

## HW #7 SOLUTIONS

### #1 Qualitative

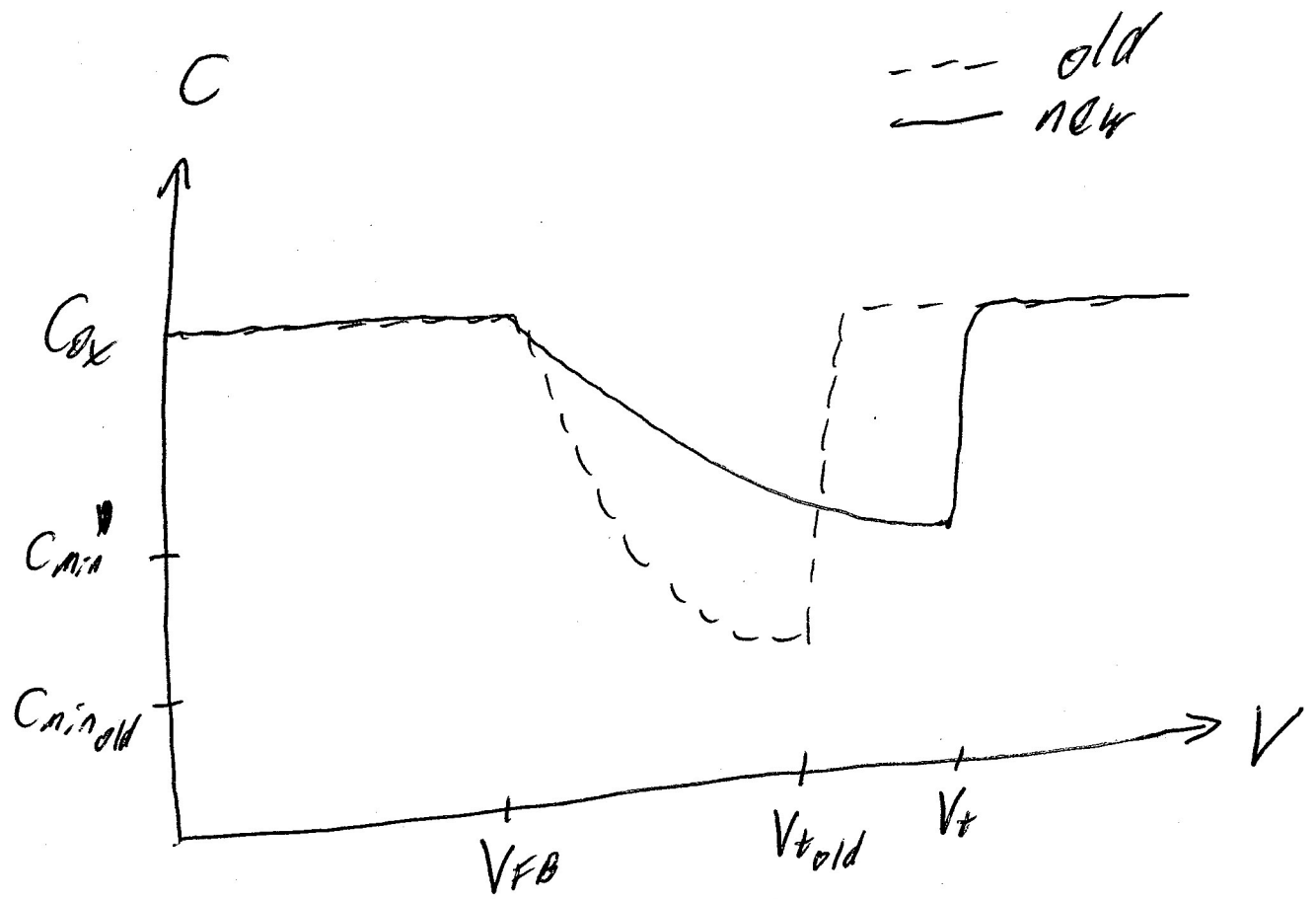
- $\bar{\mu}_n$  stays constant (approximately) because the implant does not extend to the surface of the device
- $V_{FB}$  stays approximately constant, again because only the surface doping is important at  $f_b$ .
- $W_{max}$  decreases because as the depletion edge extends into the silicon, it runs into the higher concentration. Then more ions are available to take up the field and  $W_{max}$  tends to clamp at the implant depth.

$$\rightarrow V_t = \Delta\phi_{ms} + 2\phi_f + \frac{e\alpha_x}{\epsilon_{ox}} \sqrt{2q\epsilon_s N_a 2\phi_f}$$

Since  $N_a$  at  $W_{max}$  has effectively increased,  $V_t$  increases, slightly.

