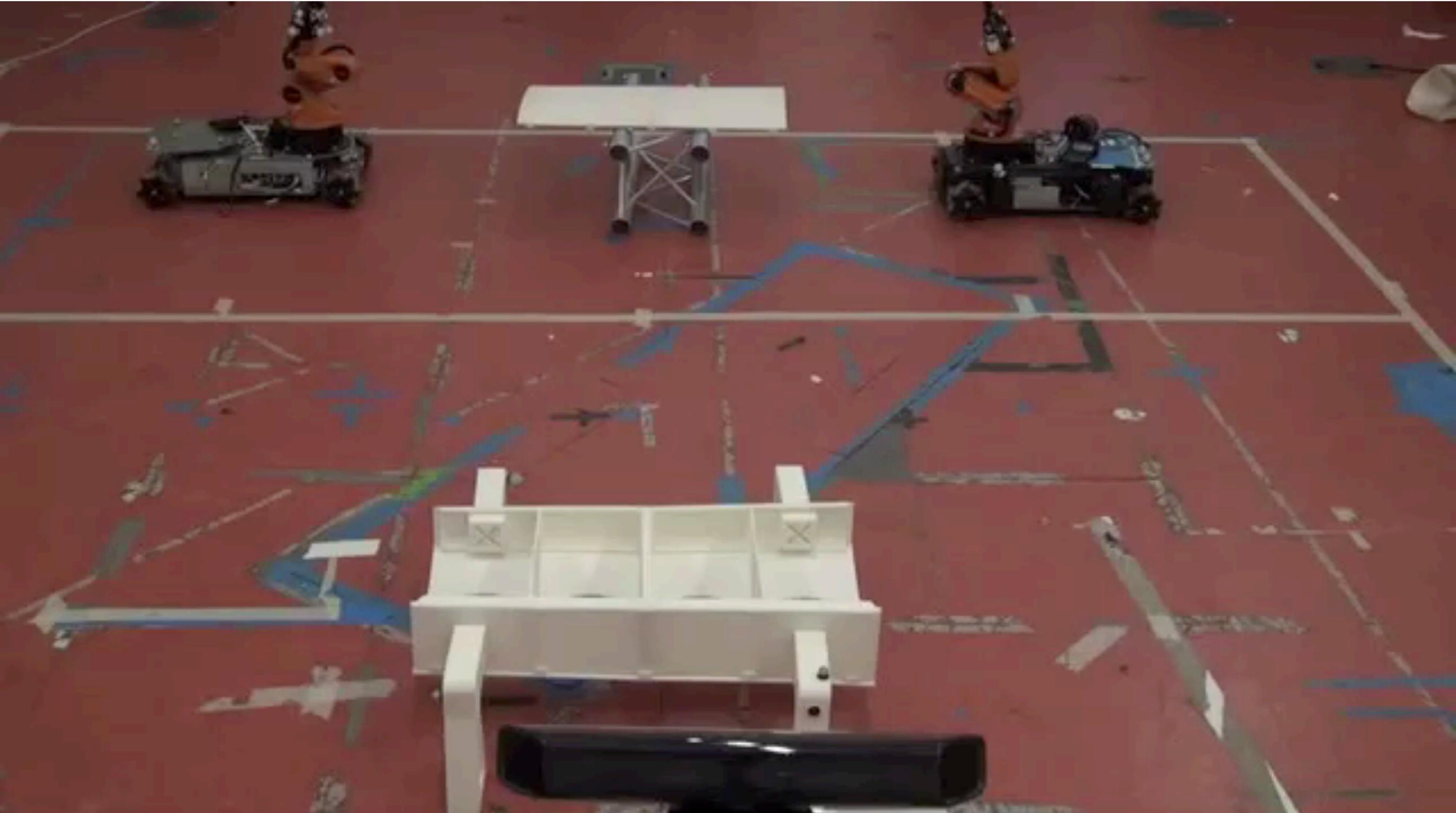
Share Embed

**Herman Miller**  
44 models

For more information, visit:  
<http://www.hermanmiller.com>



# Robotic Assembly



# Conclusions

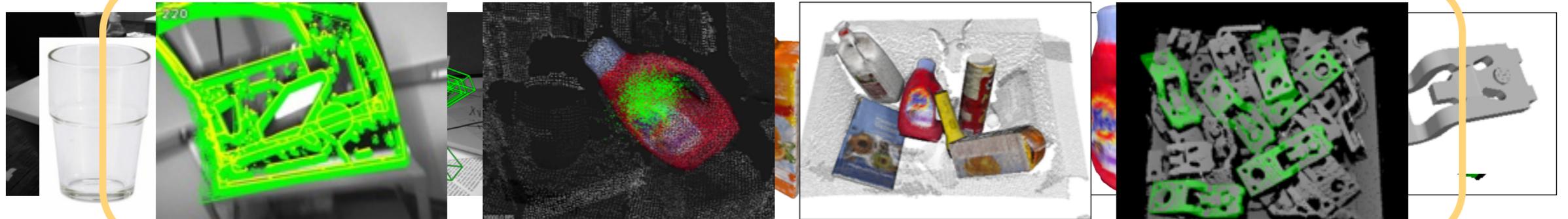


- Contributed toward robust object perception in unstructured environments

## Four challenges

- object perception regardless of the degree of texture
- highly cluttered backgrounds
- object discontinuities
- real-time constraints
- combined photometric and geometric features
- multiple pose hypotheses frameworks
- combined pose estimation and tracking
- parallelized on GPU

# Revisit Thesis Statement



- To close the loop between the **geometric era** of early computer vision and the currently dominating **appearance age**, both **photometric** and **geometric** features need to be considered.
- The **combination** of these features enables object perception algorithms not only to be **more effective** but also to handle an **increased spectrum of objects**.
- **Two theoretical frameworks** using **multiple pose hypotheses** based on combined features are contributed in this thesis.
- These new frameworks are **robust** to significant **clutter** and **occlusions**, and are therefore **efficacious** solutions for visual object perception in **unstructured** environments.

# Future Work



- Object model adaptation
- Object modeling
- Multi-object tracking
- Scalable object perception
- Object categorization