Note that  $\phi_s$  must remain =  $2\phi_f$ , a constant,

i.e.  $E_{ox} \uparrow$  relative to the old values  
 $\Delta V_{ox} \uparrow$

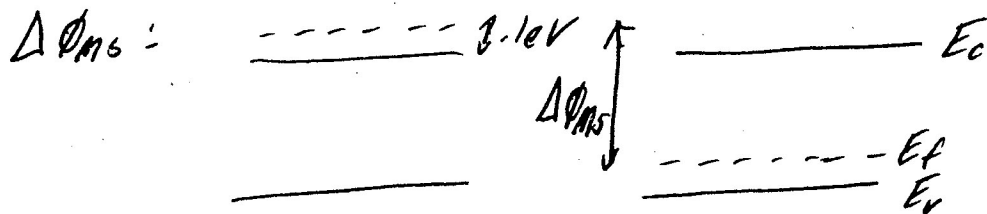


$V_t \uparrow$   
 $W_{max} \downarrow, \therefore C_{min} \uparrow$   
 $V_{FB} \text{ const}$   
 $C_{ox} \text{ const}$

② Quantitative

a.)  $V_{FB} = \Delta\phi_{ms} - \frac{Q_F}{C_F}$

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$$\rho = N_v e^{-\frac{(E_f - E_v)}{kT}}$$

$$10^{16} = 1.04 \times 10^{19} e^{-\frac{(E_f - E_v)}{kT}}$$

$$E_f - E_v = 0.18 \text{ eV}$$

$$q\Delta\phi_{ms} = -(E_c - E_f + 0.1 \text{ eV})$$

$$\Delta\phi_{ms} = (-0.92 \text{ eV} + 0.1 \text{ eV}) = -1.02 \text{ eV}$$


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$\frac{Q_F}{C_F} :$

$$Q_F = 2 \times 10^{-8} \text{ coul}$$

$$C_F = \frac{\epsilon_{ox}}{\frac{1}{2} T_{ox}} = 2.3 \times 10^{-3} \text{ F/cm}^2$$

$$\frac{Q_F}{C_F} = 0.09 \text{ V}$$


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$V_{FB} = -1.11 \text{ V}$

$$b.) V_t = V_{FB} + 2\phi_f + |V_{BS}| + \frac{tox}{\epsilon_{ox}} \sqrt{2q\epsilon_s N_a (2\phi_f + |V_{BS}|)}$$

$$2\phi_f = 2kT \ln \frac{N_a}{n_i} = .71V$$

$$|V_{BS}| = 2V$$

$$V_t = -1.11 + .71 + 2 + .82$$

$$\boxed{V_t = 2.42V}$$

$$c.) I_{Dsat} = \frac{Z \mu_n C_{ox}}{2L} (V_g - V_t)^2$$

$$C_{ox} = 115 \text{ nF/cm}^2$$

$$\boxed{I_{Dsat} = .21 \text{ mA}}$$

d.) We already know  $V_{FB}$ ,  $V_t$ ,  $C_{ox}$ ,  
All we need is  $C_{min}$

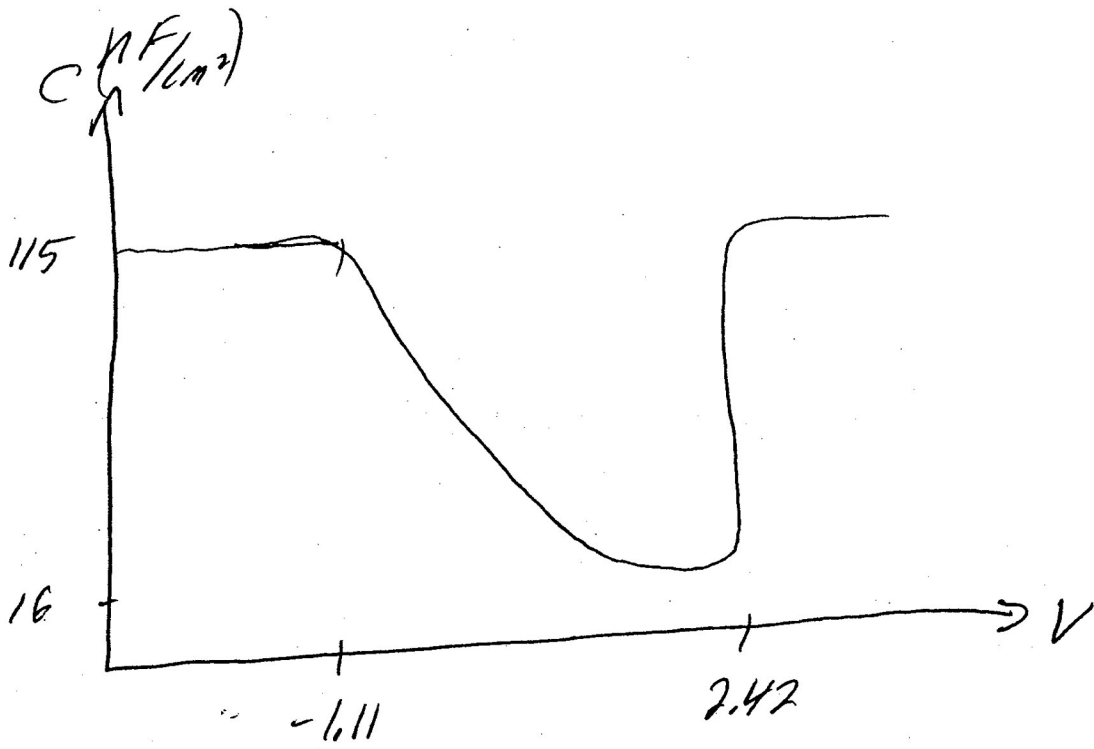
$$C_{min} \rightarrow \begin{array}{c} | \quad | \\ \hline C_{ox} \quad C_{dep,max} \end{array}$$

$$C_{dep,max} = \frac{\epsilon_s}{W_{max}}$$

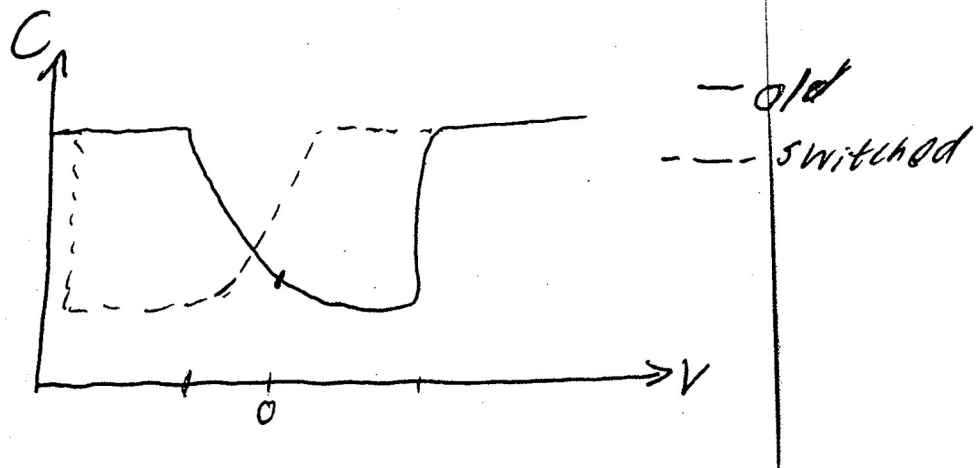
$$W_{max} = \sqrt{\frac{2\epsilon_s (2\phi_f + |V_{BS}|)}{qN_a}} = .59 \mu\text{m}$$

$$C_{dep,max} = \frac{\epsilon_s}{W_{max}} = 18 \text{ nF/cm}^2$$

$$C_{min} = \frac{C_{ox} C_{dep}}{C_{ox} + C_{dep}} = 16 \text{ nF/cm}^2$$

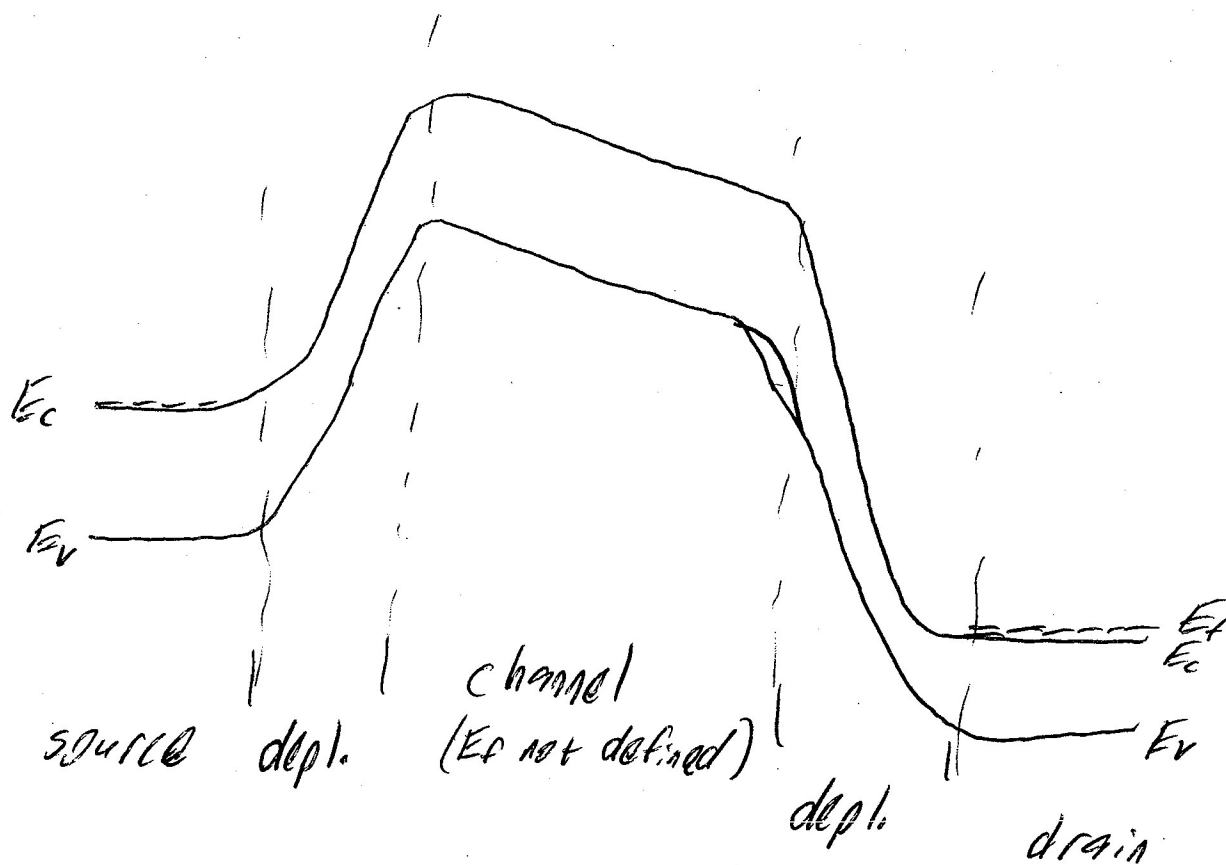


If  $n+p$  are switched, then  $\Delta\phi_{ns}$ ,  $2\phi_f$  &  $\Delta\phi_{ox}$  change signs.  $-\frac{Q_f}{C_f}$  stays constant. Also the voltages must change sign or we will forward bias the source-substrate & drain substrate junctions.