# Thank You



Henrik Christensen  
Gatech



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UW



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Gatech



Jim Rehg  
Gatech



Anthony Yezzi  
Gatech



Alex Trevor  
Gatech



Yuichi Taguchi  
MERL



Ming-Yu Liu  
MERL



Srikumar Ramalingam  
MERL



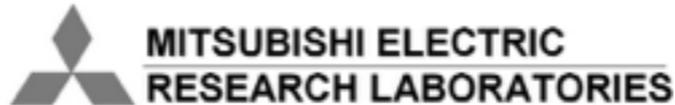
Oncel Tuzel  
MERL



Ross Knepper  
MIT



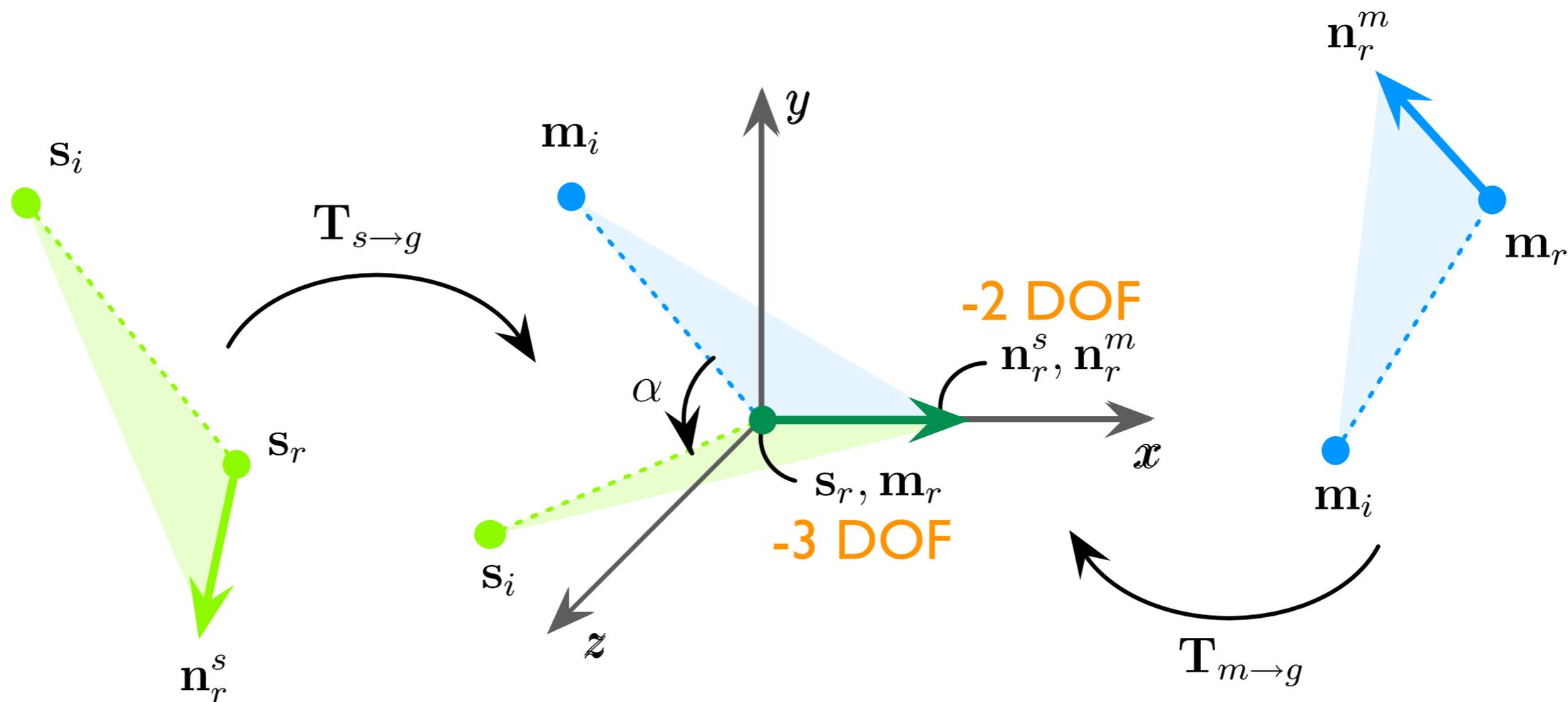
Mehmet Dogar  
MIT





# Backup Slides

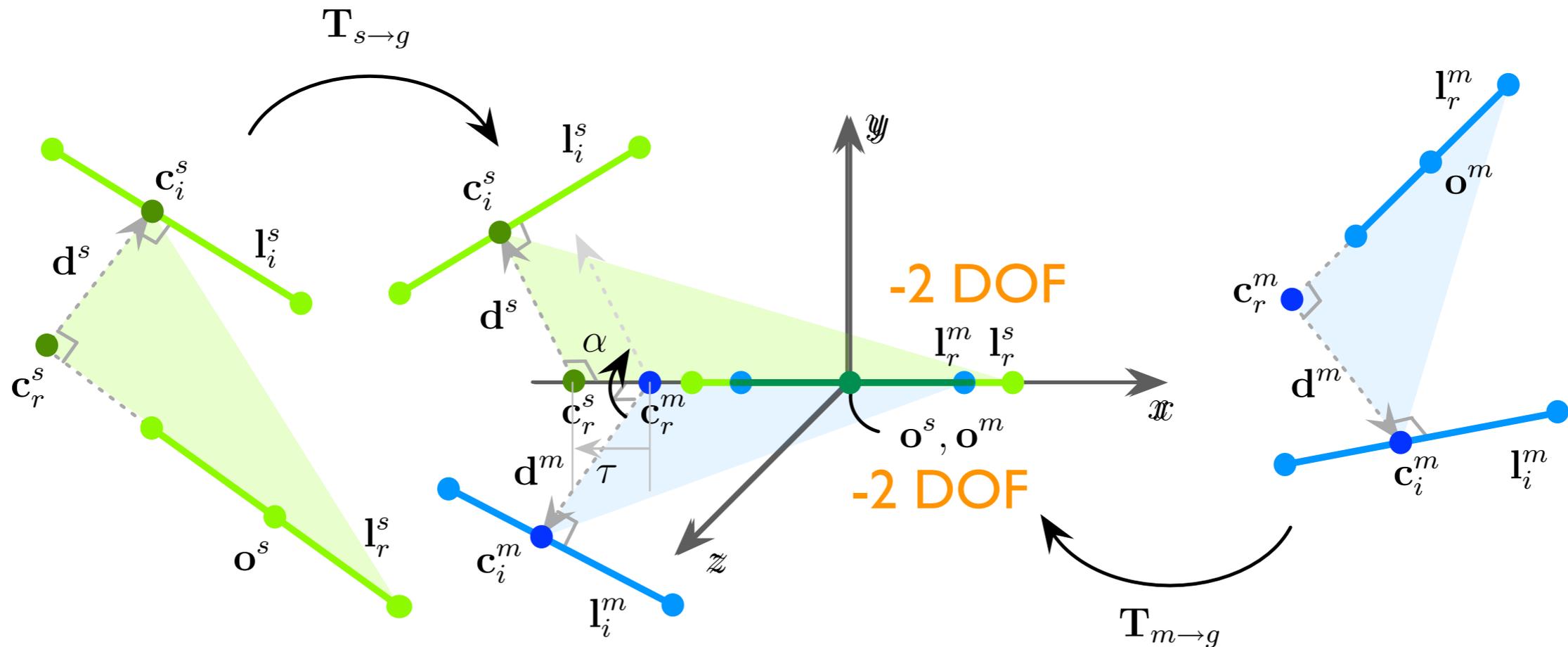
# Voting Scheme I



$$\mathbf{s}_i = \mathbf{T}_{s \rightarrow g}^{-1} \mathbf{R}_x(\alpha) \mathbf{T}_{m \rightarrow g} \mathbf{m}_i$$