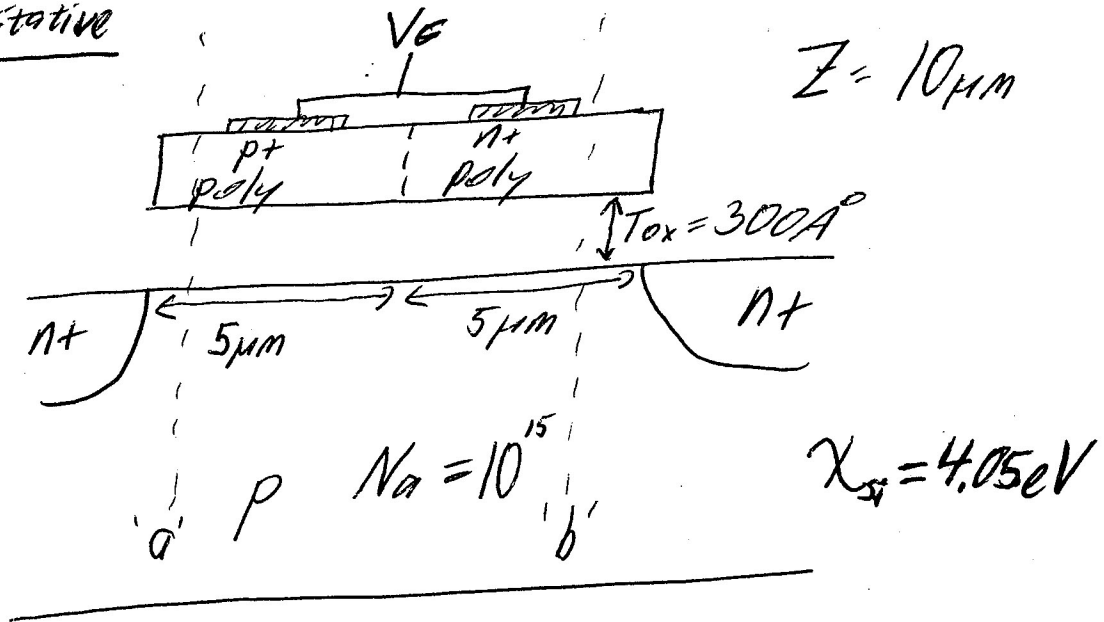


e.) If  $V_g = 0V$  &  $V_{sub} = 0V$ , then  $\phi_s = 0V$

$$V_s = 2V \quad V_d > V_{dsat} (> 2V)$$



3. Quantitative

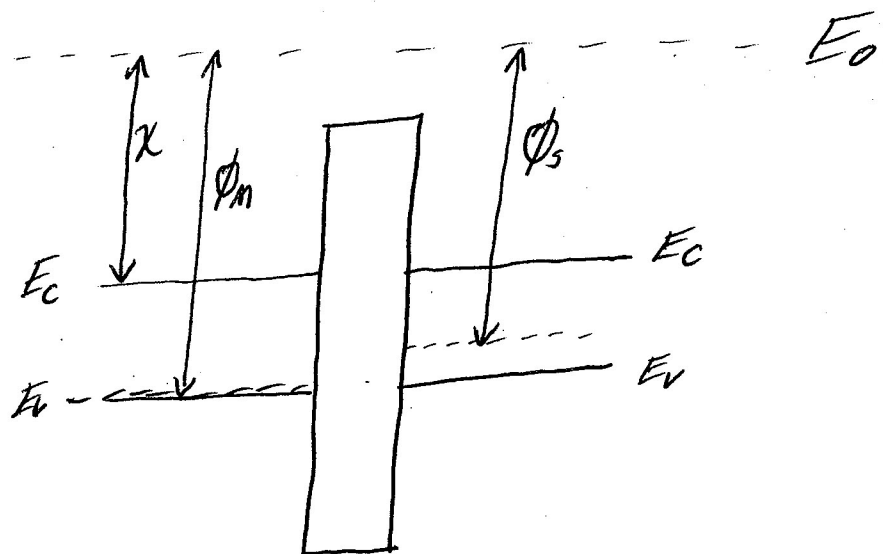


a) Find  $C_{ox} \left( \frac{F}{\text{cm}^2} \right)$

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} = \frac{(3.9)(8.854 \times 10^{-14} \frac{F}{\text{cm}})}{(300 \times 10^{-8} \text{ cm})}$$

$$C_{ox} = 1.15 \times 10^{-7} \frac{F}{\text{cm}^2}$$

b.)  $V_{FB}$  @ 'a'



$$\begin{aligned} \phi_m &= \chi + E_c - E_f \\ &= \chi + E_c - E_v = \chi + E_g \\ &= 4.05 + 1.1 \text{ eV} = \underline{5.15 \text{ eV}} \end{aligned}$$