- 2D accumulator space:  $(\mathbf{m}_r, \alpha)$
- $S2S$ ,  $B2B$ , and  $S2B$  share the same transform

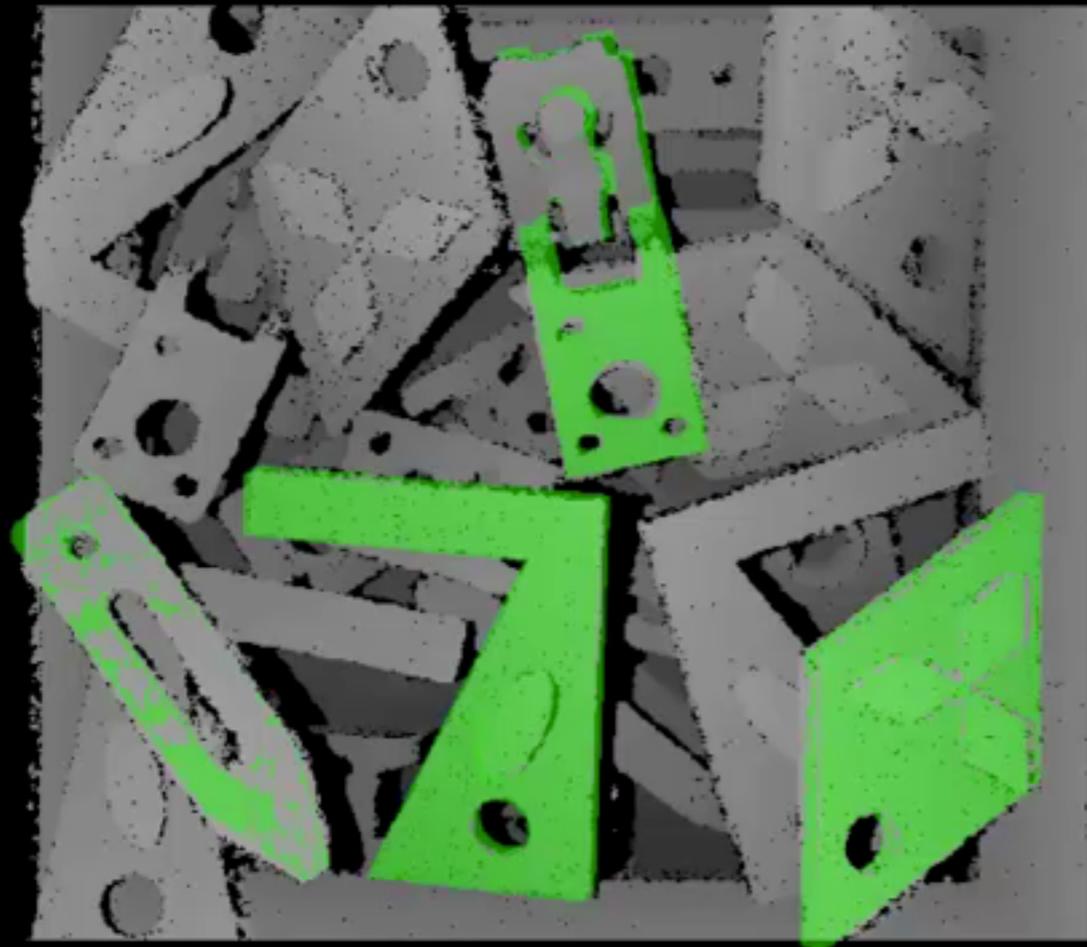
# Voting Scheme II



$$\mathbf{l}_i^s = \mathbf{T}_{s \rightarrow g}^{-1} \mathbf{T}_{\mathbf{x}}(\tau) \mathbf{R}_{\mathbf{x}}(\alpha) \mathbf{T}_{m \rightarrow g} \mathbf{l}_i^m$$