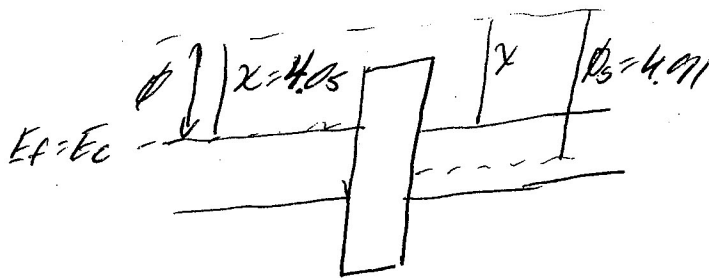
$$\begin{aligned}
 \phi_s &= \chi + E_c - E_f \\
 &= \chi + [(E_c - E_v) - (E_f - E_v)] \\
 &= 4.05 \text{ eV} + [1.1 \text{ eV} - (E_f - E_v)] \\
 -(E_f - E_v) &= kT \ln \frac{N_a}{N_v} \\
 &= .026 \text{ eV} \ln \frac{10^{15} \text{ cm}^{-3}}{1.04 \times 10^{19} \text{ cm}^{-3}} \\
 E_f - E_v &= .24 \text{ eV}
 \end{aligned}$$

$$\phi_s = 4.05 \text{ eV} + (1.1 \text{ eV} - .24 \text{ eV})$$

$$\underline{\phi_s = 4.91 \text{ eV}}$$

$$\boxed{qV_{FB_a} = \phi_m - \phi_s = +.24 \text{ eV}}$$

$V_{FB}$  @ 'b'



$$\begin{aligned}
 \phi_m &= \chi = 4.05 \text{ eV} \text{ since } E_c = E_f \\
 \phi_s &= 4.91 \text{ eV} \text{ as before}
 \end{aligned}$$

$$\boxed{qV_{FB_b} = \phi_m - \phi_s = -.86 \text{ eV}}$$



$$c.) V_T = V_{FB} + 2\phi_f + \frac{t_{ox}}{\epsilon_{ox}} \sqrt{2q\epsilon_{si}N_a} 2\phi_f$$

$$\phi_f = \frac{kT}{q} \ln \frac{N_a}{n_i}$$

$$\phi_f = .30 \text{ V}$$

$$2\phi_f = .60 \text{ V}$$

$$\frac{t_{ox}}{\epsilon_{ox}} \sqrt{2q\epsilon_{si}N_a} 2\phi_f = .12 \text{ V}$$

at point 'a':

$$V_{T_a} = V_{FB_a} + .60 \text{ V} + .12 \text{ V}$$

$$V_{T_a} = +.24 \text{ V} + .60 \text{ V} + .12 \text{ V}$$

$$\boxed{V_{T_a} = .96 \text{ V}}$$

at point 'b':

$$V_{T_b} = V_{FB_b} + .60 \text{ V} + .12 \text{ V}$$

$$V_{T_b} = -.86 + .60 \text{ V} + .12 \text{ V}$$

$$\boxed{V_{T_b} = -.14 \text{ V}}$$

d)  $W_{max}$  is the same for both 'a' & 'b'

(or  
 $W_T$ )

$$W_{max} = \sqrt{\frac{2 \epsilon_{si}}{q N_a} 2 \phi_f}$$

$$W_{max} = .88 \mu m$$

e.) Draw a C-V curve for the structure

$C_{min} = C_{ox}$  in series with  $C_{dep}$  (depletion)

$$C_{dep} = \frac{\epsilon_s}{W} = \frac{(11.7)(8.854 \times 10^{-14} \frac{F}{cm})}{(.88 \times 10^{-4} cm)}$$

$$C_{dep} = 1.18 \times 10^{-8} \frac{F}{cm^2}$$

$$\frac{1}{C_{min}} = \frac{1}{C_{dep}} + \frac{1}{C_{ox}}$$

$$C_{min} = \frac{C_{dep} C_{ox}}{C_{dep} + C_{ox}}$$

$$C_{min} = 1.07 \times 10^{-8} \frac{F}{cm^2}$$

$$C_{ox} = 1.15 \times 10^{-7} \frac{F}{cm^2}$$

$$C_{min} = 1.07 \times 10^{-8} \frac{F}{cm^2}$$

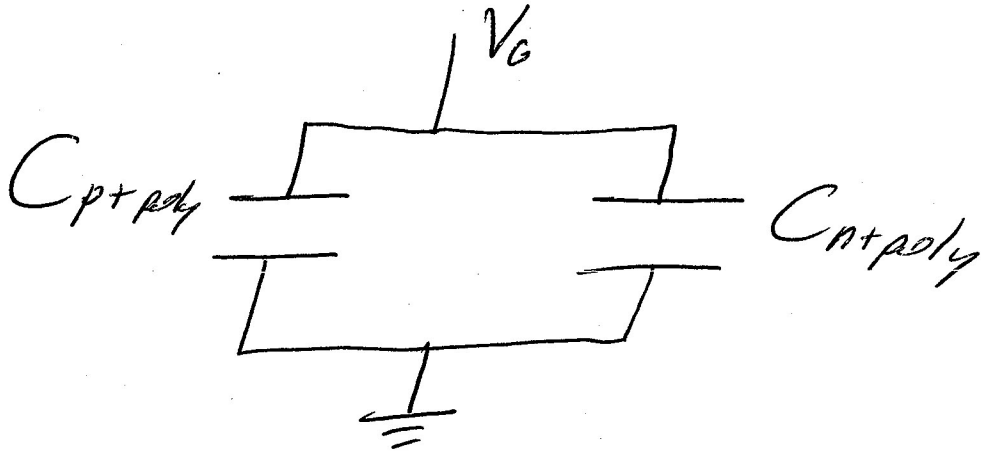
$$V_{FBa} = .24V$$

$$V_{FBb} = -.86V$$

$$V_{T_a} = .96V$$

$$V_{T_b} = -.14V$$

Now this device is essentially two capacitors in parallel



The area for both capacitors is

$$A = (L)(Z) = (5\mu m)(10\mu m)$$

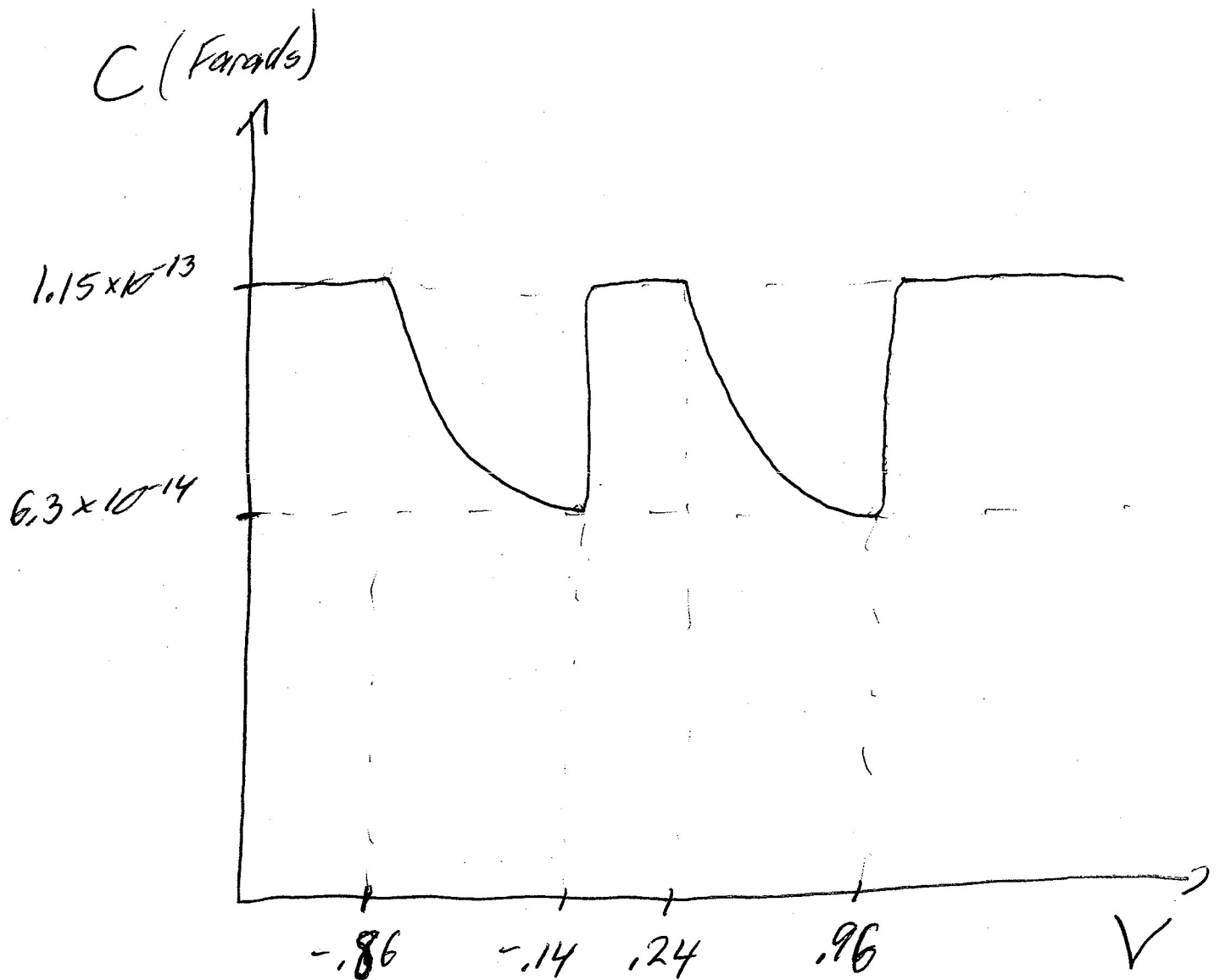
$$A = 5.0 \times 10^{-7} cm^2$$

$$(C_{ox})A = 5.75 \times 10^{-14} \text{ F}$$

$$(C_{min})A = 5.35 \times 10^{-15} \text{ F}$$

$$2 C_{ox} A = 1.15 \times 10^{-13} \text{ F}$$

$$C_{min}A + C_{ox}A = 6.3 \times 10^{-14} \text{ F}$$



(4.) a) Yes, but only a little. The substrate is highly doped and the gate oxide is very thin. Both of these mitigate short channel effects. So one would likely see velocity saturation and channel length modulation, but only a little  $V_T$  lowering and no punch-through at standard  $V_d$ .