- 3D accumulator space:  $(\mathbf{o}^m, \alpha, \tau)$

# Real Scan: *S2B* feature



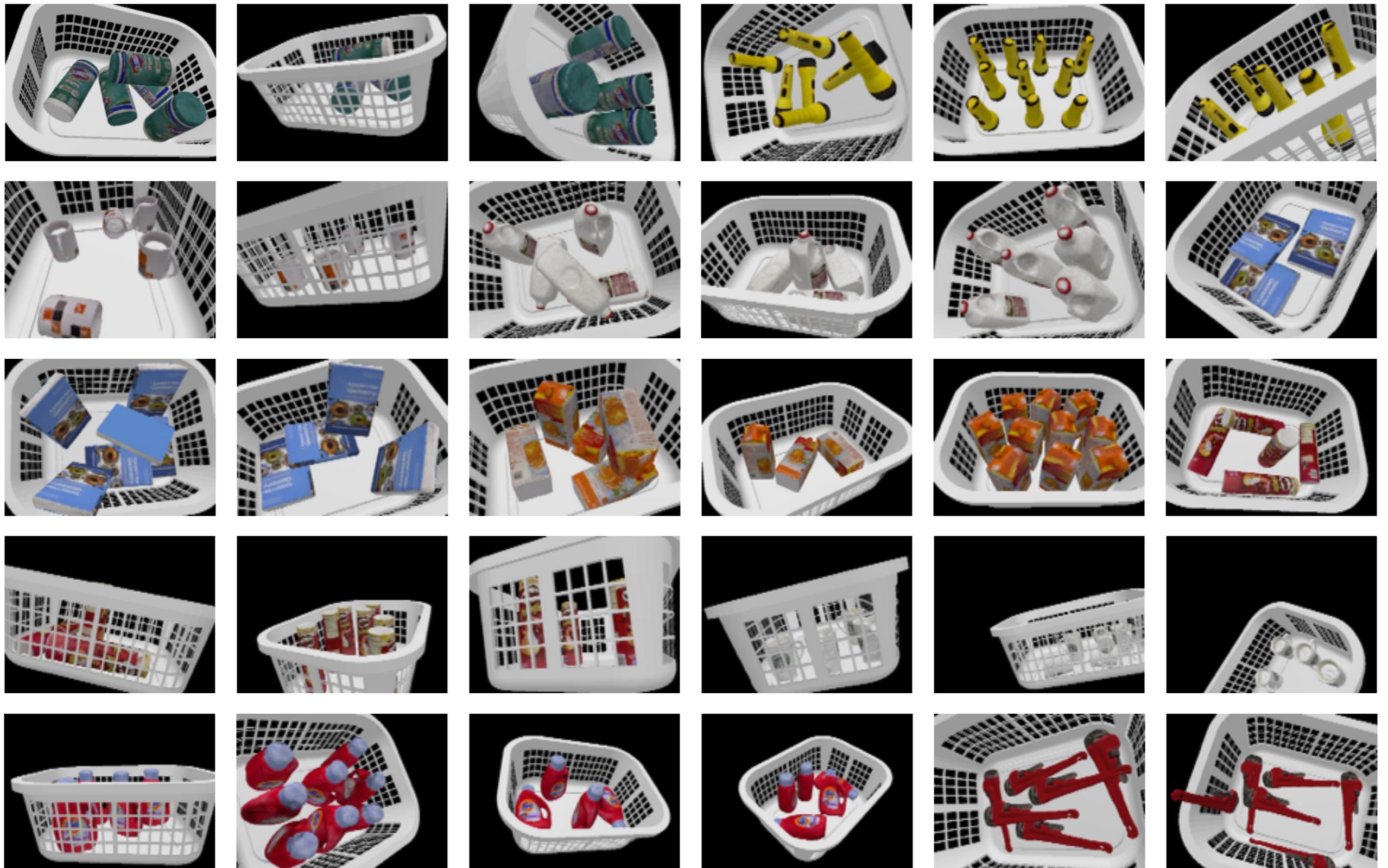


# Results: MOSI

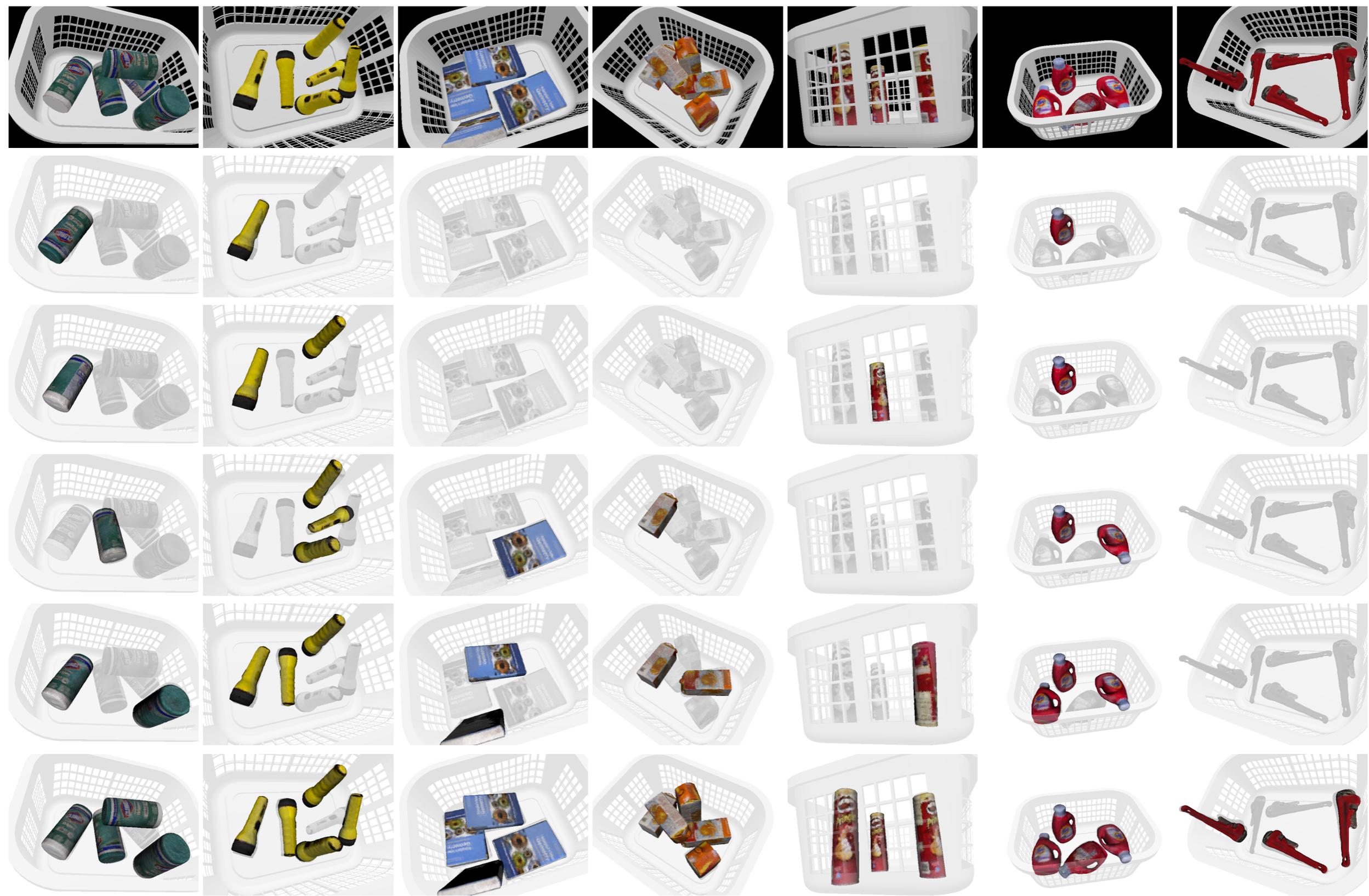


Hinterstoisser et al. without [1] and with ICP [2], Papazov et al. [3], Drost et al. [4], and ours [5]

# Dataset: SOMI



# Results: SOMI



Hinterstoisser et al. without [1] and with ICP [2], Papazov et al. [3], Drost et al. [4], and ours [5]