$$b) V_T = V_{FB} + 2\phi_f + \frac{\epsilon_{ox}}{t_{ox}} \sqrt{2q\epsilon_s n_a} 2\phi_f + \Delta V_T (V_T \text{ lowering})$$

$$\Delta V_T = -\frac{q N_a W_T}{C_{ox}} \frac{r_j}{L} \left( \sqrt{1 + \frac{2W_T}{r_j}} - 1 \right)$$

$$q\phi_f = E_f - E_i = kT \ln \frac{N_a}{n_i} \approx .42V \quad 2\phi_f \approx .83V$$

$$W_T = \sqrt{\frac{2\epsilon}{qN_a}} 2\phi_f \approx .1\mu m$$

$$r_j = .2\mu m \quad L = .5\mu m$$

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} = 8.63 \times 10^{-7} \text{ F/cm}^2$$

$$\Delta V_T \approx -.03V$$



I'll use  $\mu_n \approx 400 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}$  but any reasonably lower number is fine

$$I_d = \frac{(1.5 \mu\text{m}) (400 \frac{\text{cm}^2}{\text{V}\cdot\text{s}}) (9.63 \times 10^{-7} \frac{\text{F}}{\text{cm}^2}) (1 - .18\text{V})^2}{2(1.5 \mu\text{m})}$$

$$I_d = .24 \text{ mA}$$

d.) The  $\text{HfO}_2$  will have the bigger effect on  $V_T$  because  $\epsilon_{\text{ox}}$  is explicitly in the term  $\frac{\epsilon_{\text{ox}}}{t_{\text{ox}}} \sqrt{2q \epsilon_{\text{Si}} N_A} 2\phi_F$ .  
The strained silicon has a higher mobility but this does not directly affect  $V_T$  & the strain impact on  $\epsilon_{\text{Si}}, E_g, n_i$  etc... is relatively small.

e.) C-V Transistor 1:  $V_T = -.18\text{V}$   
 $V_{FB} = -1.17\text{V}$   
 $C_{\text{ox}} = 9.63 \times 10^{-7} \frac{\text{F}}{\text{cm}^2}$   
 $C_{\text{min}} = C_{\text{HF}} = \frac{C_{\text{ox}}}{1 + \frac{\epsilon_{\text{ox}} W_T}{\epsilon_{\text{Si}} t_{\text{ox}}}}$

$$C_{\text{min}} \approx \frac{C_{\text{ox}}}{9.3} \approx 9.3 \times 10^{-8} \frac{\text{F}}{\text{cm}^2}$$

Transistor 2:

$V_{FB}$  same as Trans. #1

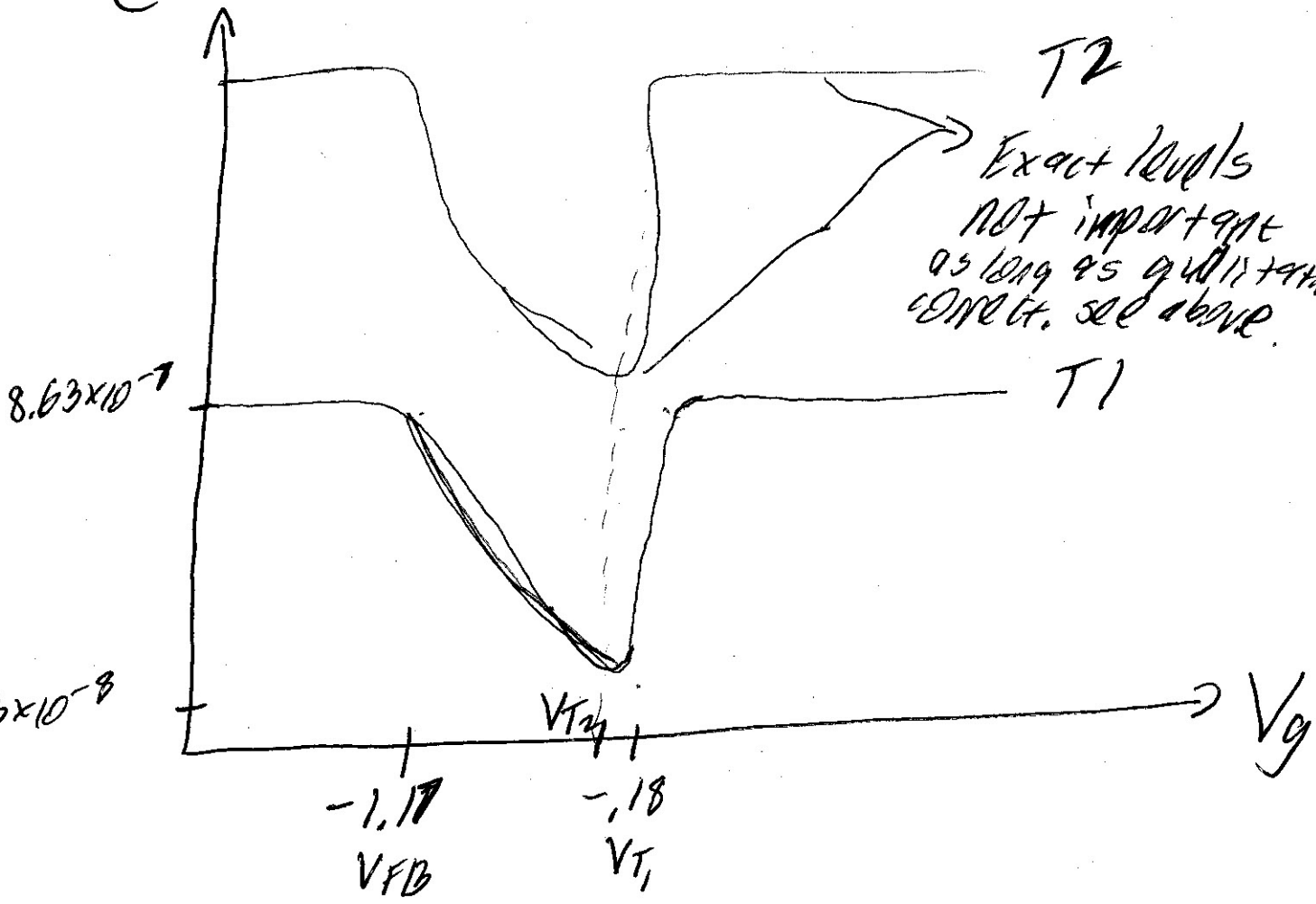
$V_T$  will be slightly lower because

$$\epsilon_{HfO_2} > \epsilon_{SiO_2}$$

$C_{ox}$  will be <sup>much</sup> higher ( $\epsilon_{HfO_2}$ )

$C_{min}$  will be higher for same reason

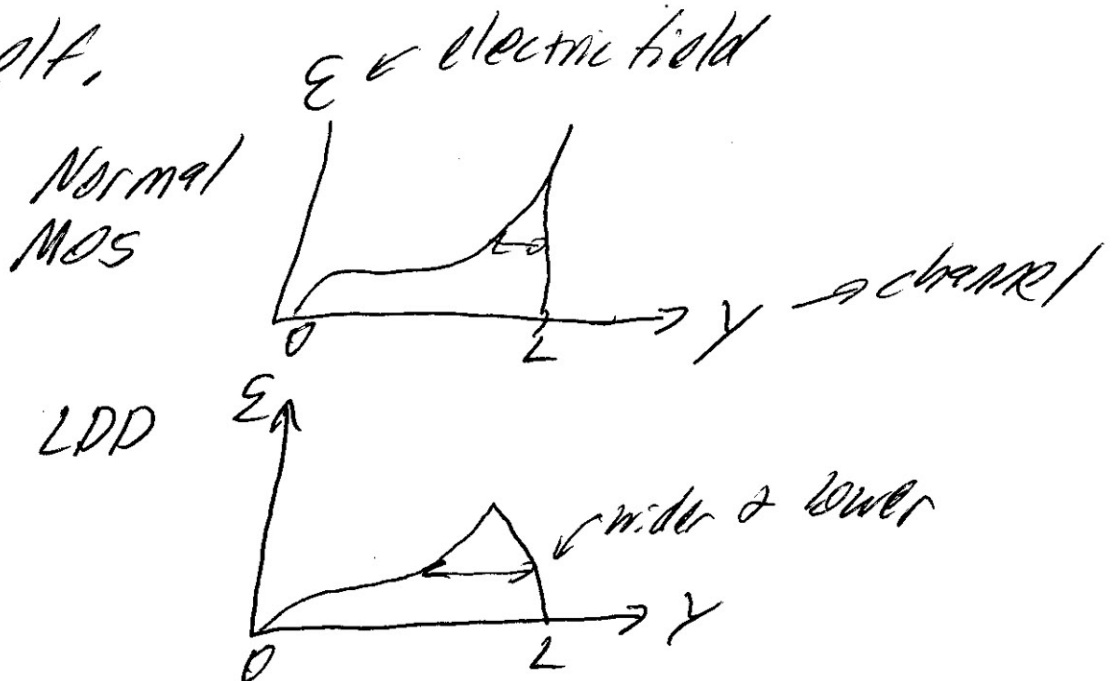
$C$  (F/cm<sup>2</sup>)





5. LDD

a.) LDD reduces hot carriers because the "pinch off" region is extended by the n-region. The light doping acts as a resistor + drops some of the voltage across itself.



b.) The charge in the channel is  $\sim C_{ox}(V_g - V_t)$ . As  $V_g$  increases, the charge density increases and begins to exceed the level of n- in the lightly doped regions.

